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## 10. Influence Propagation in Social Networks

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Adapted from

<http://keg.cs.tsinghua.edu.cn/jietang/publications/WSDM13-tutorial-social-influence-analysis.pptx>

# Course Content

- Collection of three main topics of high recent interest.
  - Search engines (Crawling, Indexing, Ranking)
    - Language Modeling
    - Text Indexing and Crawling
    - Relevance Ranking
    - Link Analysis Algorithms
  - Text Processing (NLP, NER, Sentiments)
    - Natural Language Processing
    - Named Entity Recognition
    - Sentiment Analysis
    - Summarization
  - Social networks (Properties, Influence Propagation)
    - Social Network Analysis
    - **Influence Propagation in Social Networks**

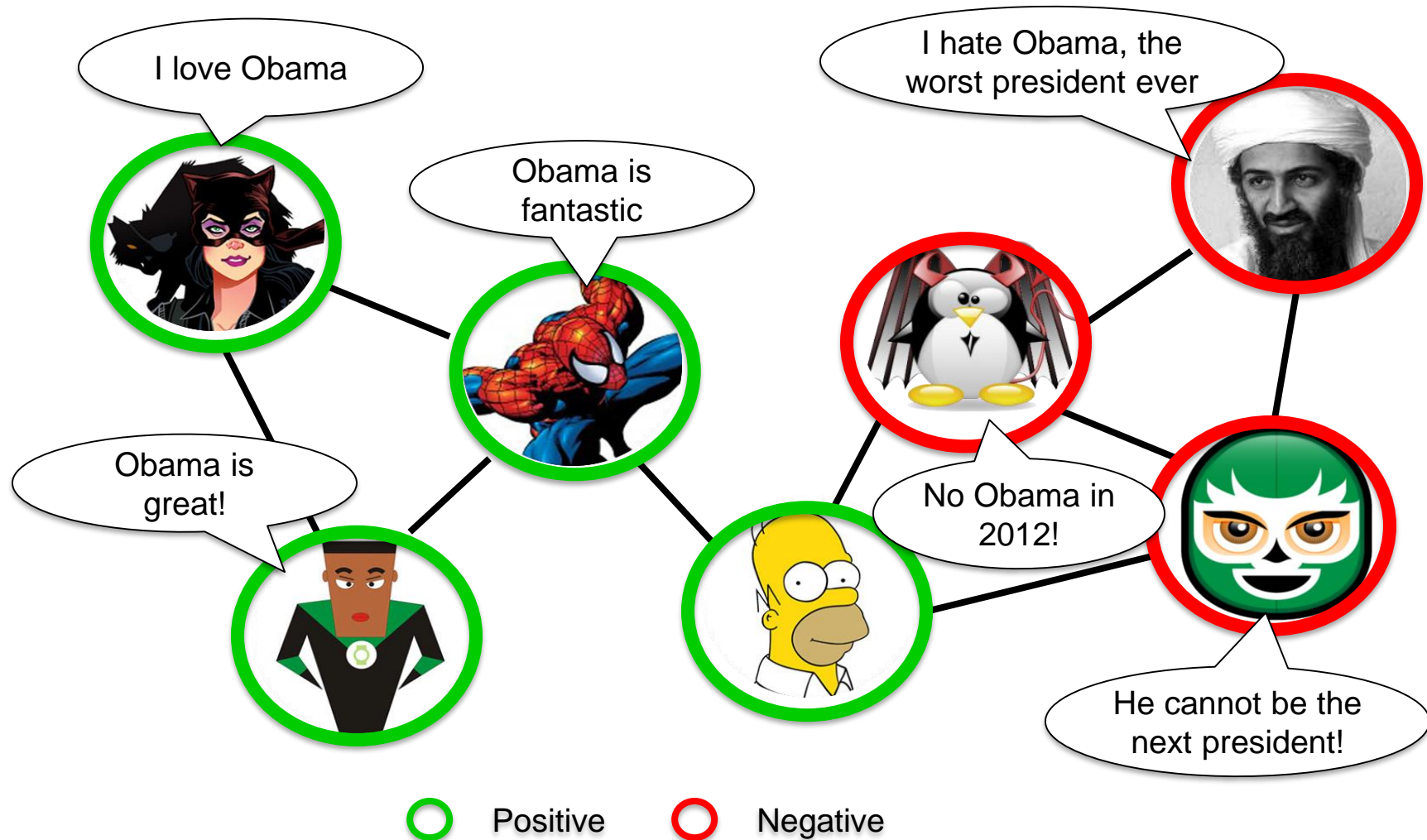
# Scale of Social Networks Data

- Twitter
  - A billion registered of which 316M are active
  - 6000 tweets per second
- Facebook
  - 1.49 billion monthly active users
    - 8 new users join every second
    - 0.5M likes every minute
    - 1.3M pieces of content shared every minute
    - 350M photo uploads per day
    - 31.25M messages per minute
- Instagram
  - 300M+ users
  - 48611 photos posted per minute
- Whatsapp
  - 700M users
  - 30B messages per day
- LinkedIn
  - 17361 profile views per minute
- Tinder
  - 694444 swipes per minute
- Youtube
  - 300 hours of video uploaded per minute
- Vine
  - 1041666 video loops per minute

# Today's Agenda

- Does social influence really matter?

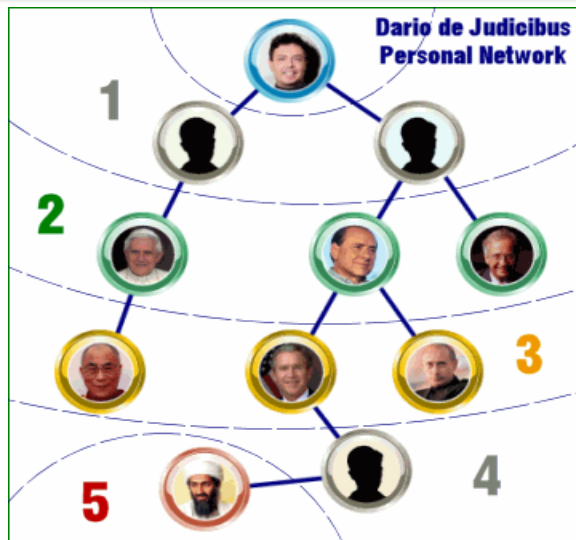
# “Love Obama” or “Hate Obama”?



# Three Degree of Influence

- Social influence occurs when one's **opinions**, **emotions**, or **behaviors** are affected by others, intentionally or unintentionally.<sup>[1]</sup>

## Six degree of separation<sup>[2]</sup>



## Three degree of Influence<sup>[3]</sup>



You can **influence** >1,000,000 persons in the world, according to the **Dunbar's number**<sup>[4]</sup>. Humans can comfortably maintain 150 stable relationships

[1] [http://en.wikipedia.org/wiki/Social\\_influence](http://en.wikipedia.org/wiki/Social_influence)

[2] S. Milgram. The Small World Problem. Psychology Today, 1967, Vol. 2, 60–67

[3] J.H. Fowler and N.A. Christakis. The Dynamic Spread of Happiness in a Large Social Network: Longitudinal Analysis Over 20 Years in the Framingham Heart Study. British Medical Journal 2008; 337: a2338

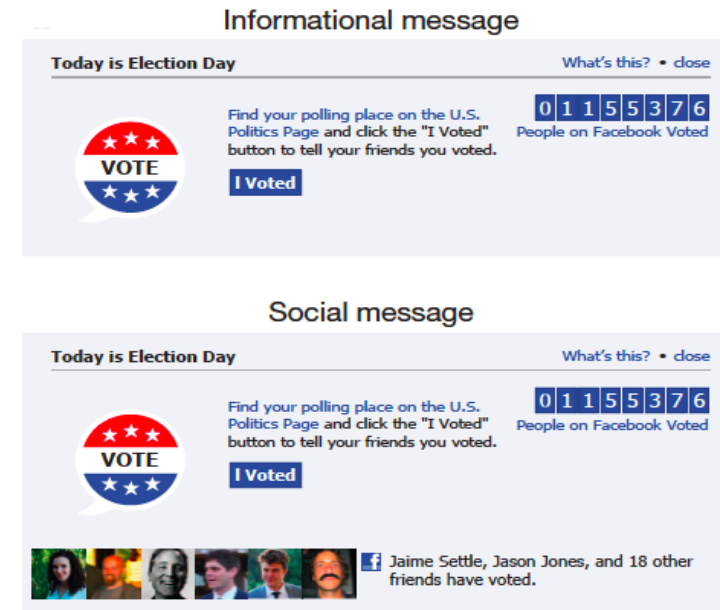
[4] R. Dunbar. Neocortex size as a constraint on group size in primates. Human Evolution, 1992, 20: 469–493.

# Does Social Influence really matter?

- **Case 1:** Social influence and political mobilization<sup>[1]</sup>
  - Will online political mobilization really work?

## **A controlled trial** (with 61M users on FB)

- **Social msg group:** was shown a msg that indicates one's friends who have made the votes.
- **Informational msg group:** was shown a msg that indicates how many others voted.
- **Control group:** did not receive any msg.



Social msg group were 2.08% more likely to click on the “I Voted” button compared to the info msg group. Also, social msg group were 0.39% more likely to **actually vote** (via examination of public voting records) than control group.

## Case 2: Klout<sup>[1]</sup>—Social Media Marketing

- Toward measuring real-world influence
  - Twitter, Facebook, G+, LinkedIn, etc.
  - Klout generates a score on a scale of 1-100 for a social user to represent her/his ability to engage other people and inspire social actions.
- Though controversial<sup>[2]</sup>, in May 2012, Cathay Pacific opened SFO lounge to Klout users
  - A high Klout score gets you into Cathay Pacific's SFO lounge

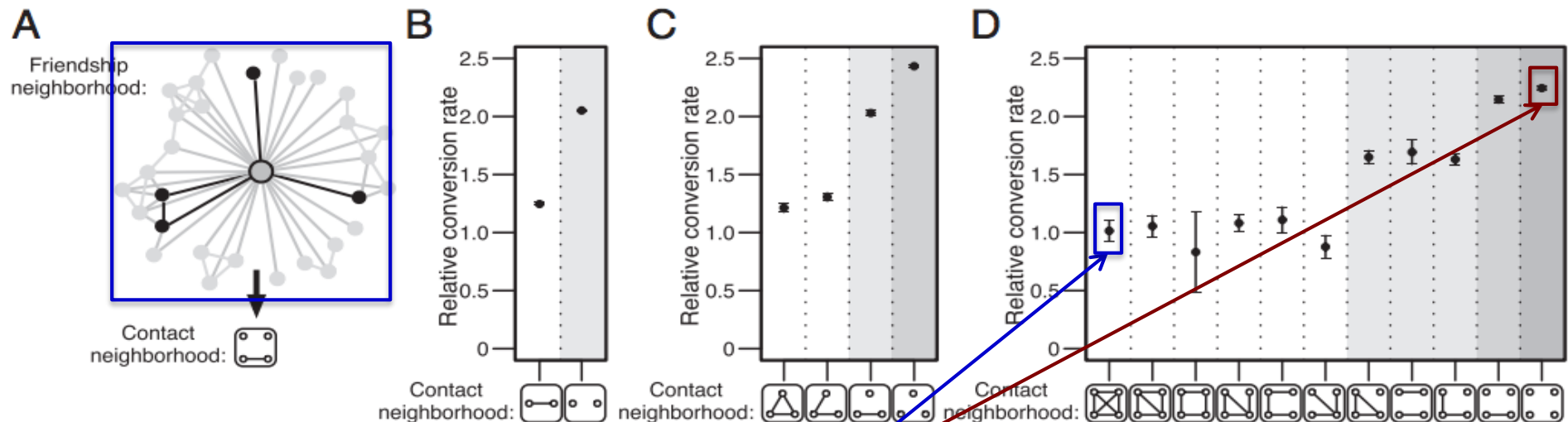
[1] <http://klout.com>

[2] Why I Deleted My Klout Profile, by Pam Moore, at Social Media Today, originally published November 19, 2011; retrieved November 26 2011



# Case 3: Who Influenced you and How?

- Magic: the structural diversity of the ego network<sup>[1]</sup>



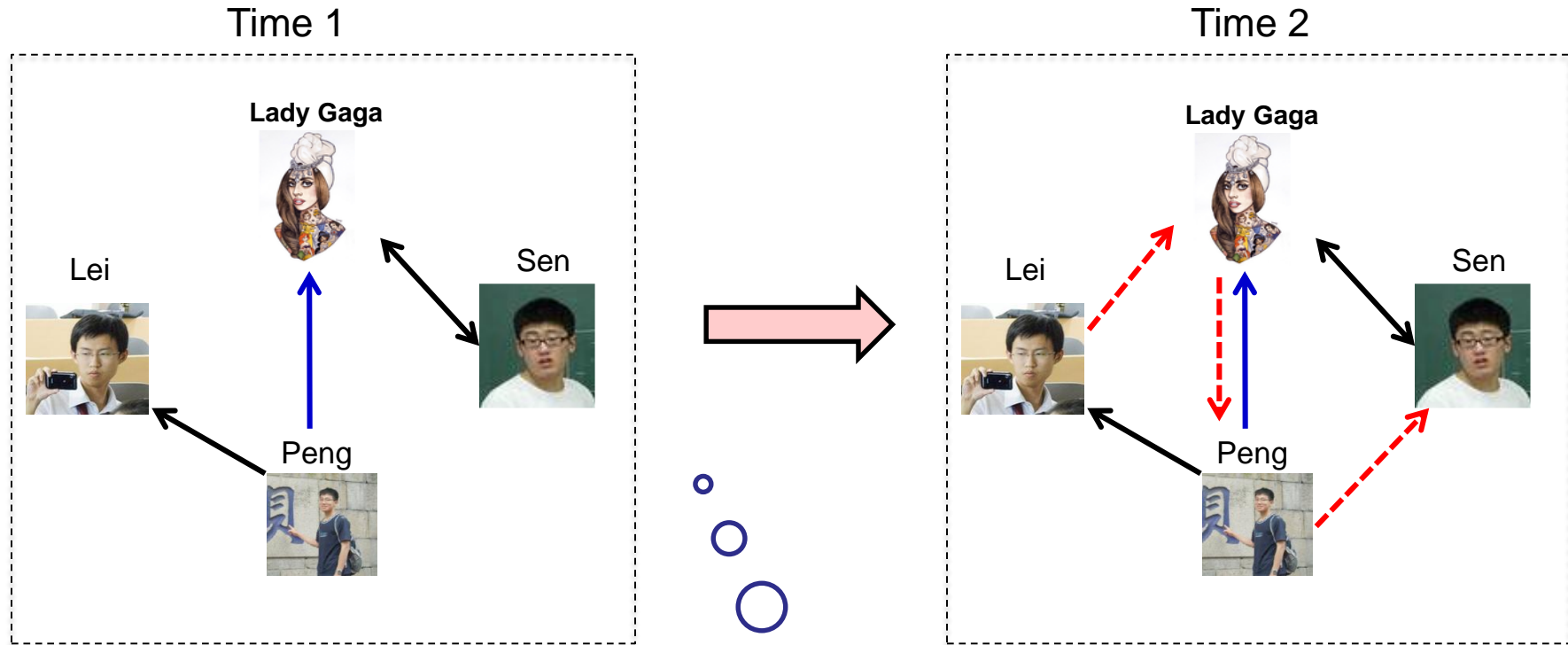
**Results:** Your behavior is influenced by the “structural diversity” (the number of connected components in your ego network) instead of the number of your friends.

[1] J. Ugander, L. Backstrom, C. Marlow, and J. Kleinberg. Structural diversity in social contagion. PNAS, 109 (20):7591-7592, 2012.

# Today's Agenda

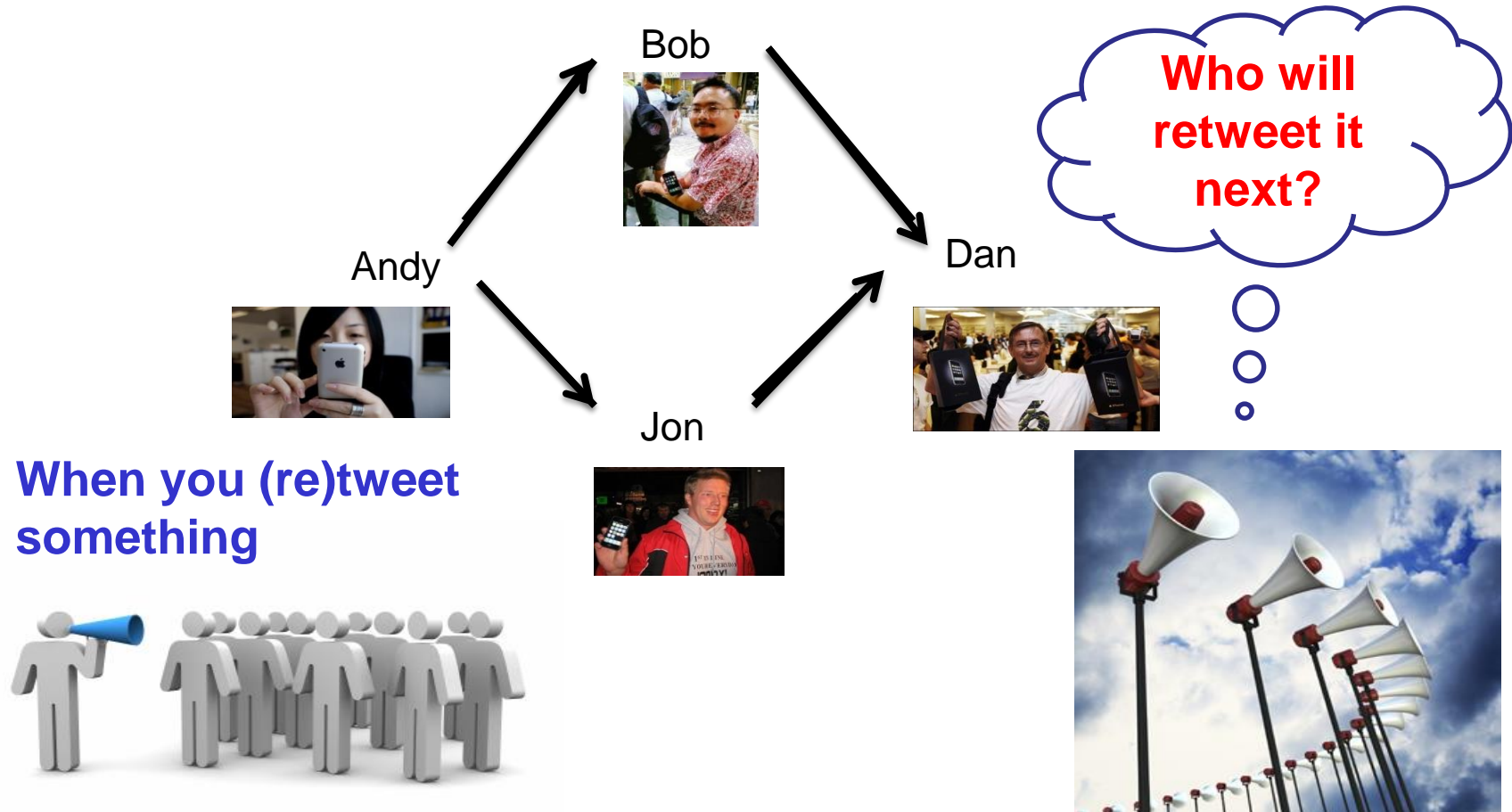
- Does social influence really matter?
- Examples of social influence

# Types of Social Influence: Follow Influence on Twitter



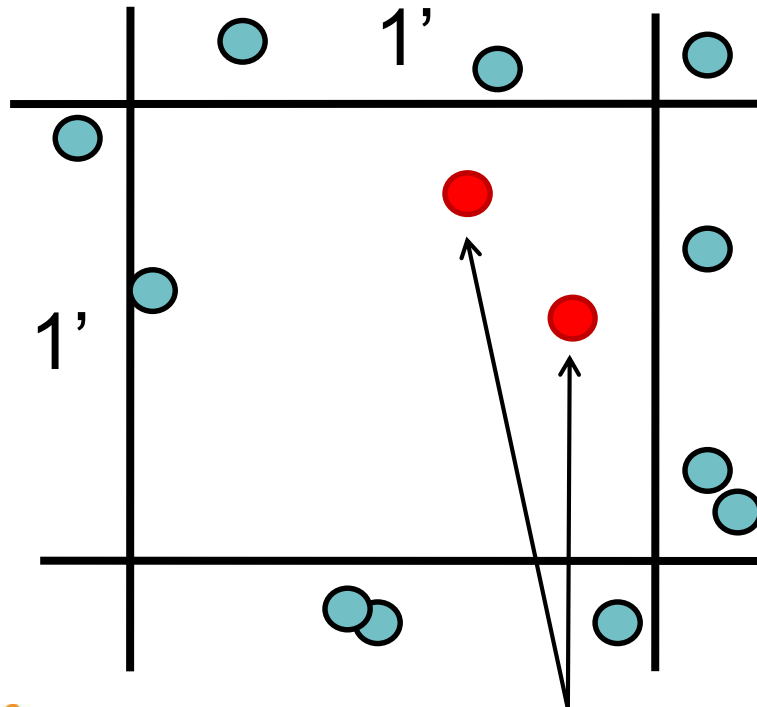
When you **follow** a user in a social network, will the behavior **influence** your friends to also follow her?

# Types of Social Influence: Retweet Influence

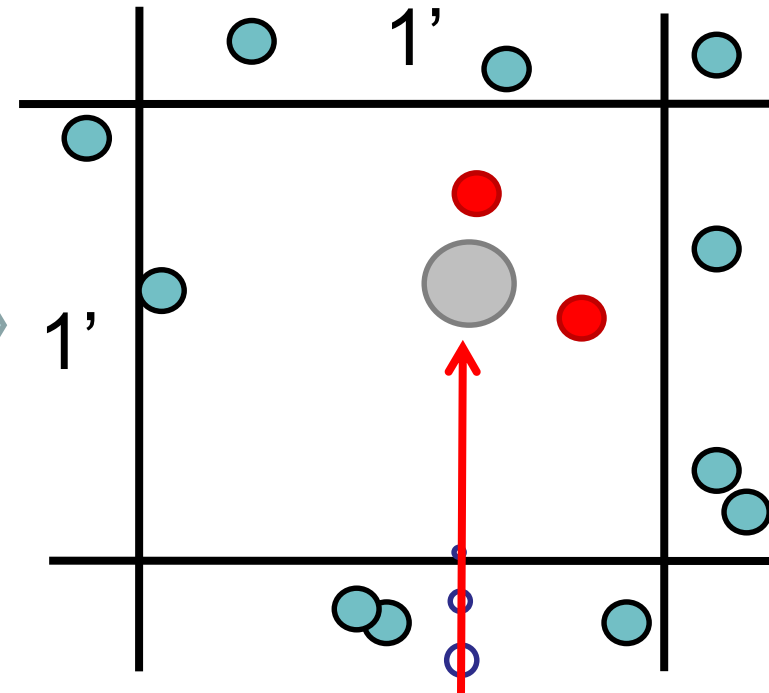
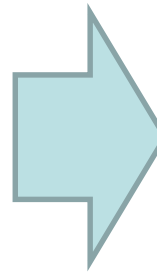


# Types of Social Influence: Check-in Influence in Gowalla

Legend     Alice     Alice's friend     Other users



If Alice's friends check in this location at time  $t$



Will Alice also check in nearby?



# Today's Agenda

- Does social influence really matter?
- Examples of social influence
- **Ways of measuring social influence**

# Test for Existence of Social Influence

- Randomized Control Trials (RCT)
  - People are randomly assigned to a “treatment” group or a “controlled” group;
  - People in the treatment group receive some kind of “treatment”, while people in the controlled group do not receive the treatment;
  - Compare the result of the two groups, e.g., survival rate with a disease with/without a treatment.
- Two challenges:
  - How to define the **treatment group** and the **controlled group**?
  - How to find a real **random** assignment?

[1] Rubin, D. B. 1974. Estimating causal effects of treatments in randomized and nonrandomized studies. Journal of Educational Psychology 66, 5, 688–701.

[2] [http://en.wikipedia.org/wiki/Randomized\\_experiment](http://en.wikipedia.org/wiki/Randomized_experiment)

# Example: Political mobilization

- There are two kinds of treatments.

## A controlled trial

- Social msg group:** was shown with msg that indicates one's friends who have made the votes.
- Informational msg group:** was shown with msg that indicates how many others voted.
- Control group:** did not receive any msg.

Treatment for Group 1

Treatment for Group 2



Treatment for Group 1

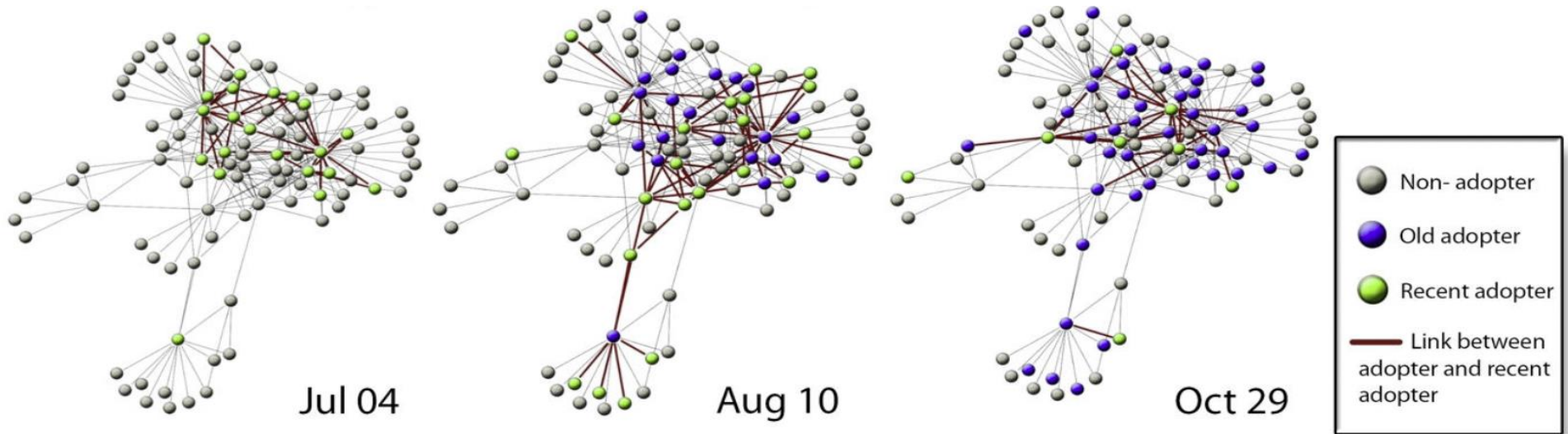
Treatment for Group 1&2

[1] R. M. Bond, C. J. Fariss, J. J. Jones, A. D. I. Kramer, C. Marlow, J. E. Settle and J. H. Fowler. A 61-million-person experiment in social influence and political mobilization. Nature, 489:295-298, 2012.



# Adoption Diffusion of Y! Go (1)

Yahoo! Go is a product of Yahoo to access its services of search, mailing, photo sharing, etc.

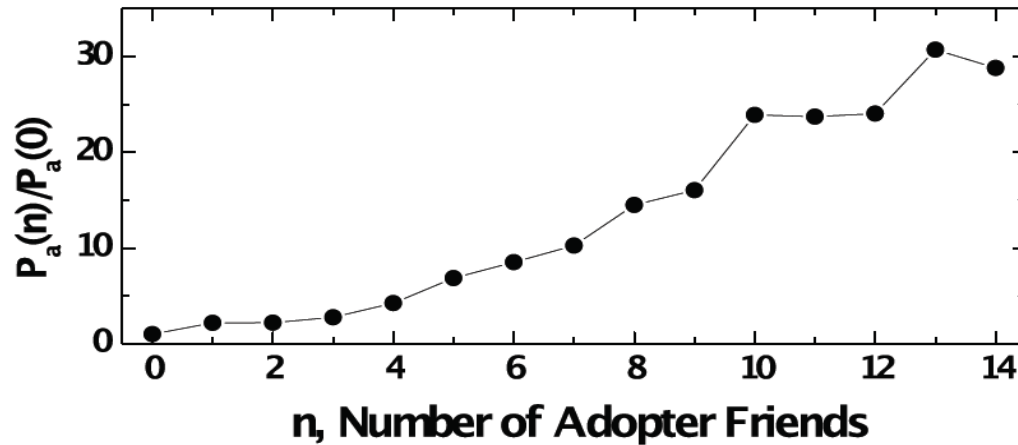


## RCT:

- **Treatment group:** people who adopted Y! Go and also have friend(s) who adopted Y! Go at time  $t$ ;
- **Controlled group:** people who adopted Y! Go and have no friends who adopted Y! Go at time  $t$ .

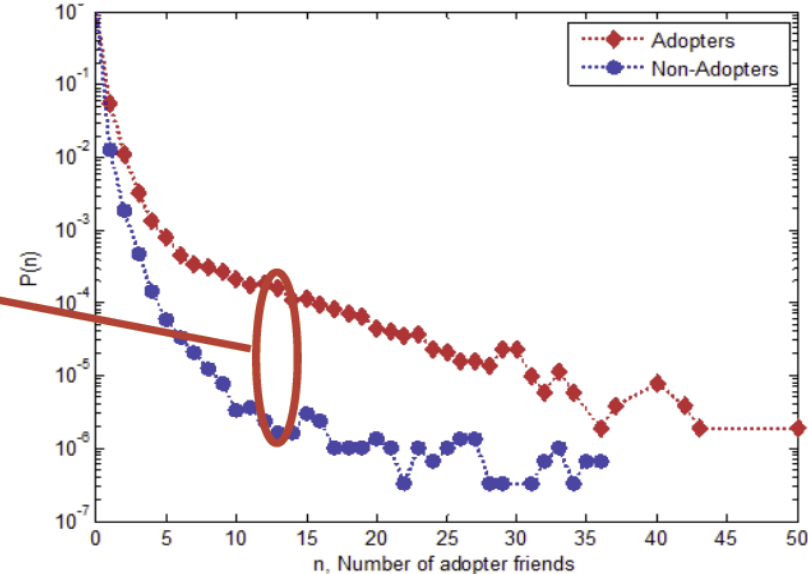
[1] S. Aral, L. Muchnik, and A. Sundararajan. Distinguishing influence-based contagion from homophily-driven diffusion in dynamic networks. PNAS, 106 (51):21544-21549, 2009.

# Evidence of Influence?



The ratio of the likelihood of adoption given  $n$  adopter friends  $P_a(n)$  and the likelihood of adoption given 0 adopter friends  $P_a(0)$  where the number of adopter friends is assessed at the time of adoption.

**Adopters are 100 times more likely to have 12 adopter friends than non-adopters**

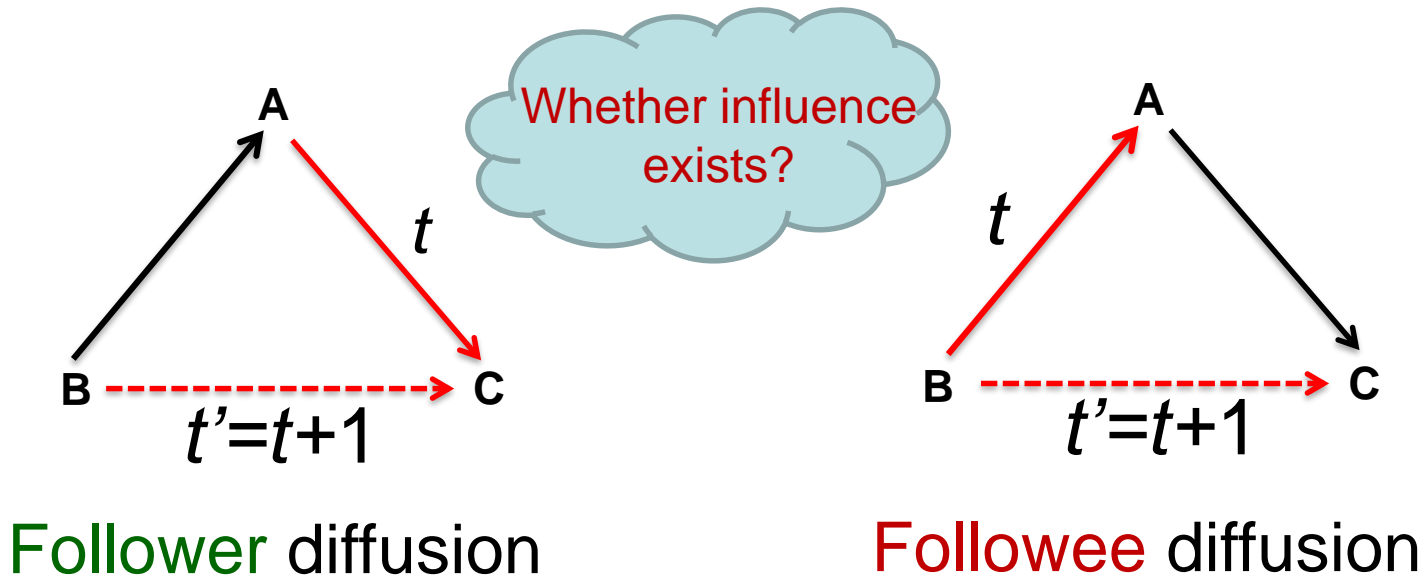


# Two More Methods

- **Shuffle test:** shuffle the activation time of users.
  - If social influence does not play a role, then the timing of activation should be independent of the timing of activation of others.
- **Reverse test:** reverse the direction of all edges.
  - Social influence spreads in the direction specified by the edges of the graph, and hence reversing the edges should intuitively change the estimate of the correlation.

# Influence Test via Triad Formation

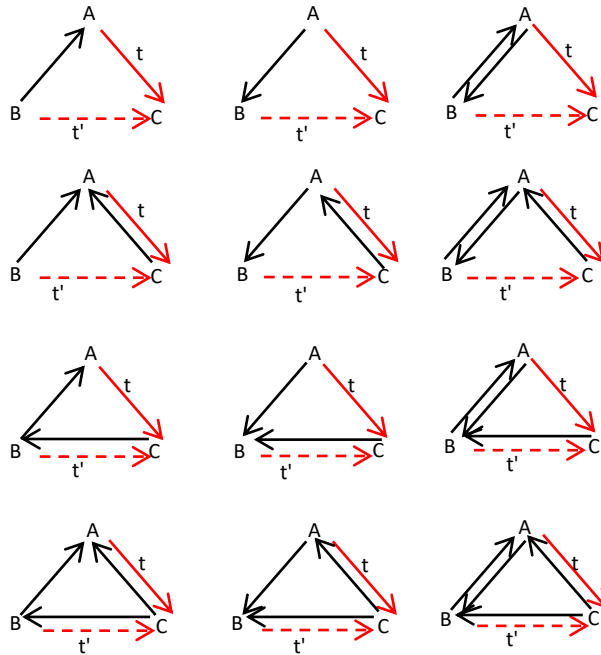
## Two Categories of Following Influences



- : pre-existed relationships
- : a new relationship added at  $t$
- >: a possible relationship added at  $t+1$

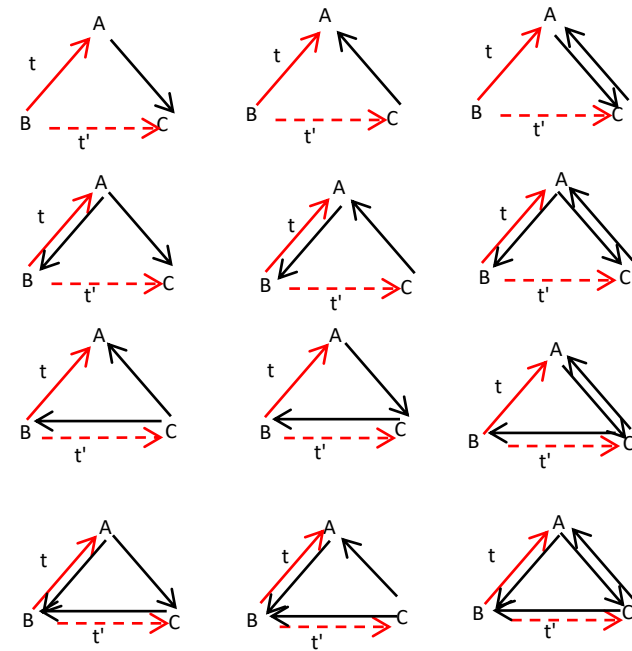
# 24 Triads in Following Influence

## Follower diffusion



12 triads

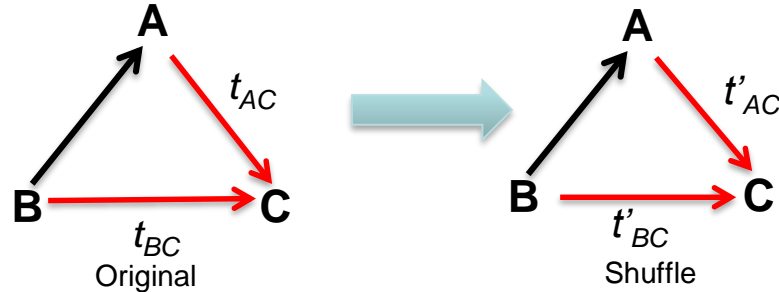
## Followee diffusion



12 triads

# Timing Shuffle Test

- Method: Shuffle the timing of all the following relationships.

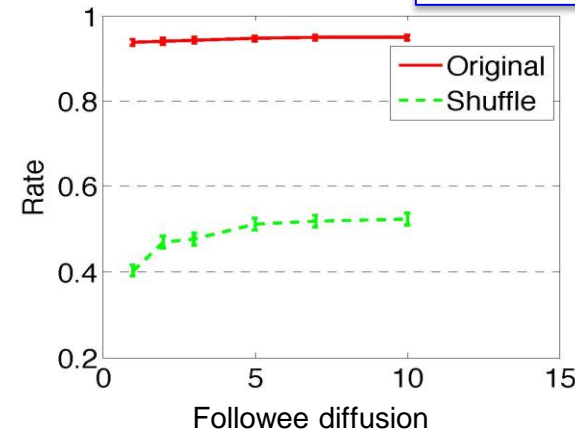
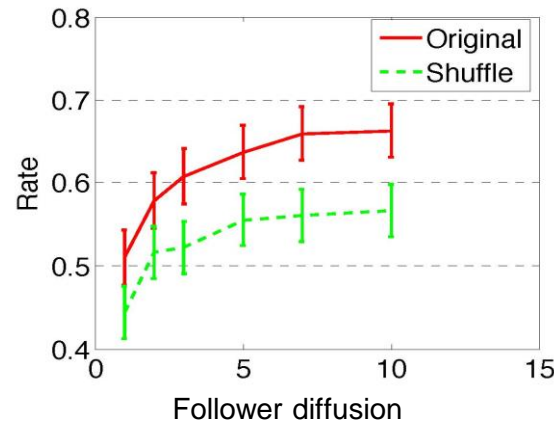


**Shuffle test**

$$Rate = \frac{\#Triad \mid 0 < t_{BC} - t_{AC} < d}{\#Triad \mid t_{BC} \text{ and } t_{AC} \text{ exist}}$$

- Compare the rate under the original and shuffled dataset.

- Result



**t-test,  $P < 0.01$**

[1] A. Anagnostopoulos, R. Kumar, M. Mahdian. Influence and correlation in social networks. In KDD, pages 7-15, 2008.

# Reachability-based Method<sup>[1]</sup>

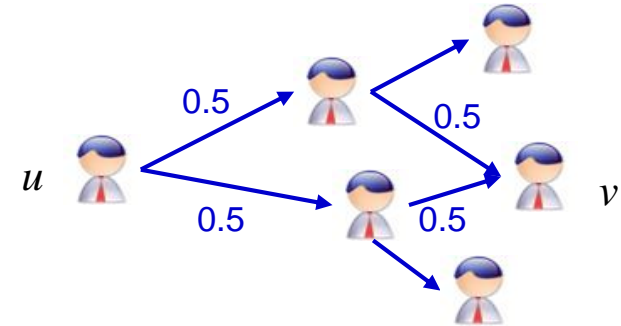
- PageRank, Random Walk with Restart
- Influence of a path

$$\text{inf}(p) = \prod_{v_i \in p} \frac{1}{\text{outdeg}(v_i)}$$

- Influence of user  $u$  on  $v$

$$\text{influence}(u, v) = \lim_{t \rightarrow \infty} \sum_{p \in \text{path}_t(u, v)} \text{inf}(p)$$

All paths from  $u$  to  $v$  within path length  $t$



$$\begin{aligned} \text{Influence}(u, v) \\ = 0.5 * 0.5 + 0.5 * 0.5 \end{aligned}$$

**Note:** The method only considers the network information and does not consider the content information

[1] G. Jeh and J. Widom. Scaling personalized web search. In WWW '03, pages 271-279, 2003.

# Action-based Methods: Learning Influence Probabilities [1]

- **Goal:** Learn user influence from historical actions
- **Assumption**
  - If user  $v_i$  performs an action  $y$  at time  $t$  and later his friend  $v_j$  also perform the action, then there is an influence from  $v_i$  to  $v_j$
- **User Influenceability:** quantifies how influenceable a user is.

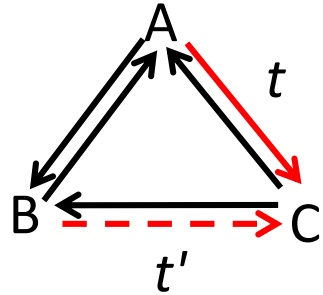
$$\text{influence}(v_i) = \frac{|\{y \mid \exists v_j, Dt : \text{prop}(y, v_i, v_j, Dt) \wedge t \geq Dt \geq 0\}|}{Y_{v_i}}$$

where  $\Delta t = t_j - t_i$  is the difference between the time when  $v_j$  performing the action and the time when user  $v_i$  performing the action, given  $e_{ij}=1$ .

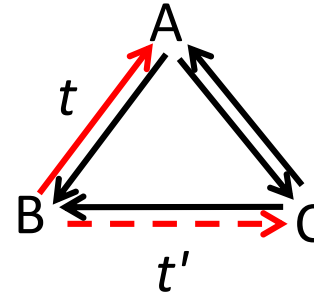
[1] A. Goyal, F. Bonchi, and L. V. Lakshmanan. Learning influence probabilities in social networks. In WSDM'10, pages 207–217, 2010.



# Social Theories: Structural Balance<sup>[1]</sup>



Follower diffusion



Followee diffusion

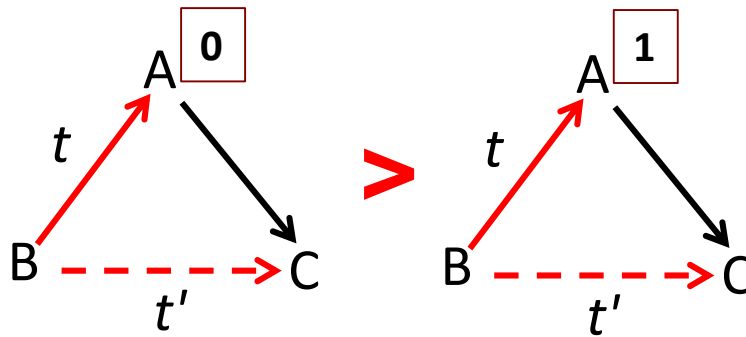
**Social Balance:** my friend's friend is also my friend

**Explanation:** Users have tendency to form a balanced triad

Fritz Heider (1958). The Psychology of Interpersonal Relations. John Wiley & Sons.

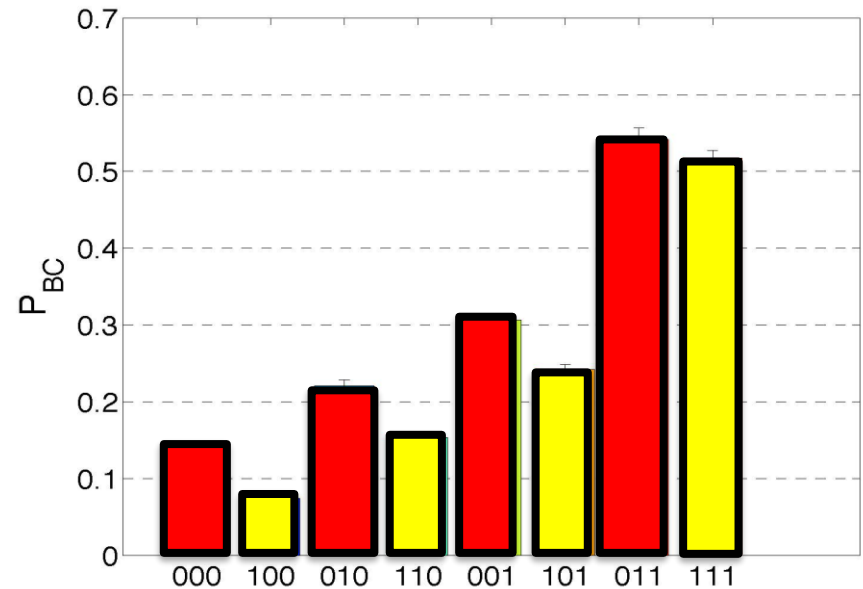
# Social Theories: Social Status

Followee diffusion:  $P(0XX) > P(1XX)$



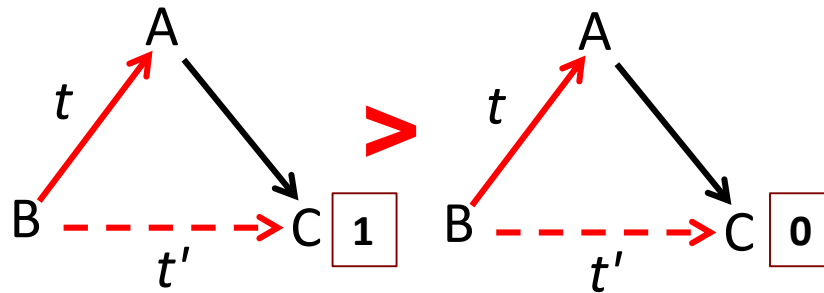
- Low-status users act as a bridge to connect users so as to form a closure triad.
- The likelihood of 0XX is 1.4 times of 1XX.

1: Elite user  
0: Low-status user



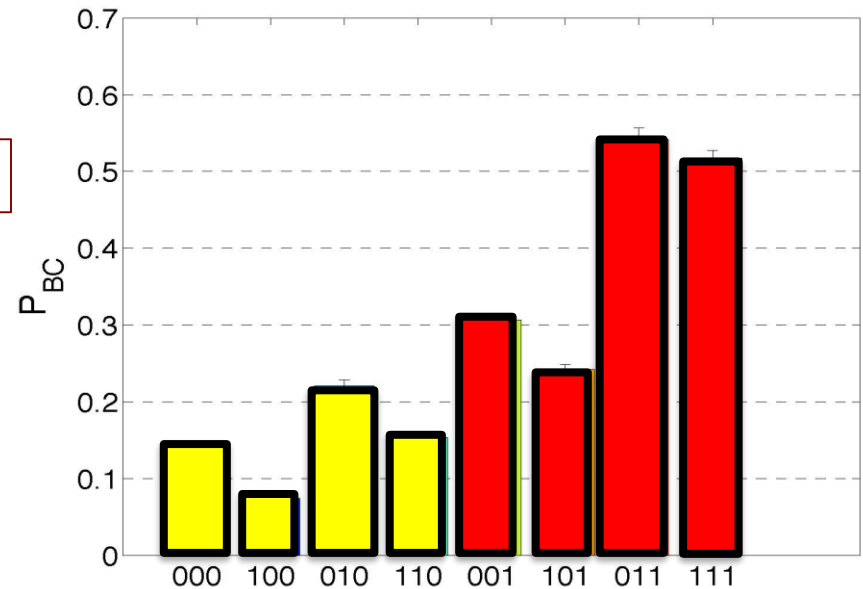
# Social Theories: Social Status

Followee diffusion:  $P(XX1) > P(XX0)$

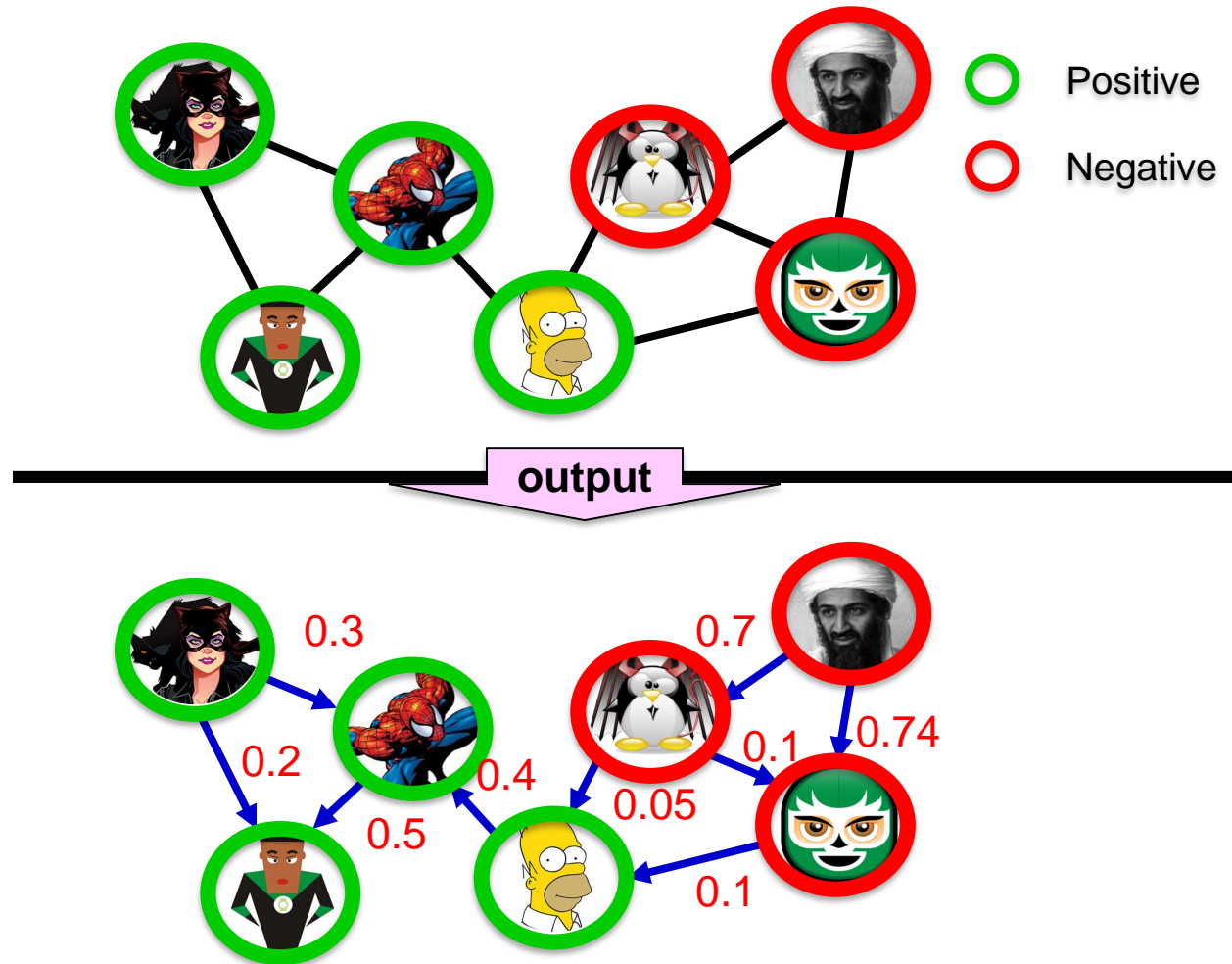


- The rich gets richer.
- The likelihood of XX1 is nearly 2 times higher than that of XX0.
- This phenomenon validates the mechanism of preferential attachment.

1: Elite user  
0: Low-status user



# Output of Measuring Social Influence



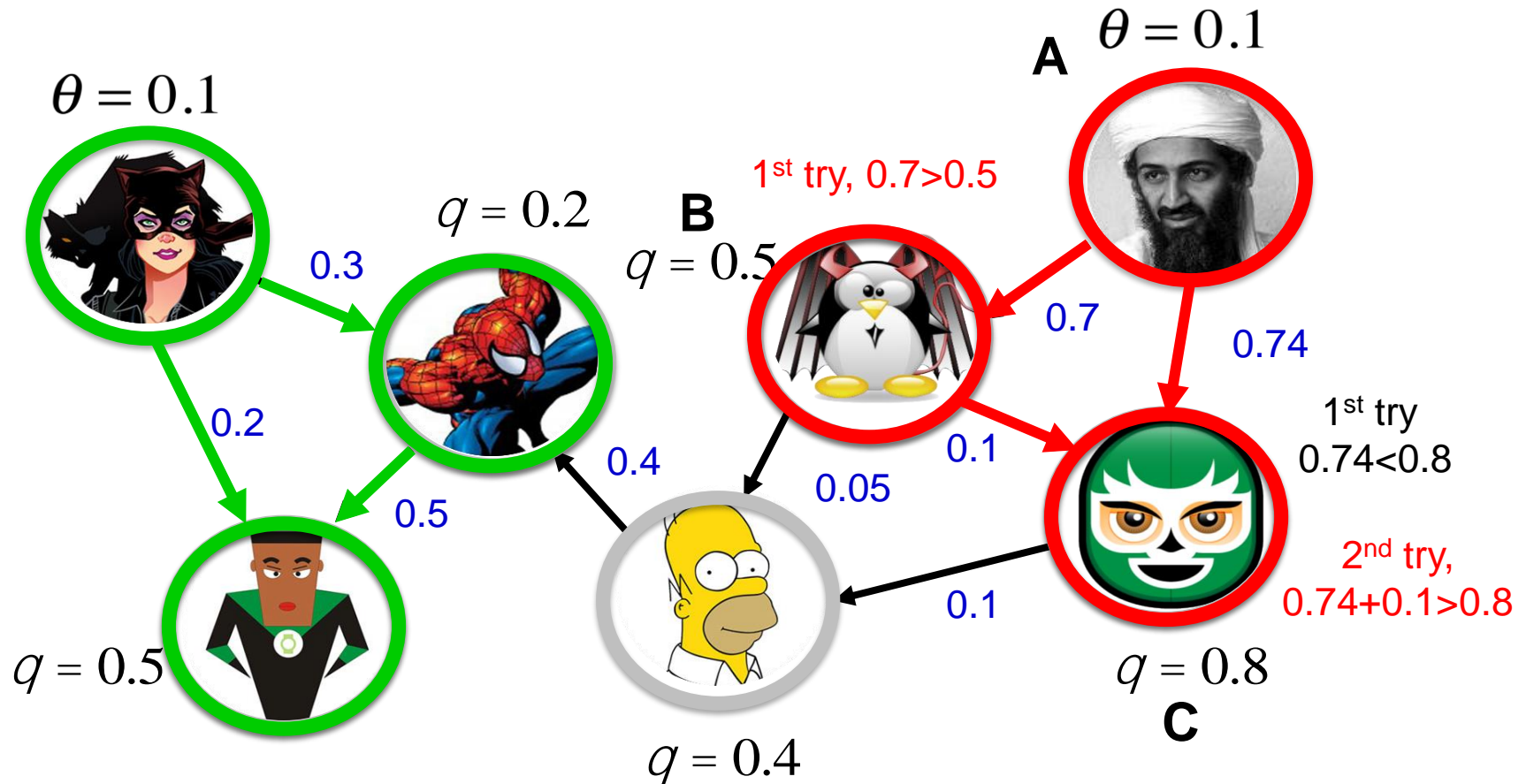
# Today's Agenda

- Does social influence really matter?
- Examples of social influence
- Ways of measuring social influence
- **Models for social influence analysis**

# Models for Social Influence Analysis

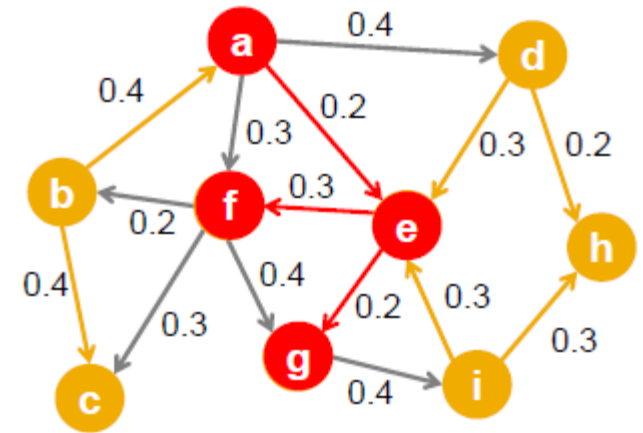
- Decision based models
  - Models of product adoption, decision making
    - A node observes decisions of its neighbors and makes its own decision
    - E.g., You join demonstrations if at least  $k$  (*threshold*) of your friends do so too
    - Linear Threshold Model
- Probabilistic Models
  - Models of influence or disease spreading
    - An infected node tries to “push” the contagion to an uninfected node
    - E.g., You “catch” a disease with some prob. from each active neighbor in the network
    - Cascade Model

# Linear Threshold Model: An Example



# Probabilistic Models: Independent Cascade Model

- Initially some nodes  $S$  are active
- Each edge  $(u,v)$  has probability (weight)  $p_{uv}$
- When node  $v$  becomes active
  - It activates each out-neighbor  $v$  with prob.  $p_{uv}$
- Activations spread through the network
- Independent cascade model is simple but requires many parameters!

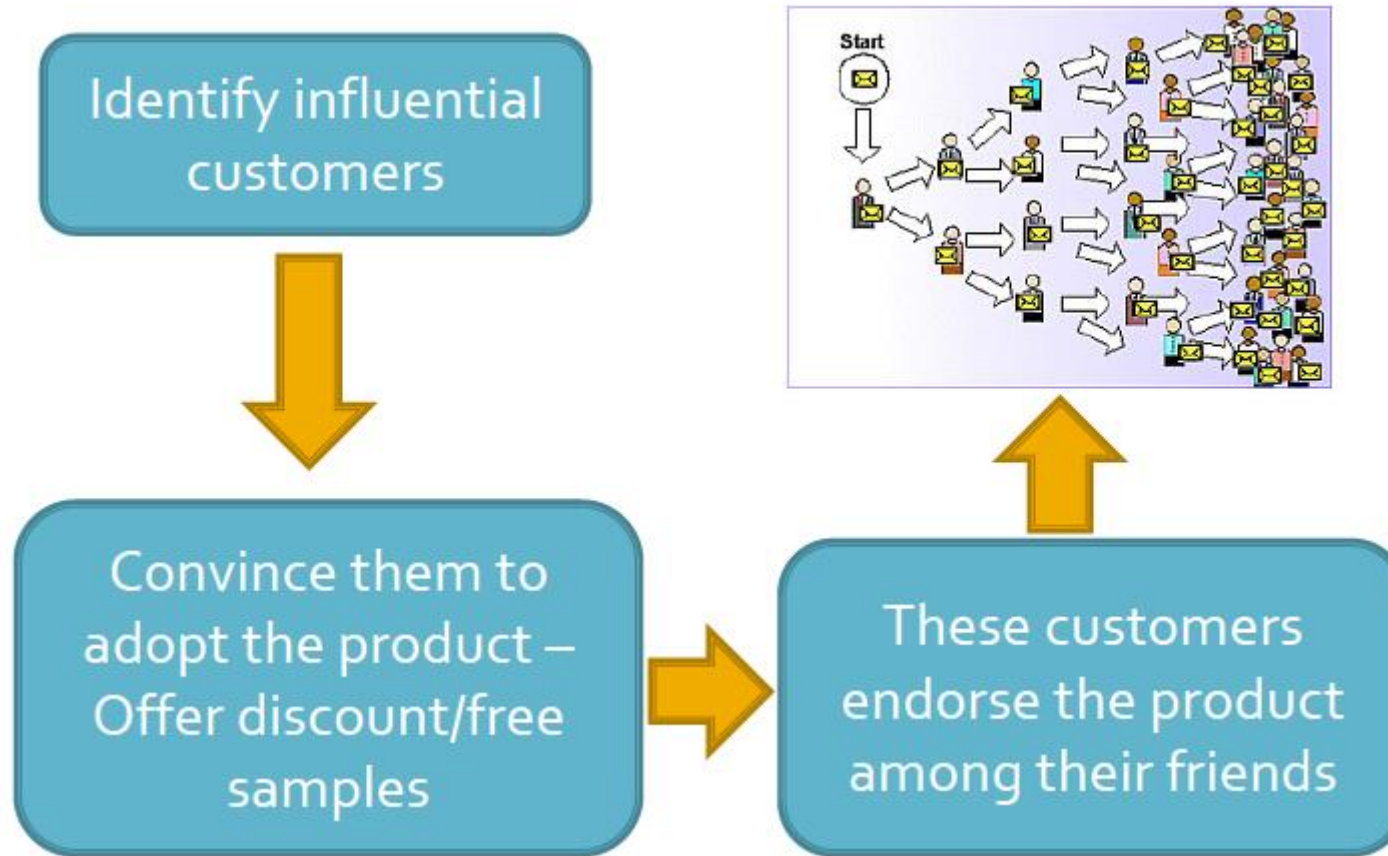




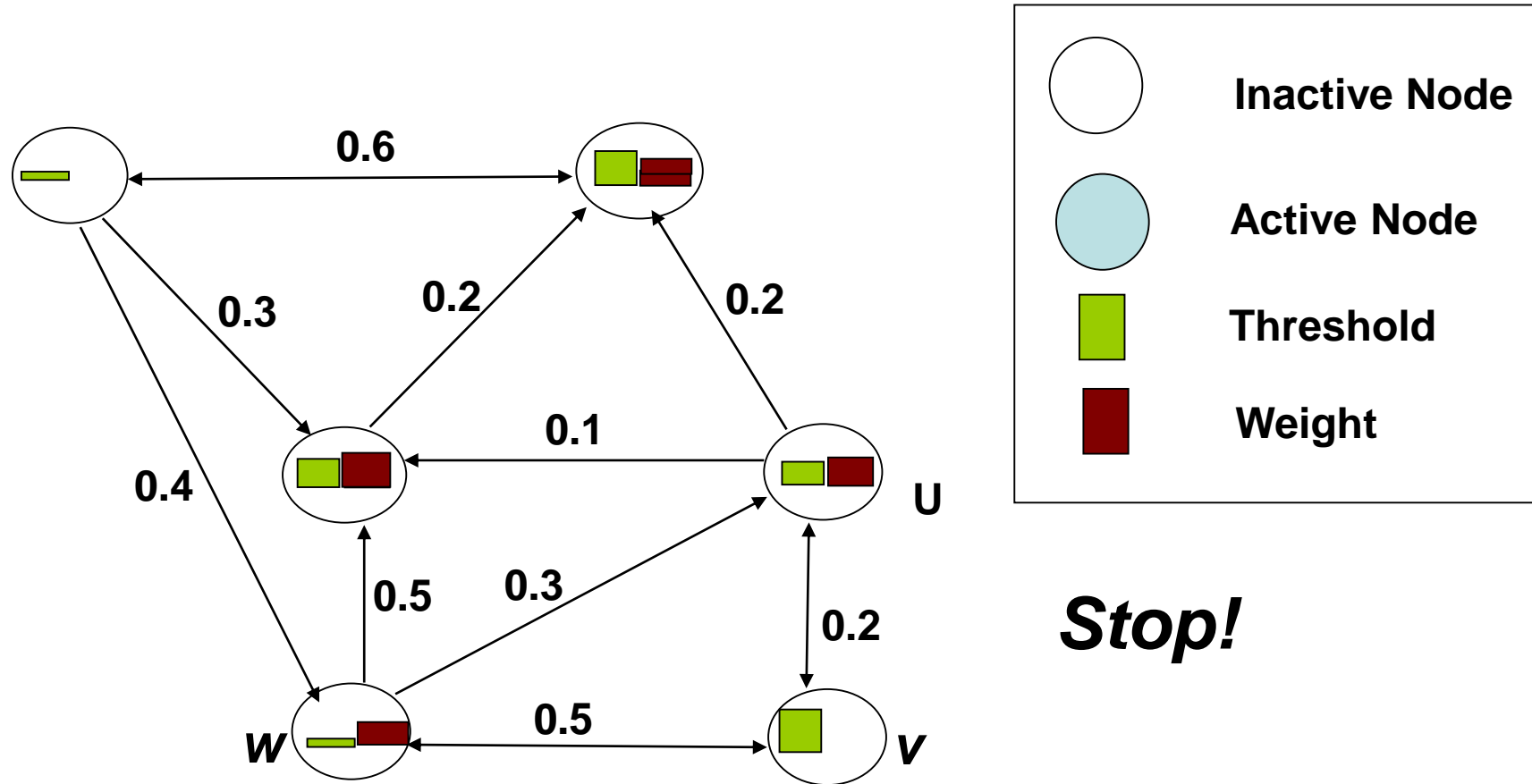
# Today's Agenda

- Does social influence really matter?
- Examples of social influence
- Ways of measuring social influence
- Models for social influence analysis
- **The influence maximization problem**

# Why Maximize Influence?



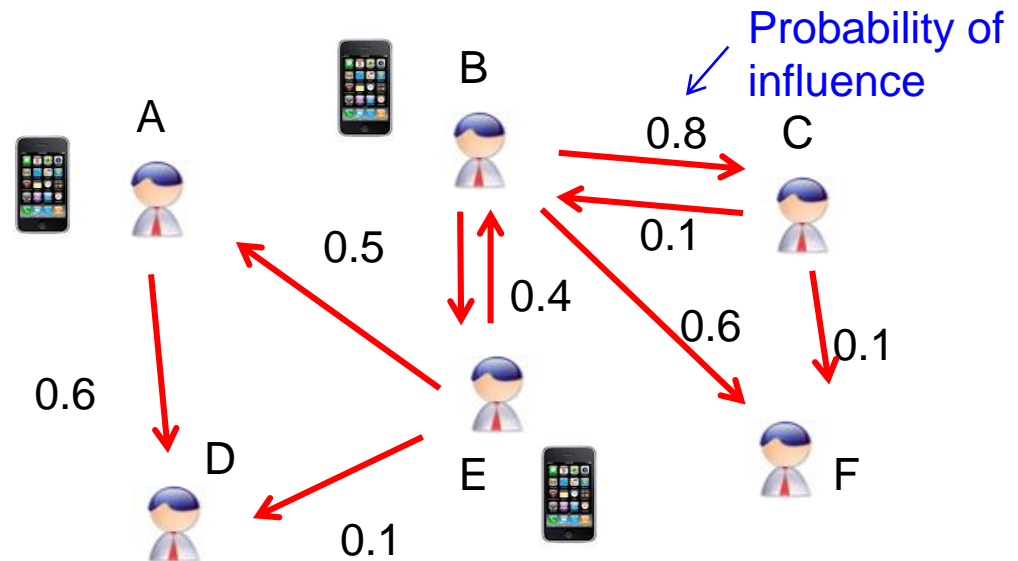
# Who is influential? Influence Spread



Source: David Kempe's slides

# Influence Maximization

- Influence of a set of nodes  $A$ , i. e.,  $\sigma(A)$ , is the number of active nodes at the end of the process starting from  $A$ .
- Problem Definition:
  - Given a parameter  $k$ , find a  $k$ -node set  $A$  to maximize  $\sigma(A)$ .
- It is an NP-hard problem.



# Influence Maximization Problem

- Find an approximation algorithm for the influence maximization problem.
- Using a greedy algorithm, one can obtain a  $(1-1/e)$  optimal result
- Greedy Algorithm
  - Start with an empty set  $A$
  - Choose an element that provides the largest marginal increase in the function value  $\sigma(A)$ .
  - Until  $|A| = k$

# Algorithms

- General Greedy
  - In each round, the algorithm adds one vertex into the selected set  $S$  such that this vertex together with current set  $S$  maximizes the influence spread.
    - Involves running random cascade model from each node
- Low-distance Heuristic: nodes with the shortest paths to other nodes as seed nodes
  - Individuals are more likely to be influenced by those who are closely related to them.
- High-degree heuristic
  - Nodes with more neighbors would arguably tend to impose more influence upon its direct neighbors.
- Degree Discount Heuristic
  - If  $u$  has been selected as a seed, then when considering selecting  $v$  as a new seed based on its degree, we should not count the edge  $v \rightarrow u$  and also edges from  $v$  to  $u$ 's influence set.

# Take-away Messages

- We discussed basics of social influence and observed examples where social influence is prominent.
- We discussed various tests to test for existence of social influence.
- We studied the decision based and probabilistic models for Social Influence Analysis
- We also visited the Influence Maximization and studied various approximate and heuristic solutions

# Further Reading

- Jimeng Sun, Jie Tang: A Survey of Models and Algorithms for Social Influence Analysis. 177-214. Social Network Data Analytics. Springer. 2011
- Chapter 19 and 21 of “Easley-Kleinberg” book
  - <http://www.cs.cornell.edu/home/kleinber/networks-book/>
- R. M. Bond, C. J. Fariss, J. J. Jones, A. D. I. Kramer, C. Marlow, J. E. Settle and J. H. Fowler. A 61-million-person experiment in social influence and political mobilization. Nature, 489:295-298, 2012.
- P. Domingos and M. Richardson. Mining the network value of customers. In Proceedings of the seventh ACM SIGKDD international conference on Knowledge discovery and data mining (KDD’01), pages 57–66, 2001.



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