



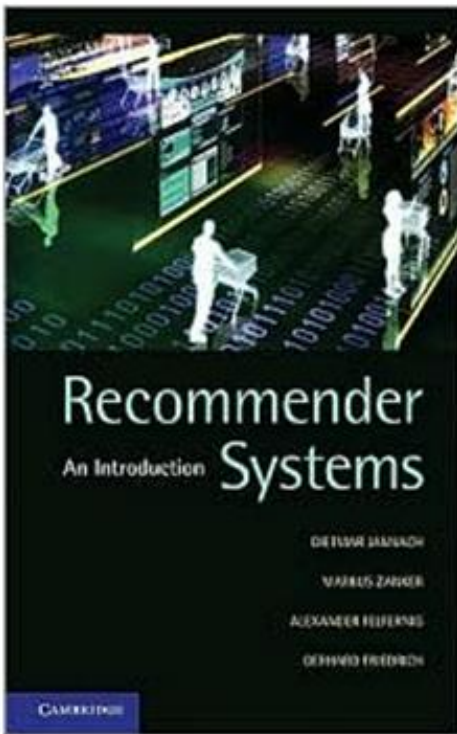
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Collaborative Filtering

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Recommender Systems: An Introduction

by [Dietmar Jannach](#), [Markus Zanker](#), [Alexander Felfernig](#), [Gerhard Friedrich](#)

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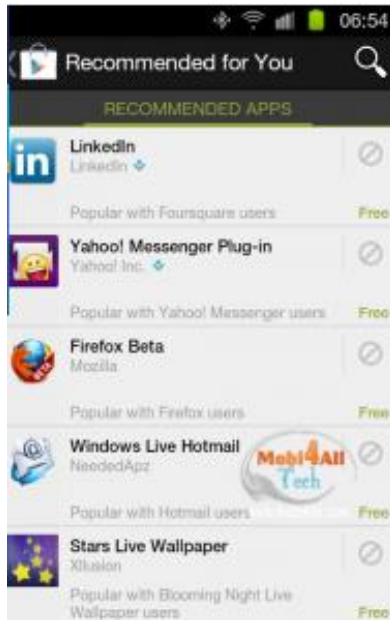
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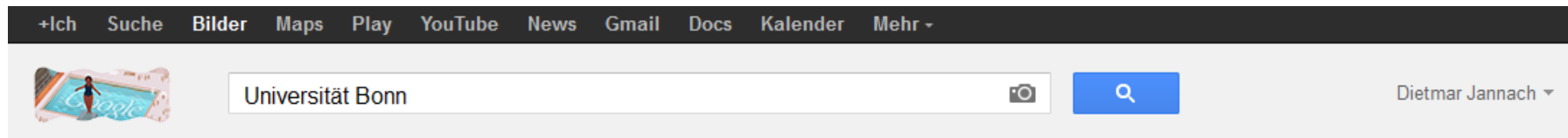


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Even more ...

- Personalized search



- "Computational Advertising"

A collage of three personalized advertisements. The top-left ad shows a woman's profile picture and a blue box, followed by the text 'gefällt Danubius Hotels in Bad Bük und Bad Sárvár.' Below this is a small image of a couple in a pool and the text 'Danubius Hotels in Bad Bük und Bad Sárvár' with a thumbs-up icon and 'Gefällt mir'. The top-right ad is titled 'Gewinne Deine Insel' with the URL 'bahamas.canusa.de', an image of a tropical island, and the text 'Hast Du Lust auf Urlaub auf Deiner eigenen Insel? Dann spiel mit!'. The bottom-right ad is titled 'Citroën Austria', features an image of a red car, and the text 'Genieße Sommer-Feeling pur mit den CITROËN Sommer-Collection Modellen.'

Why use Recommender Systems?

- Value for the customer
 - Find things that are interesting
 - Narrow down the set of choices
 - Help me explore the space of options
 - Discover new things
 - Entertainment
 -
- Value for the provider
 - Additional and probably unique personalized service for the customer
 - Increase trust and customer loyalty
 - Increase sales, click through rates, conversion etc.
 - Opportunities for promotion, persuasion
 - Obtain more knowledge about customers

Real-World Check

- Myths from industry
 - Amazon.com generates X percent of their sales through the recommendation lists ($30 < X < 70$)
 - Netflix (DVD rental and movie streaming) generates X percent of their sales through the recommendation lists ($30 < X < 70$)
- There must be some value in it
 - See recommendation of groups, jobs or people on LinkedIn
 - Friend recommendation and ad personalization on Facebook
 - Song recommendation at last.fm
 - News recommendation at Forbes.com (plus 37% CTR)
- Academia
 - A few studies exist that show the effect
 - increased sales, changes in sales behavior

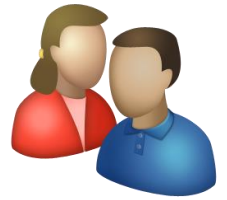
Problem Domain

- Recommendation systems (RS) help to match users with items
 - Ease information overload
 - Sales assistance (guidance, advisory, persuasion,...)

RS are software agents that elicit the interests and preferences of individual consumers [...] and make recommendations accordingly.

They have the potential to support and improve the quality of the decisions consumers make while searching for and selecting products online.

- Different system designs / paradigms
 - Based on availability of exploitable data
 - Implicit and explicit user feedback
 - Domain characteristics



Recommender Systems

- RS seen as a function
- **Given:**
 - User model (e.g. ratings, preferences, demographics, situational context)
 - Items (with or without description of item characteristics)
- **Find:**
 - Relevance score. Used for ranking.
- **Finally:**
 - Recommend items that are assumed to be relevant
- **But:**
 - Remember that relevance might be context-dependent
 - Characteristics of the list itself might be important (diversity)

Collaborative Filtering (CF)

- The most prominent approach to generate recommendations
 - used by large, commercial e-commerce sites
 - well-understood, various algorithms and variations exist
 - applicable in many domains (book, movies, DVDs, ..)
- Approach
 - use the "wisdom of the crowd" to recommend items
- Basic assumption and idea
 - Users give ratings to catalog items (implicitly or explicitly)
 - Customers who had similar tastes in the past, will have similar tastes in the future



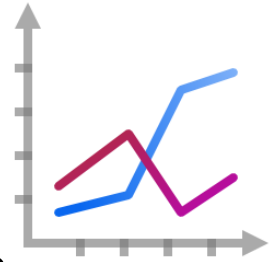
User-based kNN CF (1)

- The basic technique:
 - Given an "active user" (Alice) and an item I not yet seen by Alice
 - The *goal is to estimate Alice's rating for this item*, e.g., by
 - find a set of users (peers) who liked the same items as Alice in the past **and** who have rated item I
 - use, e.g. the average of their ratings to predict, if Alice will like item I
 - do this for all items Alice has not seen and recommend the best-rated

	Item1	Item2	Item3	Item4	Item5
Alice	5	3	4	4	?
User1	3	1	2	3	3
User2	4	3	4	3	5
User3	3	3	1	5	4
User4	1	5	5	2	1

User-based kNN CF (2)

- Some first questions
 - How do we measure similarity?
 - How many neighbors should we consider?
 - How do we generate a prediction from the neighbors' ratings?



	Item1	Item2	Item3	Item4	Item5
Alice	5	3	4	4	?
User1	3	1	2	3	3
User2	4	3	4	3	5
User3	3	3	1	5	4
User4	1	5	5	2	1

Measuring user similarity

- A popular similarity measure in user-based CF: **Pearson correlation**

a, b : users

$r_{a,p}$: rating of user a for item p

P : set of items, rated both by a and b

Possible similarity values between -1 and 1;

$$sim(a, b) = \frac{\sum_{p \in P} (r_{a,p} - \bar{r}_a)(r_{b,p} - \bar{r}_b)}{\sqrt{\sum_{p \in P} (r_{a,p} - \bar{r}_a)^2} \sqrt{\sum_{p \in P} (r_{b,p} - \bar{r}_b)^2}}$$

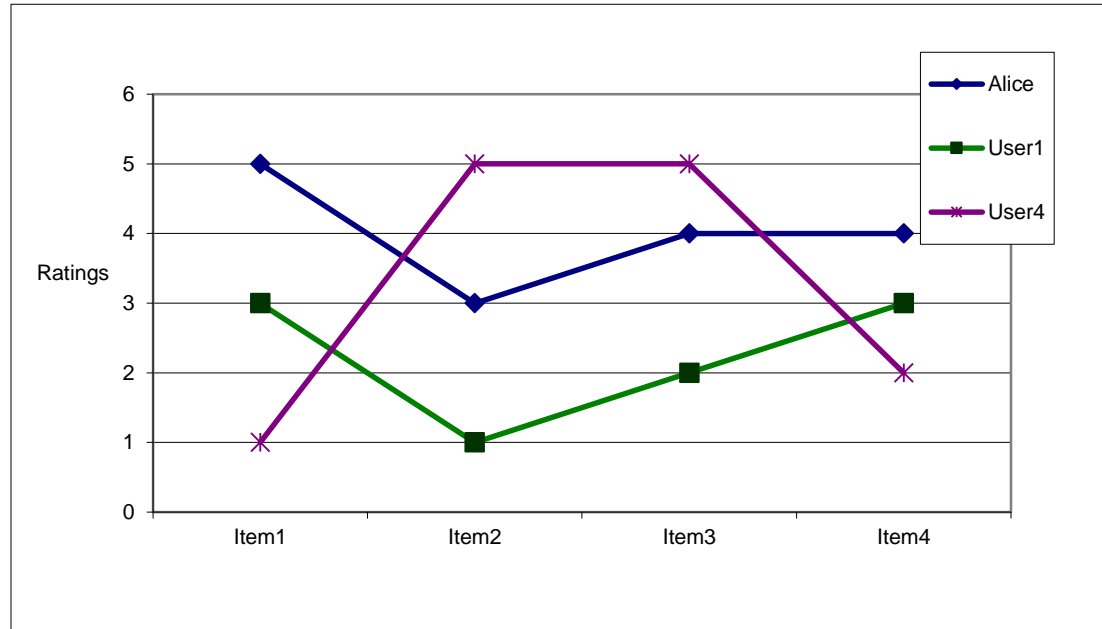
\bar{r}_a, \bar{r}_b = user's average ratings

	Item1	Item2	Item3	Item4	Item5
Alice	5	3	4	4	?
User1	3	1	2	3	3
User2	4	3	4	3	5
User3	3	3	1	5	4
User4	1	5	5	2	1

$sim = 0.85$
 $sim = 0.70$
 $sim = -0.79$

Pearson Correlation

- Takes differences in rating behavior into account



- Works well in usual domains, compared with alternative measures
 - such as cosine similarity

Making Predictions

- A common prediction function:

$$pred(a, p) = \bar{r}_a + \frac{\sum_{b \in N} sim(a, b) * (r_{b,p} - \bar{r}_b)}{\sum_{b \in N} sim(a, b)}$$



- Calculate, whether the neighbors' ratings for the unseen item i are higher or lower than their average
- Combine the rating differences – use the similarity as a weight
- Add/subtract the neighbors' bias from the active user's average and use this as a prediction

Making Recommendations

- Making predictions is typically not the ultimate goal
- Usual approach (in academia)
 - Rank items based on their predicted ratings
- However
 - This might lead to the inclusion of (only) niche items
 - **In practice also:** Take item popularity into account
- Approaches
 - "Learning to rank"
 - Optimize according to a given rank evaluation metric

Improving the Prediction Function

- Not all neighbor ratings might be equally "valuable"
 - Agreement on commonly liked items is not so informative as agreement on controversial items
 - **Possible solution:** Give more weight to items that have a higher variance
- Value of number of co-rated items
 - Use "significance weighting", by e.g., linearly reducing the weight when the number of co-rated items is low
- Case amplification
 - Intuition: Give more weight to "very similar" neighbors, i.e., where the similarity value is close to 1.
- Neighborhood selection
 - Use similarity threshold or fixed number of neighbors

Memory-based and Model-based Approaches

- User-based CF is said to be "memory-based"
 - the rating matrix is directly used to find neighbors / make predictions
 - does not scale for most real-world scenarios
 - large e-commerce sites have tens of millions of customers and millions of items
- Model-based approaches
 - based on an offline pre-processing or "model-learning" phase
 - at run-time, only the learned model is used to make predictions
 - models are updated / re-trained periodically
 - large variety of techniques used
 - model-building and updating can be computationally expensive

Item-based CF

- Basic idea:
 - Use the similarity between items (and not users) to make predictions
- Example:
 - Look for items that are similar to Item5
 - Take Alice's ratings for these items to predict the rating for Item5

	Item1	Item2	Item3	Item4	Item5
Alice	5	3	4	4	?
User1	3	1	2	3	3
User2	4	3	4	3	5
User3	3	3	1	5	4
User4	1	5	5	2	1

The cosine similarity measure

- Produces better results in item-to-item filtering
 - for some datasets, no consistent picture in literature
- Ratings are seen as vector in n-dimensional space
- Similarity is calculated based on the angle between the vectors

$$sim(\vec{a}, \vec{b}) = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| * |\vec{b}|}$$



- Adjusted cosine similarity
 - take average user ratings into account, transform the original ratings
 - 11. set of users who have rated both items a and b

$$sim(a, b) = \frac{\sum_{u \in U} (r_{u,a} - \bar{r}_u)(r_{u,b} - \bar{r}_u)}{\sqrt{\sum_{u \in U} (r_{u,a} - \bar{r}_u)^2} \sqrt{\sum_{u \in U} (r_{u,b} - \bar{r}_u)^2}}$$



Pre-processing for Item-based CF

- Item-based filtering does not solve the scalability problem itself
- Pre-processing approach by Amazon.com (in 2003)
 - Calculate all pair-wise item similarities in advance
 - The neighborhood to be used at run-time is typically rather small, because only items are taken into account which the user has rated
 - Item similarities are supposed to be more stable than user similarities
- Memory requirements
 - Up to N^2 pair-wise similarities to be memorized (N = number of items) in theory
 - In practice, this is significantly lower (items with no co-ratings)
 - Further reductions possible
 - Minimum threshold for co-ratings (items, which are rated at least by n users)
 - Limit the size of the neighborhood (might affect recommendation accuracy)

More on Ratings...

- Pure CF-based systems only rely on the rating matrix
- Explicit ratings
 - Most commonly used (1 to 5, 1 to 7 Likert response scales)
 - Research topics
 - "Optimal" granularity of scale; indication that 10-point scale is better accepted in movie domain
 - Multidimensional ratings (multiple ratings per movie)
 - Challenge
 - Users not always willing to rate many items; sparse rating matrices
 - How to stimulate users to rate more items?
- Implicit ratings
 - Clicks, page views, time spent on some page, demo downloads ...
 - Can be used in addition to explicit ones; question of correctness of interpretation

Data Sparsity Problems

- Cold start problem
 - How to recommend new items? What to recommend to new users?
- Straightforward approaches
 - Ask/force users to rate a set of items
 - Use another method (e.g., content-based, demographic or simply non-personalized) in the initial phase
- Alternatives
 - Use better algorithms (beyond nearest-neighbor approaches)
 - Example:
 - In nearest-neighbor approaches, the set of sufficiently similar neighbors might be too small to make good predictions
 - Assume "transitivity" of neighborhoods

Example Algorithms for Sparse Datasets

- Recursive CF
 - Assume there is a very close neighbor n of u who however has not rated the target item i yet.
 - Idea:
 - Apply CF-method recursively and predict a rating for item i for the neighbor
 - Use this predicted rating instead of the rating of a more distant direct neighbor

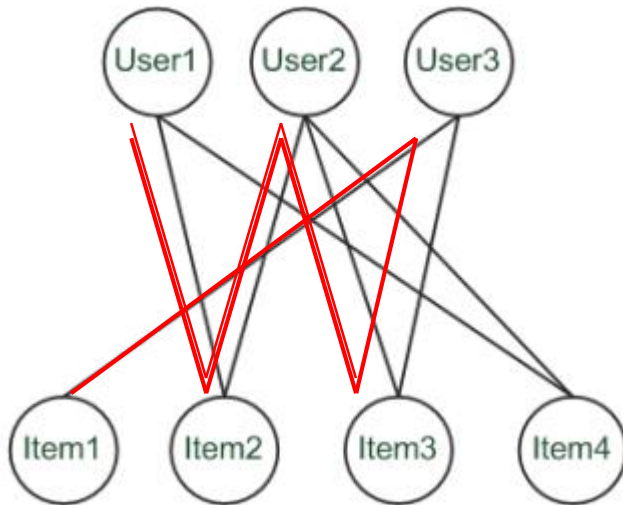
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User2	4	3	4	3	5
User3	3	3	1	5	4
User4	1	5	5	2	1

sim = 0,85

Predict
rating for
User1

Graph-based Methods

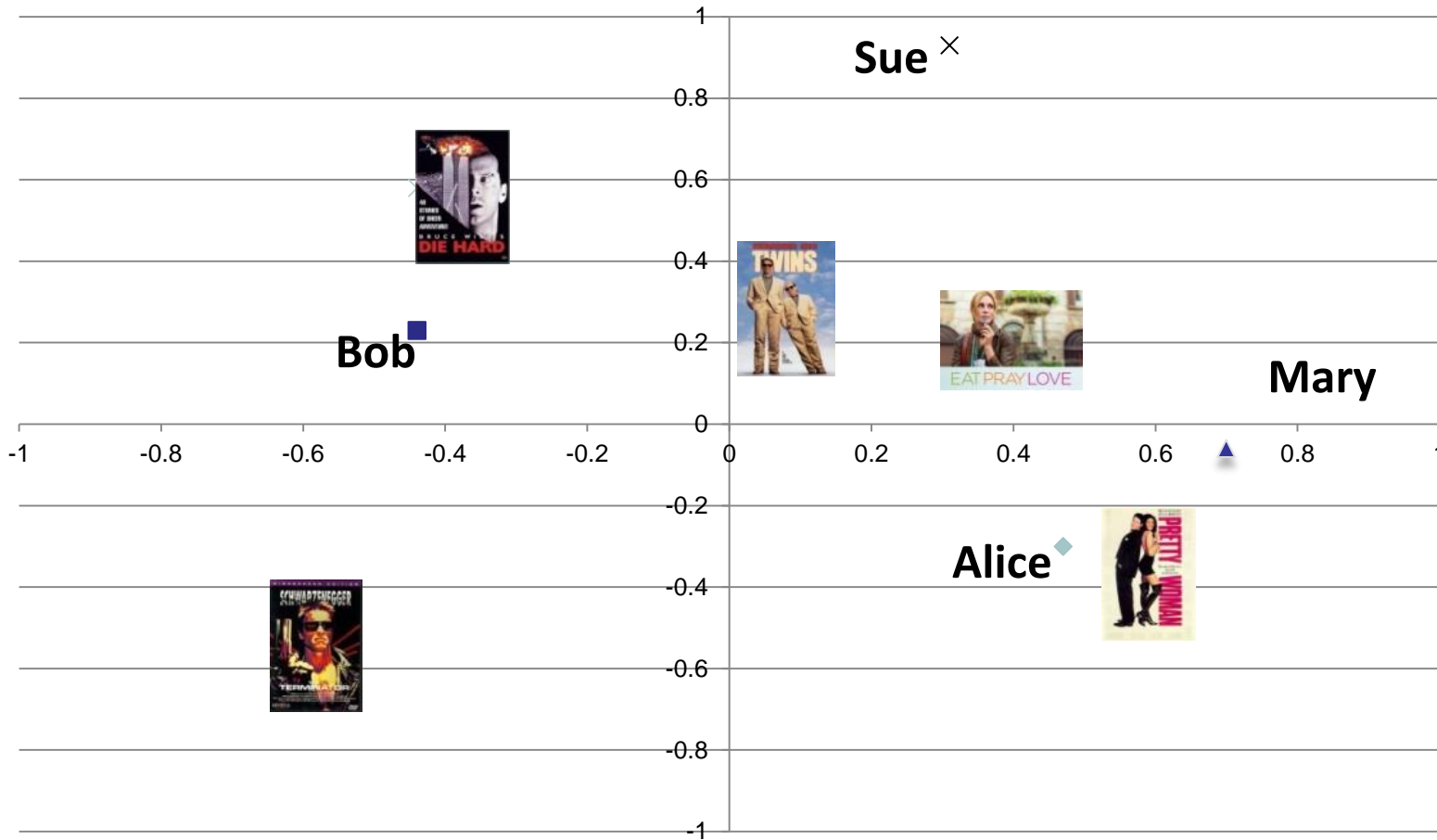
- "Spreading Activation" (sketch)
 - Idea: Use paths of lengths > 3 to recommend items
 - Length 3: Recommend Item3 to User1
 - Length 5: Item1 also recommendable



More Model-based Approaches

- Plethora of different techniques proposed in the last years, e.g.,
 - Matrix factorization techniques, statistics
 - singular value decomposition, principal component analysis
 - Association rule mining
 - compare: shopping basket analysis
 - Probabilistic models
 - clustering models, Bayesian networks, probabilistic Latent Semantic Analysis
 - Various other machine learning approaches
- Costs of pre-processing
 - Usually not discussed
 - Incremental updates possible?






A Picture Says ...



Matrix Factorization

- SVD: $M_k = U_k \times \Sigma_k \times V_k^T$

U_k	Dim1	Dim2
Alice	0.47	-0.30
Bob	-0.44	0.23
Mary	0.70	-0.06
Sue	0.31	0.93

V_k^T					
Dim1	-0.44	-0.57	0.06	0.38	0.57
Dim2	0.58	-0.66	0.26	0.18	-0.36

Σ_k	Dim1	Dim2
Dim1	5.63	0
Dim2	0	3.23

- Prediction: $\hat{r}_{ui} = \bar{r}_u + U_k(\text{Alice}) \times \Sigma_k \times V_k^T(\text{EPL})$
 $= 3 + 0.84 = 3.84$

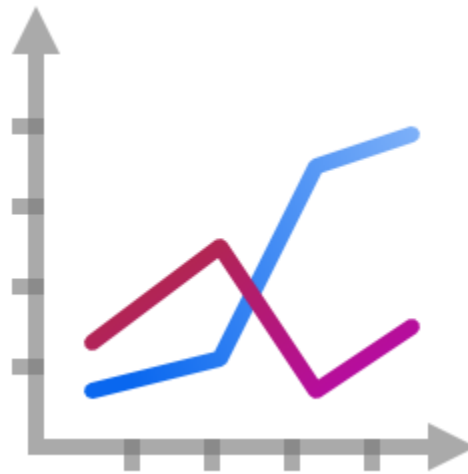
Association Rule Mining

- Commonly used for shopping behavior analysis
 - aims at detection of rules such as
"If a customer purchases baby-food then he also buys diapers in 70% of the cases"
- Association rule mining algorithms
 - can detect rules of the form $X \Rightarrow Y$ (e.g., baby-food \Rightarrow diapers) from a set of sales transactions $D = \{t_1, t_2, \dots, t_n\}$
 - measure of quality: support, confidence

Probabilistic Methods

- Basic idea (simplistic version for illustration):
 - given the user/item rating matrix
 - determine the probability that user Alice will like an item i
 - base the recommendation on such these probabilities
- Calculation of rating probabilities based on Bayes Theorem
 - How probable is rating value "1" for Item5 given Alice's previous ratings?
 - Corresponds to conditional probability $P(\text{Item5}=1 \mid X)$, where
 - $X = \text{Alice's previous ratings} = (\text{Item1}=1, \text{Item2}=3, \text{Item3}= \dots)$
 - Can be estimated based on Bayes' Theorem
- Usually more sophisticated methods used
 - Clustering
 - pLSA ...

Evaluation of Recommender Systems



What is a good Recommendation?

What are the measures in practice?

- Total sales numbers
- Promotion of certain items
- ...
- Click-through-rates
- Interactivity on platform
- ...
- Customer return rates
- Customer satisfaction and loyalty

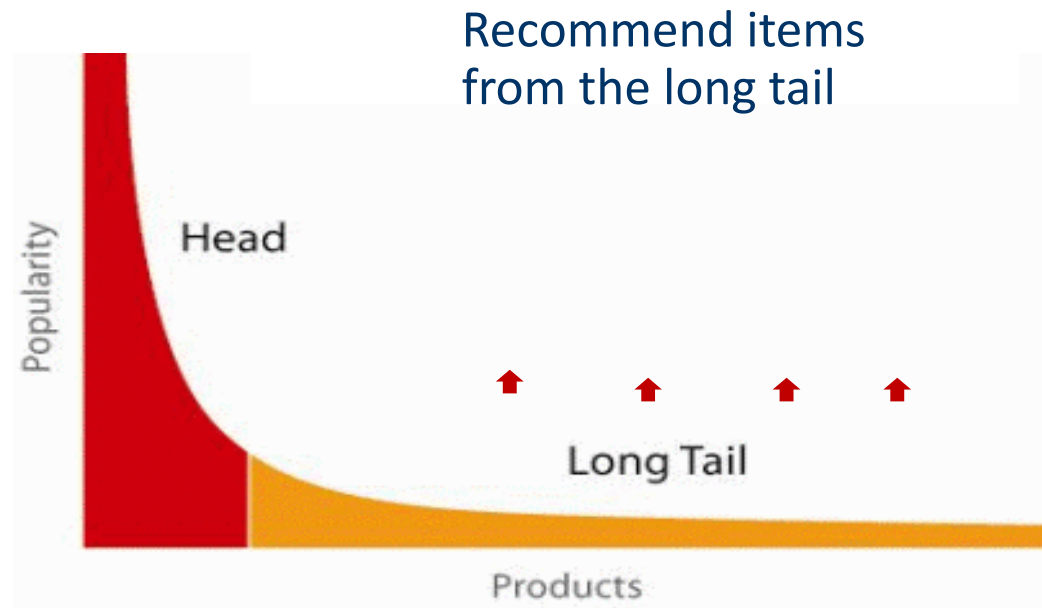


Purpose and Success Criteria (1)

Different perspectives/aspects

- Depends on domain and purpose
- No holistic evaluation scenario exists
- Retrieval perspective
 - Reduce search costs
 - Provide "correct" proposals
 - Assumption: Users know in advance what they want
- Recommendation perspective
 - Serendipity – identify items from the Long Tail
 - Users did not know about existence

When does a RS do its job well?



- "Recommend widely unknown items that users might actually like!"
- 20% of items accumulate 74% of all positive ratings

Purpose and Success Criteria (2)

- Prediction perspective
 - Predict to what degree users like an item
 - Most popular evaluation scenario in research
- Interaction perspective
 - Give users a "good feeling"
 - Educate users about the product domain
 - Convince/persuade users - explain
- Finally, conversion perspective
 - Commercial situations
 - Increase "hit", "clickthrough", "lookers to bookers" rates
 - Optimize sales margins and profit

Evaluation in Information Retrieval (IR)

- Recommendation is viewed as information retrieval task:
 - Retrieve (recommend) all items which are predicted to be "good" or "relevant".
- Common protocol :
 - Hide some items with known ground truth
 - Rank items or predict ratings -> Count -> Cross-validate
- Ground truth established by human domain experts

		Reality	
		Actually Good	Actually Bad
Prediction	Rated Good	True Positive (tp)	False Positive (fp)
	Rated Bad	False Negative (fn)	True Negative (tn)

Metrics: Precision and Recall

- **Precision:** a measure of exactness, determines the fraction of relevant items retrieved out of all items retrieved
 - E.g. the proportion of recommended movies that are actually good

$$Precision = \frac{tp}{tp + fp} = \frac{|good\ movies\ recommended|}{|all\ recommendations|}$$

- **Recall:** a measure of completeness, determines the fraction of relevant items retrieved out of all relevant items
 - E.g. the proportion of all good movies recommended

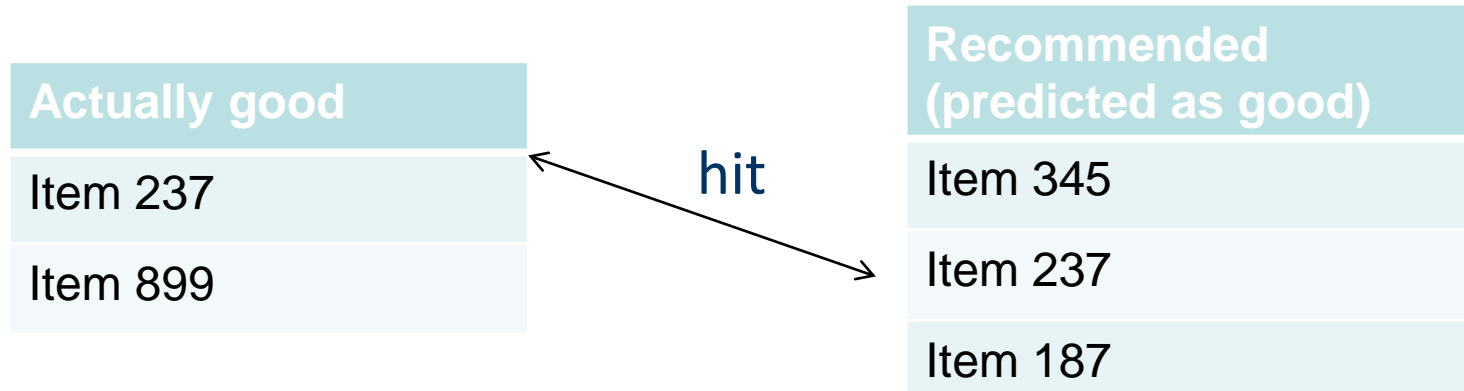
$$Recall = \frac{tp}{tp + fn} = \frac{|good\ movies\ recommended|}{|all\ good\ movies|}$$

Dilemma of IR measures in RS

- **IR measures** are frequently applied, however:
 - Ground truth for most items actually unknown
 - What is a relevant item?
 - Different ways of measuring precision possible
- Results from offline experimentation may have limited predictive power for online user behavior.

Metrics: Rank Score – Position Matters

For a user:



- **Rank Score** extends recall and precision to take the positions of correct items in a ranked list into account
 - Particularly important in recommender systems as lower ranked items may be overlooked by users
 - Learning-to-rank: Optimize models for such measures (e.g., AUC)

Accuracy Measures

- Datasets with items rated by users
 - MovieLens datasets 100K-10M ratings
 - Netflix 100M ratings
- Historic user ratings constitute ground truth
- Metrics measure error rate
 - Mean Absolute Error (*MAE*) computes the deviation between predicted ratings and actual ratings
 - Root Mean Square Error (*RMSE*) is similar to *MAE*, but places more emphasis on larger deviation

$$MAE = \frac{1}{n} \sum_{i=1}^n |p_i - r_i|$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (p_i - r_i)^2}$$

Offline Experimentation Example

- Netflix competition
 - Web-based movie rental
 - Prize of \$1,000,000 for accuracy improvement (RMSE) of 10% compared to own Cinematch system.
- Historical dataset
 - ~480K users rated ~18K movies on a scale of 1 to 5 (~100M ratings)
 - Last 9 ratings/user withheld
 - Probe set – for teams for evaluation
 - Quiz set – evaluates teams' submissions for leaderboard
 - Test set – used by Netflix to determine winner
- Today
 - Rating prediction only seen as an additional input into the recommendation process

An Imperfect World...

- Offline evaluation is the cheapest variant
 - Still, gives us valuable insights
 - and lets us compare our results (in theory)
- Dangers and trends:
 - Domination of accuracy measures
 - Focus on small set of domains (40% on movies in CS)
- Alternative and complementary measures:
 - Diversity, Coverage, Novelty, Familiarity, Serendipity, Popularity, Concentration effects (Long tail)

Online Experimentation Example

- Effectiveness of different algorithms for recommending cell phone games [Jannach, Hegelich 09]
- Involved 150,000 users on a commercial mobile internet portal
- Comparison of recommender methods



CF – Pros and Cons

- Pros:
 - well-understood, works well in some domains, no knowledge engineering 👍 required
- Cons:
 - requires user community, sparsity problems, no integration of other knowledge sources, no explanation of results 👎
- What is the best CF method?
 - In which situation and which domain? Inconsistent findings; always the same domains and data sets; differences between methods are often very small (1/100)
- How to evaluate the prediction quality?
 - MAE / RMSE: What does an MAE of 0.7 actually mean?
 - Serendipity: Not yet fully understood
- What about multi-dimensional ratings?

Summary

- CF is one of a handful of learning-related tools that have had broadly *visible* impact:
 - Google, TIVO, Amazon, personal radio stations, ...
- Critical tool for finding “consensus information” present in a large community (or large corpus of web pages, or large DB of purchase records,)
 - Similar in some respects to Q/A with corpora
- Science is relatively-well established
 - in certain narrow directions, on a few datasets
- Set of applications still being expanded
- Some resources:
 - <http://www.sims.berkeley.edu/resources/collab/>
 - <http://www.cs.umn.edu/Research/GroupLens/>
 - <http://www.cis.upenn.edu/~ungar/CF/>

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