

Not an intuitive question. (Floyds)

Q 11 Find the duplicate number in an array of $n+1$ integers where numbers are from $[1, n]$.

i/p $\rightarrow \{1, 4, 4, 2, 4\}$

o/p $\rightarrow 4$

- * The simplest approach can be like running 2 nested loops and then finding a number which is equal to number present at i^{th} index & j^{th} index (starting from $i+1$) but this has time complexity of $O(n^2)$.
- * We can make a frequency / count array and then store the frequency of each number in that array & if we find any number having frequency > 1 , that will be the answer. It has time & space complexity of $O(n)$.
- * Now the approach of constant space can be just sort the array & then compare the adjacent elements & if found equal, then simply return that number. Time complexity of the solution will be $O(n \log n)$.

Dry run

1) Sort the array

$\{1, 2, 4, 4, 4\}$

2) Start from $i=1$ till size of array &

compare $(i-1)^{th}$ index element and i^{th} index element. If found equal store it & simply come out of loop by break.

(i) $i=1$, $ans = arr[0] = 1$
 $arr[i-1] = arr[0] = 1$
 $arr[i] = arr[1] = 2$
 $1 \neq 2$ hence simply move to next element

(ii) $i=2$, $ans = arr[0] = 1$
 $arr[i-1] = arr[1] = 2$
 $arr[i] = arr[2] = 4$
 $2 \neq 4$ hence simply move to next element

(iii) $i=3$, $ans = arr[0] = 1$
 $arr[i-1] = arr[2] = 4$
 $arr[i] = arr[3] = 4$
 $4 = 4$ hence $ans = arr[i] = 4$ & break

3) Simply return ans i.e 4 in this case.

Code

```
int findDuplicate (vector<int>& nums) {
    //Sort the vector
    sort (nums.begin(), nums.end());
    //Random guess
    int ans = nums[0];
    //Comparing the adjacent elements
    for (int i=1; i<nums.size(); i++) {
        if (nums[i-1] == nums[i]) {
            ans = nums[i];
            break; // Duplicate is there
        }
    }
}
```

```
}
```

```
return ans; // Duplicate element is returned
```

```
}
```

Time complexity = $O(n \log n)$

Space complexity = $O(1)$

Note → In the question there were 2 constraints,
(i) no modification in array
(ii) no extra space to be used

The above 2 constraints can be made sure with fast & slow pointer approach which we will be discussing in linked list.

Floyd's detection (Cycle detection)

0 1 2 3 4

1	3	4	2	2
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Think of every value as the pointer.

$\text{arr}[0] = 1$

pointing to 1st index.

$\text{arr}[1] = 3$

pointing to 3rd index

$\text{arr}[3] = 2$

pointing to 2nd index

$\text{arr}[2] = 4$

pointing to 4th index

$\text{arr}[4] = 2$

again pointing to 2nd index & hence here

We got the duplicate value.

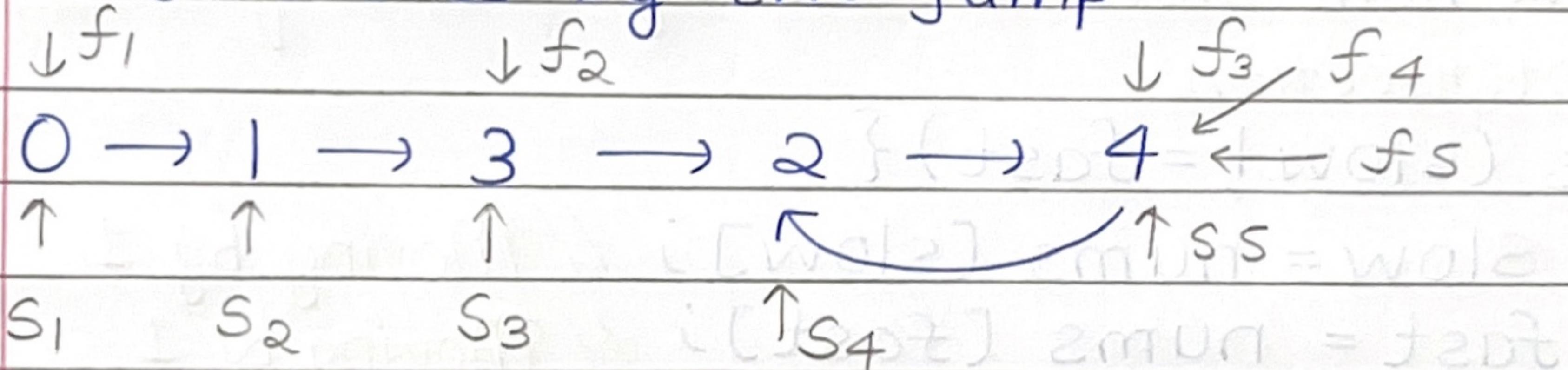
Also we can say that we won't be getting any value pointing to 0th index as numbers are in range from 1 to n.

$0 \rightarrow 1 \rightarrow 3 \rightarrow 2 \rightarrow 4$ Cycle

Slow and fast pointer

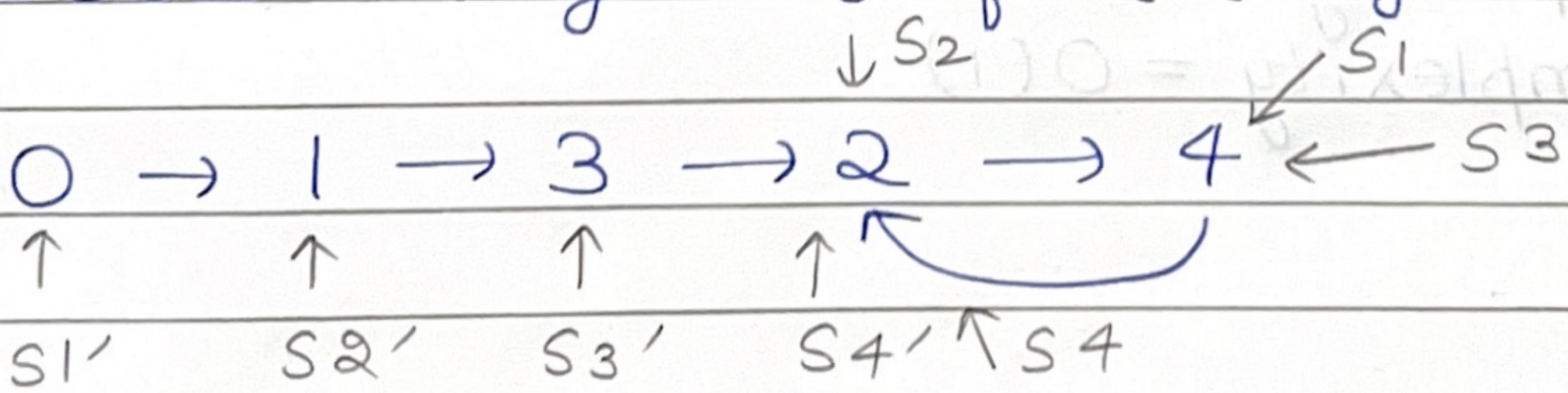
Slow → moves by one jump

fast → moves by two jumps



After 5 jumps of slow & 10 jumps of fast, they both intersect & hence this is the intersection point.

Now take 2nd slow pointer at the start & Start moving both of them by 1.



both slow pointers intersected.

Hence we found the starting point of the cycle.

Code

```
int findDuplicate (vector<int> &nums) {
```

H Range $\rightarrow [1, n]$

// 0th index not pointed by anyone

int slow = 0;

int fast = 0;

// Find intersection of fast & slow

do {

slow = nums[slow]; // Moving by 1

fast = nums[nums[fast]]; // moving by 2

} while (slow != fast);

// Place slow to 0.

slow = 0;

// move both slow & fast by 1 and find
the intersection

while (slow != fast) {

slow = nums[slow]; // Moving by 1

fast = nums[fast]; // Moving by 1

}

return slow; // fast can be returned

}

Time complexity = $O(n)$

Space complexity = $O(1)$