

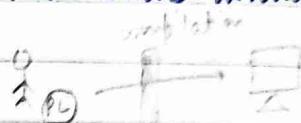
## INTRODUCTION TO C++ (RECORDED)

Platform dependent

↳ often has system specific  
code, packages available only  
if others compilation.

# What is C++ ?

- o) Programming language: is a computer language that is used by programmers to communicate with computers. It is a set of instructions written in any specific language to perform a specific task.



Output  
(Machine understandable  
format)

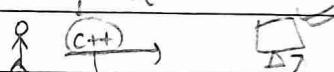
- o) C++ is a high-level, general-purpose PL.

Why do we need it?

- Object oriented Programming.
- Control over system resources and memory.
- Performance: efficiency and speed.

- o) Uses of C++: system / software development, game development, real time systems

SOURCECODE



compilation  
process

Machine understandable

- o) Compilation Process

Turning source code into executable code.

Steps in compilation process: preprocessing, compilation, assembly & linking

(Q) HW:

C++ is low-level or high-level language?

Low level language: machine-friendly. Thus, very difficult to understand and learn by human.

High level language: human-friendly. Thus, very easy to understand & learn by any programmer.

C++ can perform both low-level and high level programming. Hence, it is a mid-level language. C++ is a high-level language. (low-level features for efficient system programming and high-level features for building complex applications)

### Write your first program

```
# int main()           → starting point of program
    {
        define scope
    }
```

- # what is return 0? → represents successful execution
- if any other non-zero value is returned → unsuccessful execution.

### Let's print something

```
#include <iostream>
using namespace std;
int main()
{
    cout << "Namaste Auntya" << endl;      ← statement of line
    return 0;
}
```

#### HW Q1. Alternative of endl?

- \n
- Q2. if not using namespace std; then?
- std:: cout << "Hi";

#### Q3. return -1?

- unsuccessful execution

#### Q4. # include a preprocessor directive.

- they are not C++ statements, so doesn't end with(); semicolon.
- They are lines of the source file where the first non-whitespace character is #, which distinguishes them from other lines of text.

### Variables and Datatypes

Variables : named storage memory location.

e.g.: int marks = 50;

Syntax: datatype variable-name = value;

.obj → some code  
.exe → executable file

Datatypes : it specifies the size and type of information the variable will store.  
//declaration

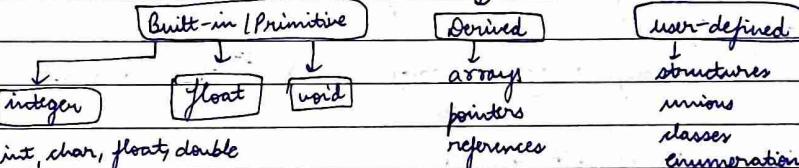
e.g.: int age; → it assigns any random value to variable age.  
age = 101; → garbage value  
//definition

e.g.: int age = 25;

\* same name ka variable 2 bar declare kri ter skte? error akayega  
→ doosre codeblock me dubara declare kr skte hoi (even in nested q3)

code block main.

### C++ datatypes



e.g.: double weight = 55.69887; → in o/p it is rounded-off values till 4 places only.  
bool isMale = false; → 0 in o/p.  
bool isFemale = 1;

#### (HW) Q. How data is stored in memory?

##### Detailed info:

Type	bits	range
int	32 bit	-2147483648 to 2147483647
unsigned int	32 bit	0 to 65535
signed int	32 bit	-2147483648 to 2147483647
short int	16 bit	-32768 to 32767

Type Bits  $\Rightarrow$  range

~~unsigned short int~~ 16 0 to 65535

~~signed short int~~ 16 -32768 to +32767

~~long int~~ 32 bits -2147483648 to 2147483647 (32 bits)

~~unsigned long int~~ 32 bits

~~signed long int~~ 32 0 to 4294967295

~~float~~ 32  $\pm 1.7 \times 10^{38}$

~~double~~ 64  $\pm 1.7 \times 10^{38}$  to  $\pm 1.7 \times 10^{308}$

~~long double~~ 80 96  $\pm 3.37 \times 10^{38}$  to  $\pm 1.18 \times 10^{308}$

~~char~~ 8 -128 to 127

~~unsigned char~~ 8 0 to 255

~~signed char~~ 8 -128 to 127

~~bool~~ 8 true or false

eg: int age = 12;  
cout << sizeof(age) << endl;  $\rightarrow$  o/p is 4

\* How data is getting stored in memory?

int age = 5;

binary  $\rightarrow$  000-----00101  $\rightarrow 2^{32} - 1$  (max'm no.)  
32 bits

eg: 3 bits 001  $\Rightarrow 7 \Rightarrow 2^3 - 1$

n bits  $\Rightarrow 2^n - 1$

Range

\* ~~int~~ signed & unsigned  $\Rightarrow 2^{n-1} \rightarrow 2^{n-1}$

~~unsigned~~  $\Rightarrow 0$  to  $2^n - 1$  if it takes n bits (n=32 here)

~~bool~~

$\rightarrow T \rightarrow 00000000$   
 $\rightarrow F \rightarrow 10000000$   $\Rightarrow$  takes up 8 bits, i.e. 1 byte.

1 byte: smallest addressable space

1 bit: smallest memory location

HW  $\rightarrow$  decimal N.S  $\rightarrow$  binary N.S conversion and vice-versa.

mSB (most significant bit)

memo: 101...11  $\rightarrow$  Least SB (LSB)

first bit

mem no. 101...11

How mem no. are stored in memory?

$\rightarrow$  2's complement = 1's complement + 1

eg: 00101011

1's complement = 11010100

2's complement = add 1

= 11010101

decimal: 1+1=2, binary: 1+1=10

eg: 00000000000000000000000000000000  $\Rightarrow$  00001000

User input in C++ : cin

eg: int age;  
cin >> age;

eg: bool marks;  $\rightarrow$  true  
cin >> marks;  $\rightarrow$  o/p is 10

{ give input as 0 or 1 in bool not as true or false }

(HW) Q. cin.ignore(), cin.fail(), getline(cin, l0)

Ans: ignore() is a method inside istream class

cin.ignore() is used to ignore or clear one or more characters from input buffer. eg: cin.ignore(256, ' '); ignore 256 characters unless a space comes. This space is called delimiter.

$\rightarrow$  cin.fail(): returns true when an input failure occurs.

$\rightarrow$  cin doesn't allow to take input in multiple lines. input: take by human

To accept multiple lines, we use getline().

eg: string name;

getline (cin, name);

cout << name << endl;

eg: cin.ignore(5, 'a');  
o/p is LK

$\rightarrow$  cin.get : get one character.

## Control flow

### Decision making :

- if statement
- if-else → if-else if → if-else if-else
- nested if.

### if-statement

Syntax:  
`if (condition) {  
 //statement  
}`

### if-else block

```
if (cond) {  
    //  
}  
else {  
    //
```

### if-else if block

```
if (cond) {  
    //  
}  
else if ( ) {  
    //  
}  
else {  
    //
```

### if-else-if-else block

### nested-if

```
if () {  
    if () {  
        //  
    }  
    else {  
        //  
    }  
} else {  
    //
```

Switch statements → control flow.

Syntax:  
`switch (expression) {`

case val1:

//statement

break;

case val2:

//statement

break;

default:

//statement

eg : `switch(grade) {`

case 'A':

`cout << "marks b/w 90 to 100" << endl;`

break;

default:

`cout << "less than 60" << endl;`

}

### Conditions pertaining to 'switch'

- Expression type → grade/day → int / char / enum → float, string will not work
- Unique Case Values → case value cannot be repeated.
- No Range checking → `case (age > 18) :` X
- Fall through Behaviour → use break after every case.
- Execution order.

### Ternary Operator

Syntax:  
`condition ? expression_if_true : expression_if_false;`

eg : `(age > 18) ? "can vote" : "cannot vote";`

eg : `int age = 12;`

`(age > 18) ? cout << "can vote" : cout << "cannot vote";`

### Loops - for, while, do-while

#### For loop

Syntax:  
`for (initialization; condition; updation) {  
 //statement`

    //

    //

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Break keyword: skip loop forward skip loop

Continue keyword: skip iteration.

While loop:

Syntax: while (condition) {  
    initialization;  
    // updation;  
}

Do-while loop

Syntax: initialization;  
do { // statement  
    // updation  
} while (p);  
    // cond

a. `for(int i=1; i<=5; i++) {`  
    `}`

b. `if (cin >> i){`  
    `cout << "Samanya";`  
}

Ans: take input and gives o/p as Samanya.

c. ~~if (cout << "hi") {~~  
    `cout << "Samanya";`  
}

Ans: o/p  $\Rightarrow$  hisamanya

### Nested Loops

Syntax:  
for ( ) {  
    for ( ) {  
        //statement  
    }  
}

eg: `for (int i=1; i<=2; i++) {`      o/p  $\Rightarrow$  1 2 2 4  
    `for (int j=1; j<=2; j=j+1) {`  
        `cout << i * j << " ";`  
    }  
}

Operators in C++: is a symbol that operates on a value to perform specific mathematical or logical computations. They form the foundation of any programming language.

### Unary Operator

$\Rightarrow$   $\text{++}$        $\text{--}$   
 $\Rightarrow$  pre-increment and post-increment.  
 eg:  $\text{++a}$        $a++$   
 $\downarrow$                  $\downarrow$   
 $\text{operand}$              $\text{a}$   
 $\text{post increment, for use}$        $\text{pre use, for increment}$

$\Rightarrow$  similarly for —  
 $\Rightarrow$  post decrement and pre-decrement.

$\text{a--}$        $--\text{a}$   
 $\text{pre use, for decrement}$        $\text{post decrement, for use}$

### Binary Operator

- $\Rightarrow$  Arithmetic       $\Rightarrow$  Assignment.
- $\Rightarrow$  Relational
- $\Rightarrow$  Logical
- $\Rightarrow$  Bitwise

Arithmetic Operators : +, -, \*, /, %

(Bonus concept)

- \* int = int eg:  $\frac{5}{2} = 2$
- \* int = float ; float = float
- \* float = float & double = double  
int

Relational Operators : >, <, >=, <=, ==, !=

↳ check relation.

↳ gives o/p as 1 or 0.

↳ if S is false then

Logical Operators : &, ||, !

↳ for multiple conditions.

eg: age > 18 & income > 12

Bitwise Operators : &, |, ~, <<, >>, ^

↳ bit level p logic

Assignment Operators : =, +=, -=, \*=, /=, %=

eg: int a=5;

a=a+s; ] something.

a+=s;

a=a\*b; ] same

a\*=b;

a=a/10.0

a=10.0 ] same

→ & → a | b | o/p  

0	0	0
0	0	0
0	1	0
1	0	0
1	1	1

eg: 5 → 00 - - 00101  
4 → 00 - - 00100  
5&4 → 000 - - 100  
5&4 → o/p = 4

'1' →	a	b	o/p
	0	0	0
	0	1	1
	1	0	1
	1	1	1

↳ 514 → o/p = 4

'~' →	a	o/p
	0	1
	1	0

5 → 000 - - 00101  
~5 → 111 - - 111010

'<<' → left shift  
eg: 100 << 5 → 100x2^5  
↳ no. of shift  
5 << 2 → 20 & 5 << n → 5 \* 2^n

'>>' → right shift  
↳ right shift by 1  
↳ can say we are dividing by 2  
eg: 10 >> 1 → 10 / 2 → 5  
↳ 100 >> 3 → 100 / 2^3 (in majority cases) → A >> n →  $\frac{A}{2^n}$

'^' → XOR

a	b	o/p
0	0	0
0	1	1
1	0	1
1	1	0

→ a^a = 0

↳ same for both b^b = 0

↳ opp to one → 5^4 → 5 → 00101

↳ 4 → 00 - - 0100

5^4 → 1 → 001

HW Q. Bitwise operator can be applied on which type of datatype?

→ integer (byte, short, int, long) → cannot be used on floating (float, double)

HW Q. % operator on float?

→ NO.

Number System (N.S.)What is number system?

- method to represent numeric values or quantities using different digits.

NumberDecimal System

- The decimal N.S has base 10.
- It uses digits from 0 to 9.
- Base: it is the number of symbols/digits a N.S has.

Binary N.S.

- It has base 2.
- It uses only two digits, i.e. 0 and 1.

(CPU works in binary, memory stored in binary)

Counting in binary N.S

Decimal	Binary	Decimal	Binary
0	0	12	1100
1	1	13	1101
2	10	14	1110
3	11	15	1111
4	100	16	10000
5	101	17	10001
6	110	18	10010
7	111	19	10011
8	1000	20	10100
9	1001	21	10101
10	1010	22	10110
11	1011	23	10111

Decimal to binary conversionDivision method

- Divide number by 2.
- Store remainder (that will be a bit in binary number)
- Repeat above steps with the quotient until quotient is less than 2.
- Reverse the bits so obtained.

eg:  $N=10 \rightarrow \frac{10}{2} \rightarrow 5$  | Remainder  
 $5 \rightarrow 2$  | 0  
 $2 \rightarrow 1$  | 1  
 $1 \rightarrow 0$  | 1

$N=10$  (decimal)  
 $1010$  (binary)  
 $10 \rightarrow (1010)_2$

for code  $\rightarrow 0 \rightarrow 0 \times 10^0 + 0 = 0$

$1 \rightarrow 1 \times 10^1 + 0 = 10$

$0 \rightarrow 0 \times 10^2 + 10 = 10$

$1 \rightarrow 1 \times 10^3 + 10 = 1000$

$+ 10$

ans = 0  
code  $\Rightarrow$  ans = (digit  $\times 10^i$ ) + ans

(bitwise AND  
bitwise method)

- Obtain bit with bitwise AND operation, i.e.,  $(N \& 1)$

- Right shift N by 1. ( $N=N>>1$ )

- Repeat above steps till  $N > 0$

- Reverse the bits so obtained.

$\Rightarrow N \& 1 \oplus 10 \rightarrow 1010$

$\oplus 0001$

0000  $\rightarrow 0$  (1<sup>st</sup> bit)

② right shift  $\Rightarrow 101$

001

001 (2<sup>nd</sup> bit)

③ right shift  $\Rightarrow 10$

01

01 (3<sup>rd</sup> bit)

$\rightarrow$  Remove it

④ right shift  $\Rightarrow 000-01$

001 (4<sup>th</sup> bit)

Binary To Decimal Conversion

1. Multiply each digit with its place value.

2. Add up all place values.

3. Sum is the decimal number.

Eg:  $1010 \rightarrow 10$

$$\begin{array}{r} 1 \ 0 \ 1 \ 0 \\ 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 = 8 + 0 + 2 + 0 = 10 \end{array}$$

Eg:  $10111 \rightarrow 23$

$$\begin{array}{r} 1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 = 32 + 0 + 8 + 4 + 2 + 1 = 23 \end{array}$$

code  $\Rightarrow$  Eg: binary =  $(1010)_2$

$$\textcircled{1} \text{ bit } = 1010 \% 10 \Rightarrow 0$$

$$\text{dec} = 0 + 0 \times 2^0 = 0$$

$$N = N/10 \Rightarrow 101$$

$$\textcircled{2} \text{ bit } = 101 \% 10 = 1$$

$$\text{dec} = 0 + 1 \times 2^1 = 2$$

$$\textcircled{3} \text{ N } = N/10 \Rightarrow 10$$

$$\textcircled{4} \text{ bit } = 10 \% 10 = 0$$

$$\text{dec} = 2 + 0 \times 2^2 = 2$$

$$N = N/10 = 1$$

$$\textcircled{5} \text{ bit } = 1 \text{ dec } = 2 + 1 \times 2^3 = 2 + 8 = 10$$

Typecasting

$\Rightarrow$  Allows you to change the datatype of a variable from one type to another.

$\Rightarrow$  Crucial when you need to perform operations involving variables of different data types, ensuring that the data is handled correctly.

Implicit Type Casting, aka, Automatic Type Conversion

- Compiler automatically converts one datatype to another during an operation.
- This happens when you perform operations involving variables of different datatypes, and the compiler promotes one type to a larger type to

maintain precision.

Eg: int n1 = 10;

float n2 = 5.5;

float result =

n1 + n2;

cout << result;

Explicit Type Casting, aka, Manual Type Conversion

$\Rightarrow$  Allows you to explicitly specify the desired datatype during an assignment or operation.

$\Rightarrow$  You use the casting operator, which is represented by parenthesis containing the target datatype.

Eg: float result = n1 + (int)n2;

FunctionsWhat is a function?

A function is a way to group code into a single unit. It can take inputs, process them, and return a result. Functions help in organising code, making it more readable and maintainable.

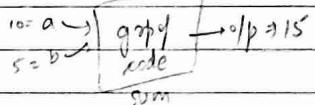
repeated code

buggy

buggy

maintainability x

readability x

Why we need Function?

Fx's reduce repetition, simplify complex tasks, and helps in debugging. They also make it easier to test individual parts of your program.

Function AnatomyDeclaration

syntax: returntype functionName (input parameters)

Definition

body

Does order matter?

void

non-void

3

Yes

int, char, float, etc

```
eg: int sum( int a, int b ) {
    return a+b;
}
```

### Calling a function

```
eg: int ans = sum(5,10);
cout << ans;
```

arguments

\* Function should be above int main(). *Keep fxn below int main, then it should be at least declared before int main.* (yo fir jaha hui use kro)

### declaration:

```
eg: int getsum( int x, int y);
```

signature

definition: → fxn logic

```
y! int getsum {
    /body
}
```

(Void wale fxn ne return value nahi kr skte but kashii return likh skte hain.)

(nw)

Q. print Numbers from 1 to 100.

Q. Write a SIP calculator using function's concept.

## BASICS OF PROGRAMMING - Level 1

[LIVE CLASS]

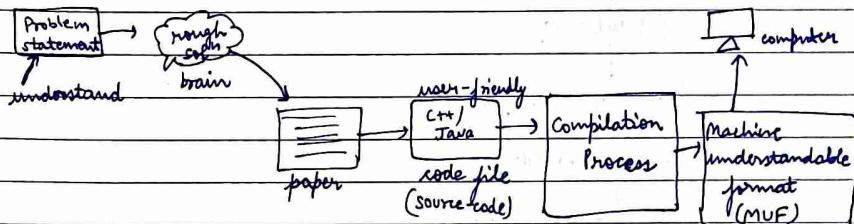
### INTRODUCTION TO THE PROGRAMMING WORLD

29/4/24

#### \* How To Approach a problem?

##### Thought process

- let's first understand the problem
- analyse problem → check input values / constraints / requirements.
- logic building / approach / algorithm.



Series of steps: algorithm.

### Flowchart & its components

Flowchart is a diagrammatic representation that illustrates the sequence of operations to be performed to arrive at a solution to a problem. It uses various symbols such as arrows, rectangles, diamonds to represent different types of actions or steps in a process.

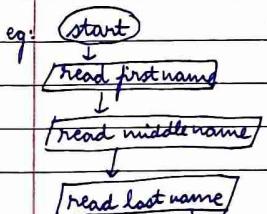
① : start/end : terminator

② : input/output

③ : process block (eg: a=a+6, etc other calculations)

④ : arrows : flow of execution.

⑤ : decision block



Pseudo:

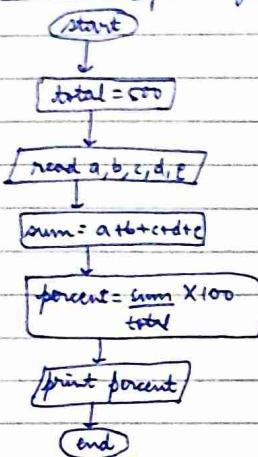
- ① start
- ② input first name
- ③ " middle name
- ④ " last name
- ⑤ print name
- ⑥ end

/print first, middle, last name/ → (end)

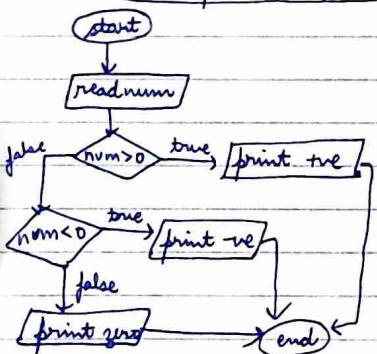
### Pseudocode

It is a notational system that resembles a simplified version of a programming language, used for writing the algorithmic steps of a program in a human-readable form. It helps programmers plan and discuss algorithms without worrying about syntax details.

e.g.: Calculate B percentage



### Check positive, -ve, or zero



Pseudocode

→ start

→ take input for num

→ if num > 0

    print +ve

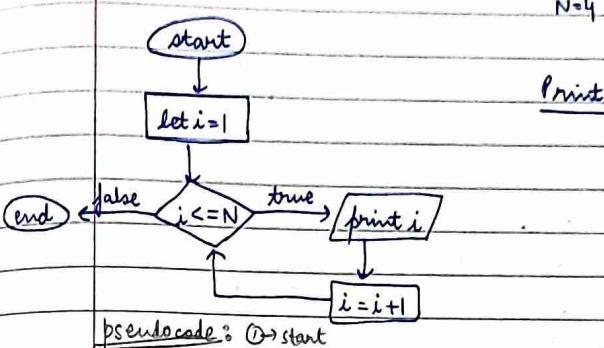
else if num < 0

    print -ve

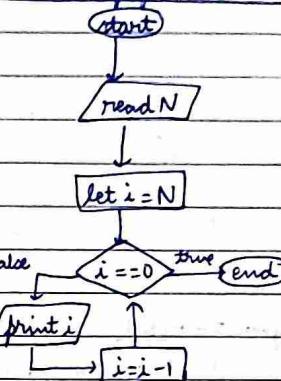
else print zero

→ end

### Print counting from 1 to N



### Print counting from N to 1



Add N Numbers from user → 5 numbers → 1 times

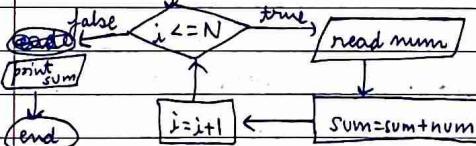
$$\begin{aligned}
 &\text{sum} = 0 \\
 &a = 3 \\
 &\text{sum} = 0 + 3 = 3 \\
 &b = 4 \\
 &\text{sum} = 0 + 3 + 4 = 7 \\
 &c = 2 \\
 &\text{sum} = 0 + 3 + 4 + 2 = 9
 \end{aligned}$$

start

/read N/

sum = 0

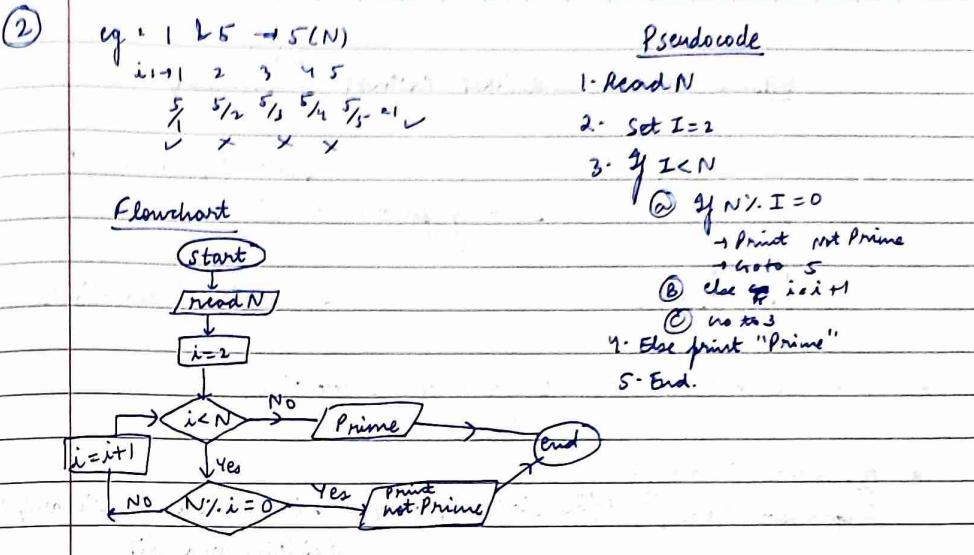
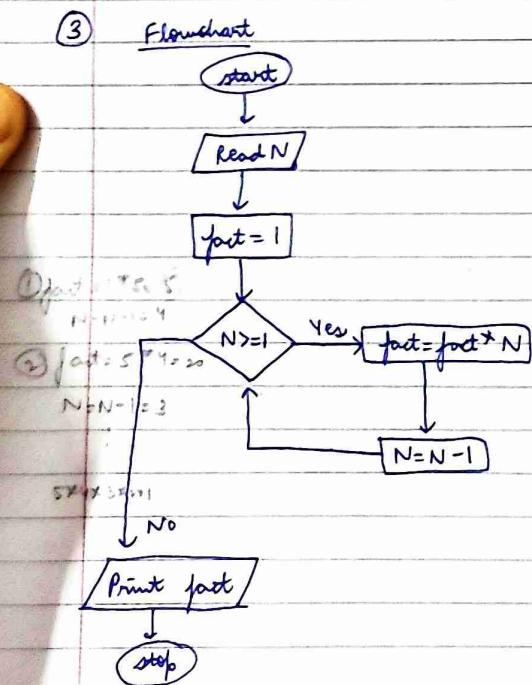
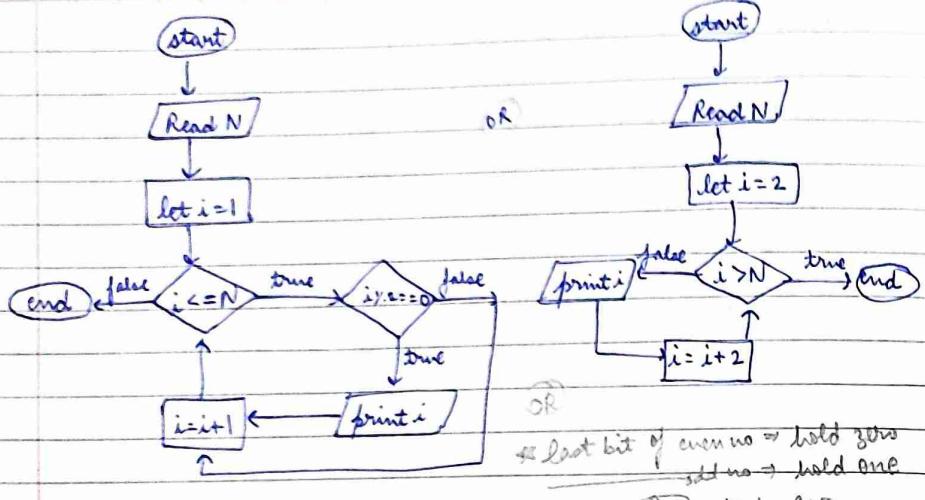
i = 1



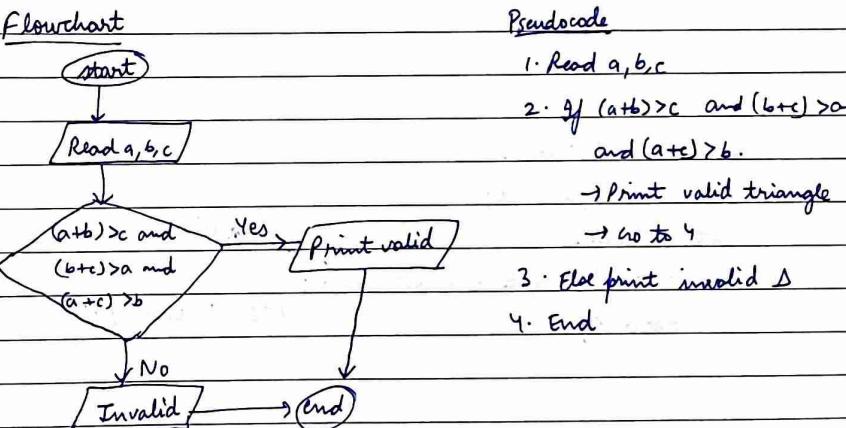
Print 1 to N numbers, only Even numbers →  $\frac{N}{2} \leq 0$

(acha kuchha ye to hoga  
wali krega  
doston method badhe  
long eng)

p.t.o



① triangle : two sides(sum) > other side



BASICS OF C++ and FIRST PROGRAM (1 May 24)

Let's write down the 1<sup>st</sup> code

```
int main()
{
}
```

return type → int  
function name → main  
starting point: int main () {  
} → scope or code-block

\* in main f() → always return 0 for successful execution.

#include <iostream>

preprocessor directive → file (i: input, o: output → use related functionality ki requirement to include some program before execution) definition yaha hai

using namespace std;  
↳ standard

```
int main()
{
    cout << "Hello World";
    cout << endl;
    cout << "I am a student of IIT Kharagpur";
    cout << endl;
}
```

#include <iostream>  
using namespace std;

```
int main()
{
    cout << "Namaste Duniya" << endl;
    return 0;
}
```

Input/Output in C++

cin >> cout <<

↳ give value to address of memory location.

eg: int age;  
cin >> age;

TIME CLASS

Page No. 23  
Date / /

Datatypes and variables → named memory location

→ type of data (int, float, string etc)  
→ size of data (4 byte)

double: can store more precision

char: a, z, A, Z, @, , , ,

use single quotes for character.

eg: char ch = 'a' 'saumya';

cout << ch; → o/b gives: a (diff behaviour in diff device)  
but keep only one character in char. last character.

→ sizeof(var-name) to get size in bytes.

→ int → 4 byte → 32 bits

show an integer  
eg: int a=3

32 dabbe → Total combination:  $2^{32}$  combination.

$$1 \rightarrow 2^{32}$$

$$\begin{aligned} &\text{normal maths: } \\ &\frac{2^a}{2^b} = 2^{a-b} \end{aligned}$$

unsigned →  $0 \rightarrow 2^{32}-1$  (range)      unsigned =  $[0 \rightarrow 2^{32}-1]$

signed

signed =  $[-2^{n-1} \rightarrow 2^{n-1}-1]$

eg: short

$$-32768 \rightarrow 32767$$

$$\text{cout} \ll 32768 \Rightarrow \text{o/b} = -32768$$

$$\text{cout} \ll 32770 \Rightarrow \text{o/b} = 32766$$

→ cyclic wapas jake print kerdega. (cyclic nature)

Variable naming convention

o) begin with alphabet

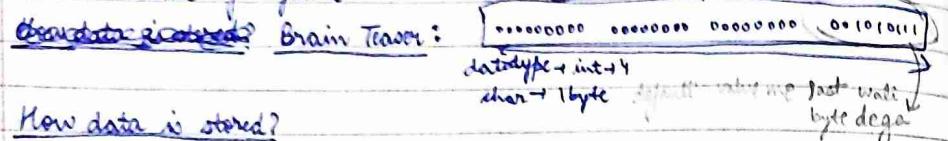
o) no space

o) digits may be used but only after alphabet

o) no special symbol except underscore()

- cannot create ~~variable~~ with reserved keyword or command.
- case sensitive (A & a are different variables)
- cannot use eg: myName

Ques: Brain Teaser:



How data is stored?  
(true or false integers)

## OPERATORS, CONDITIONALS and loops [LIVE CLASS] (6 May 2024)

Operators: symbols which carry special meaning.

- Arithmetic: +, -, \*, /, % (remainder)
- Relational: >, <,  $\geq$ ,  $\leq$ , ==, != (gives output as T or F)
- Assignment: =, +=, -=, \*=, /=, %=.
- Logical: &, |, ||, !
- Bitwise
- use brackets, there is no need of operator precedence.
- operand: value on which operation is performed.

\* Unary: single operand      binary: 2 operands

\* Assignment operator (shorthand)

$a = a + 10$  or  $a += 10$  (similar for others)

\* short circuit

eg:  $(\text{false} \text{ || true} \text{ || false}) \text{ (1 true)}$

\* ~~not~~ unary operator: ++, --

$\begin{cases} ++a & (\text{post-increment}) \\ ++a & (\text{pre-increment}) \end{cases}$

↑ ple use kro  
badme increment  
↑ ple increment kro  
↑ fir use

$\begin{cases} a-- & (\text{post-decrement}) \\ --a & (\text{pre-decrement}) \end{cases}$

eg:  $ans = ++a * ++a$

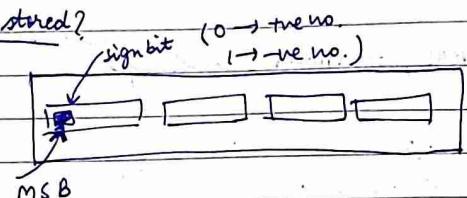
→ use brackets always

$\begin{cases} ① \\ ② \end{cases}$

$\frac{1}{2} \times 1^2$

computer dependent ans: 132 or 144

How +/ -ve no. are stored?



-ve no. → ① ignore -ve sign

② 2's complement is stored.

eg:  $a = -10$

$-10 \rightarrow -ve X$

$a = 10 \Rightarrow 0010$

1's complement  $1111 \dots 0101$

$\downarrow +1$

$1111 \dots 10110$

memory:

$$\begin{array}{r} 1111 \dots \\ \text{(re)} \downarrow \\ 0000 \dots 00001001 \end{array}$$

+ 1

$$\begin{array}{r} 0000 \dots 001010 \\ 10 \end{array}$$

Conditionals : if, if-else, nested if, ternary operator, switch.

① Basic if

Syntax: `if (cond){`

}

② if -else

Syntax: `if (cond){`

3

`else {`

}

if -else if

Syntax: `if (cond){`

3

`else if (-){`

}

`else{`

3

③ nested -if

`if (cond1){`

`if (cond2){`

=

`else {`

3

`else {`

3

[from intro to opp recording]

Q. `if (in > age){`

3

Q. `if (cont < 5){`

3

Q. `if (cond); {`

3

\* Ternary operator: `(cond)? true : false`

\* Switch case:

Syntax: `switch(expression){`

case:

`break;`

`case:`

`break;`

`default:`

`break;`

3

Loops : for, while, do-while

\* for

```
for(initialization; condition; updation){  
    }  
}
```

\* for(;;) →  $\infty$  loop

\* break : skip loop

\* continue : skip iteration.

(LIVE CLASS)  
LET'S SOLVE PATTERNS  
(8 May 2024)

\* outer loop ki har ek single value ke liye inner loop pata chalta hai.

```
eg: for(int i=1; i<=3; i++){  
    cout << i << endl;  
    for(int j=1; j<=2; j++){  
        cout << "*" << endl;  
    }  
}
```

Output:  
1 \*  
2 \*  
3 \*

Patterns : helps in logic building.

① Square

```
n0 -> * | * | * | *  
n1 -> * | * | * | *  
n2 -> * | * | * | *  
n3 -> * | * | * | *  
cols -> col1 col2 col3  
→ no. of rows = 4  
outer loop  
cols -> inner loop
```

Rules:

- ① divide in rows and columns.
  - ② find no. of rows.
  - ③ row 0 : 4 \*
  - row 1 : 4 \*
  - row 2 : 4 \*
  - row 3 : 4 \*
- (find formula by analysing rows)

code: //outer loop

```
for(int row 0 to row < 4) {
```

//inner loop

```
for(int col 0 to col < 4) {
```

cout << "\*";

}  
// after printing 4 stars, go to next line  
cout << endl;

}

② Rectangle

```
n0 → * * * *
n1 → * * * *
n2 → * * * *
c0 c1 c2 c3 c4
```

//outer loop

```
for(n=0 to n<3) {
    //inner loop
    for(c=0 to c<5) {
        cout << "*";
    }
    cout << endl;
}
```

① no. of rows → 3② n0 → 5\*n1 → 5\*n2 → 5\*n3 → 5\*n4 → 5\*③ Hollow Rectangle

```
↑ 0          ↓ 4
n0 → * * * *
n1 → * - - -
n2 → * - - -
n3 → * * * * *
```

//outer loop

```
for(int n=0 to n<4) {
    for(int c=0 to c<5) {
        //logic
    }
}
```

```
    } //logic
}
```

```
→ logic : if(n=0 || n=n=last) {
```

```
    cout << "*";
```

```
    middle rows - else {
```

```
        if(c=0 || col=last)
```

```
            cout << " * ";
```

```
        else → space
```

① no. of rows → n=4② n0 → 5\*n1 → 1\* 3 space 1\*n2 → 1\* 3 space 1\*n3 → 5\*

if(c=0 || col=last)  
cout << " \* ";

else → space

④ Hollow square

```
n0 → * * * *
n1 → *
```

```
n2 → *
```

```
n3 → *
```

```
n4 → *
```

```
c0 c1 c2 c3 c4
```

① total rows → n=5② n0 → 5\*n1 → 1\* 3 space 1\*n2 " " "n3 " " "n4 → 5\*

way 1 observation → first / last row / col → \* → \*

→ middle row → space last and first col → \*  
else → space

OR

way 2 → n=0, n=n-1, c=0, c=n-1 → print \*

else → space

⑤ Half pyramid

```
↑ 0          ↓ 4
n0 →
n1 → *
n2 → **
n3 → ***
n4 → ****
```

① total rows → n=5② n0 → 1\*n1 → 2\*n2 → 3\*n3 → 4\*n4 → 5\*

inner loop → simple

//outer loop

```
for(n=0 → n<n) {
```

```
    for(c=0 → c<row+1) {
```

```
        cout << "*";
```

```
    }
```

→ "row+1" stars

### ⑥ Inverted half pyramid

```

    *   *
    *   *
    *   *
    *   *
  
```

outer loop

```

for(r=0 to n-1) {
  for(c=0 to c<n-1) {
    cout << " ";
  }
  cout << endl;
}
  
```

### ⑦ Hit & trial : input | target

n=now	5
n=s, n=0	5
n=s, n=1	4

n=5, s=4 ↴ ↵

### ⑧ Hollow half pyramid

```

n0 *
n1 * *
n2 * - *
n3 * - - *
n4 * - - - *
n5 * * * * *
  
```

① n0 → \*  
 n1 → \*  
 n2 → \* - \*  
 n3 → \* - - \*  
 n4 → \* - - - \*

if n=0 || n=1 || now=c-1 → \*  
 col=0 or col=(now+1) → \*  
 else space

① total rows → n=4

② n0=4\*

n1=3\*

n2=2\*

n3=1\*

→ n=now → print starts

inputs available  
(n, r, stars)

⑨

### Inverted hollow half pyramid

```

    L
  → * * * *
    *
    *
    *
    *
  → *
  
```

① n=0, n-1,  
c=0, diagonal } star

② else space

diagonal  
row=col  
row+col=n-1

⑩

### Numeric half pyramid

n=4

```

for(n=0 to n<4) {
  for(c=0 to col<now+1) {
    cout << col+1;
  }
  cout << endl;
}
  
```

c0	c1	c2	c3
n0 1	1	1	1
n1 1 2	2	2	2
n2 1 2 3	3	3	3
n3 1 2 3 4	4	4	4

⑪

### Inverted numeric half pyramid

n=5 i/b target

c0 c1 c2 c3 c4
n0 1 2 3 4 5
n1 1 2 3 4
n2 1 2 3
n3 1 2
n4 1

n0 → 5 no.      n=5, n=0      5  
 n1 → 4 no.      n=n, /  
 n2 → 3 no.  
 n3 → 2 no.  
 n4 → 1 no.

```

for(n0 to n<n) {
  for(c0 to c<n-now) {
    cout << col+1;
  }
  cout << endl;
}
  
```

}

Homework: revise all patterns.

## BASICS OF PROGRAMMING - level 2

### Patterns (Mega Class) (live class) 12 May 2024

#### ① Full pyramid

```

    *
   * *
  * * *
 * * * *
* * * * *

```

$n=5$

① Outer loop : rows:  $0 \rightarrow 4$  or  $0 \rightarrow N-1$

② column wise

$n_0 \rightarrow 4 \text{ sp}, 1 *$  → row +

$n_1 \rightarrow 3 \text{ sp}, 2 *$

$n_2 \rightarrow 2 \text{ sp}, 3 *$

$n_3 \rightarrow 1 \text{ sp}, 4 *$

$n_4 \rightarrow 0 \text{ sp}, 5 *$

↓  
 $n=5$

N - n - 1 ✓

#### ② Inverted Full pyramid

```

    * * _ * _ *
   - * * _ * _ *
  - - * * _ *
  - - - * *
  - - - -

```

$n=5$

① Outer loop : rows:  $0 \rightarrow N-1$

② inner loop:  $n_0 \rightarrow 0 \text{ sp}, 5 *$

$n_1 \rightarrow 1 \text{ sp}, 4 *$

$n_2 \rightarrow 2 \text{ sp}, 3 *$

$n_3 \rightarrow 3 \text{ sp}, 2 *$

$n_4 \rightarrow 4 \text{ sp}, 1 *$

↙ ↘ N - now

#### ③ Diamond

```

      *
     * - *
    * - * - *
   * - * - * - *
  * - * - * - * - *
 * - * - * - * - *
* - * - *
* - *

```

→ full pyramid

+

→ inverted full pyramid

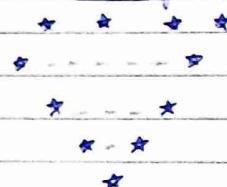
don't touch spaces with loop

#### (4) Hollow Pyramid



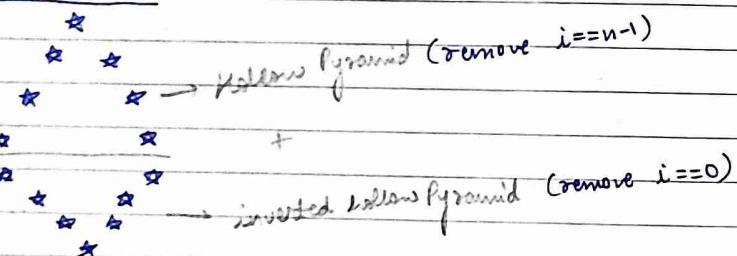
① stars:  $i=0$  or  $i=N-1$  or  $j=0$  or  $j=i$   
 $\Rightarrow$  star

#### (5) Inverted Hollow Pyramid

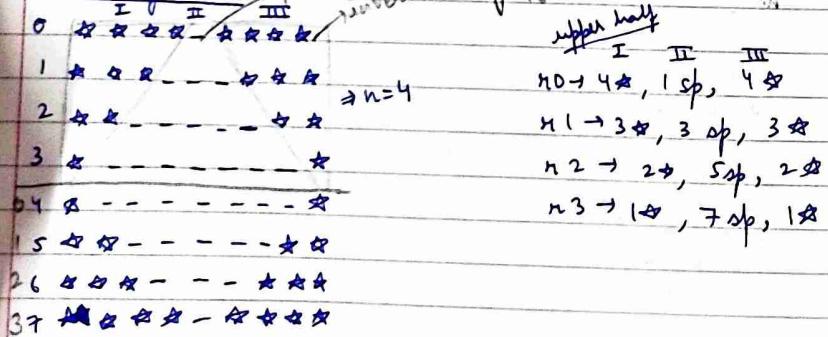


① stars:  $i=0$  or  $i=n-1$  or  
 $j=n-i-1$  or  $j=0$

#### (6) Hollow diamond



#### (7) Mixed Pyramid



- (I) stars:  $j: 0 \rightarrow n-i$
- (III) stars:  $j: 0 \rightarrow n-i$
- (II) spacers:  $0 \rightarrow 2i+1$

lower half:  $i=0 \rightarrow n=0: 1\spadesuit, 7\clubsuit, 1\clubsuit$   
 $n=1: 2\clubsuit, 5\spadesuit, 2\clubsuit$   
 $n=2 \rightarrow 3\clubsuit, 3\spadesuit, 3\clubsuit$   
 $n=3 \rightarrow 4\clubsuit, 1\spadesuit, 4\clubsuit$

(I):  $j=0 \rightarrow i+1$   
 (III):  $j=0 \rightarrow i+1$   
 (II):  $j=0 \rightarrow 2(n-i)-1$

#### (8) Fancy 12 Pattern

$n=5$

outer loop  $\rightarrow 0 \rightarrow n$   
 inner loop:  $n_0 \rightarrow 1$  times  
 $n_1 \rightarrow 3$  times  
 $n_2 \rightarrow 5$  times  
 $n_3 \rightarrow 7$  times  
 $n_4 \rightarrow 9$  times

$j: 0 \rightarrow 2i+1$

what to print?  
 check if  $j \% 2$  even  $\rightarrow$  no.  $(i+1)$   
 odd  $\rightarrow *$

#### (9) Full fancy 12

lower half:  $i=0 \rightarrow n$   
 inner:  $i=0 \rightarrow 5$  times  
 $i=1 \rightarrow 3$  times  
 $i=2 \rightarrow 1$  time  
 $j: 0 \rightarrow 2(n-i)-1$

$i=2j$

even  $\rightarrow n-i$   
 odd  $\rightarrow *$

⑩ ABCBA pattern

A  
ABA  
ABCBA  
ABCDcba  
ABCDcba  
=

char ch = 'A';  
cout << "Enter 'A':";  
cin >> ch;  
if (ch == 'A')  
{  
 cout << "A";  
 cout << "B";  
 cout << "C";  
 cout << "B";  
 cout << "A";  
}

Bitwise Operators and Functions (Live class) 13 May 2024

Bitwise Operators

- & (and)
- | (or)
- ^ (xor)
- ~ (not)
- << (left shift)
- >> (right shift)

\* avoid using % → computation intensive operation  
instead use "&" → faster

foreg:  $n \% 1 \rightarrow 0 \text{ or } 1$  (eg: 481 → 0, 581 → 1)  
 $\downarrow \text{even} \quad \downarrow \text{odd}$  (eg: 481 → odd, 581 → even)

\* XOR (^): very important application (asked many times) : find unique number. eg: 3, 8, 7, 4, 4, 12, 3, 12, 8.

$$3^8^7^4^4^12^3^12^8 \\ \downarrow \text{ans} \quad \checkmark$$

Set bit :

eg: 0000 --- 000101 : 5

$\frac{n}{41}$

$\frac{1}{\text{LSB}} \rightarrow \text{LSB}, 0 \rightarrow 0$   
LSB set bit

numb(n+);  
↳ set bit

$\text{numb}(\text{numb}(n+)) \rightarrow \text{return rightmost } 1$

$\Rightarrow 5: 0000 --- 00101$   
 $\frac{01}{1}$  1st  
set bit

$\gg 1 \Rightarrow 000 --- 0010$   
 $\frac{01}{1}$  2nd  
set bit

$\gg 1 \Rightarrow 00000001$   
 $\frac{01}{1}$  2nd  
set bit

Homework: Bitwise Operators questions will be added (SHORTCUTS A)

### Functions

eg: int main() {

    a();  
    return 0;

}

int a() {

    b();  
    return 1;

}

int b() {

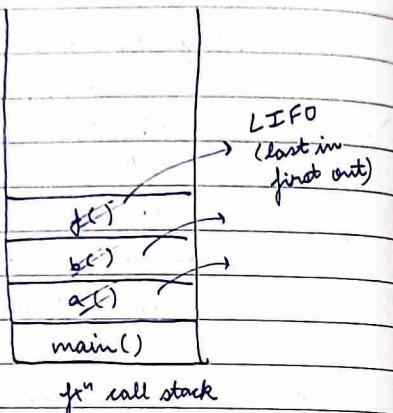
    c();  
    return 2;

}

int f() {

    return 3;

}



fun call stack

eg: (code) int main() {

    cout << 1;

    solve();

    cout << 2;

    return 0;

}

O/P = 1342

$$\text{eg: sum of AP} = \frac{n}{2} (a+l)$$

eg: Prime no. check (n=7)

- 2 → 7%2 = 1
- 3 → 7%3 = 1 } non-zero remainders
- 4 → 7%4 = 3 } → prime
- 5 → 7%5 = 2 }
- 6 → 7%6 = 1 }
- 7 → 7%7 = 0 }

② Pass by value / Pass by reference

→ normally used  
→ need to jab aro ka track  
actual value  
me change hota hai

Pass by value

eg: int main() {  
    void solve(int a) {  
        int a=15; 104 address  
        a++ ; 15  
        a++ ; 16  
        cout << a;  
        a++ ; 17  
        cout << a; 18  
    }  
    solve(a);  
    a++ ; 19  
    cout << a; 20  
}

eg: Pass by reference → void solve(int &a) { a=a+10; }

Reference value variable int age=15;



↓  
done

15

age

(memory location ko ek or usam  
edia)

HomeworkWeek-2 assignments① Numeric hollow half pyramid

1

1 2

1 3

1 4

1 2 3 4 5

n=5

for (i=0 → i &lt; n) {

for (j=0 → j &lt; i+1) {

for (j=0 → j &lt;= i) {

if (j==0 || i==n-1 || j==i) {

cout &lt;&lt; j+1; }

else { space; }

}

}

}

## ②

Numeric hollow inverted half pyramid

0 1 2 3 4 5

n=5

1 2

5

2 3

5

3 4 5

4 5

① j == i+1

② j == n

③ i == 0

for (i=0 → i &lt; n) {

for (j=i+1 → j &lt;= n) {

if (i==0 || j==i+1 || j==n) {

cout &lt;&lt; j;

}

else { " "; }

}

endl;

}

(3) Numeric Palindrome Equilateral pyramid  $n=5$  left and right both side se barabar

0	- - - 1	nos. $K < N \rightarrow i++$	row: $i=0 \rightarrow i < n$
1	- - 1 2 1	3 < 6	col: $j=0 \rightarrow j < k \quad (k++)$
2	- 1 2 3 2 1	5 < 7	Spaces: $i=0 \rightarrow 4$
3	- 1 2 3 4 3 2 1	7 < 8	$i=1 \rightarrow 3$
4	1 2 3 4 5 4 3 2 1	9 < 9	$i=2 \rightarrow 2, \quad j < N-i-1$
	0 1 2 3 4 5 6 7 8		$i=3 \rightarrow 1$
	numbers $\Rightarrow$ <del>int c=1;</del> cont << c;		$i=4 \rightarrow 0$

eg:  $i=3, \quad c=1$

1 2 3 4 3 2 1

$\downarrow$   
 $c=5 \rightarrow c=c-2$

Pseudocode ①  $n=5; K=n;$

②  $\text{for}(\text{int } i=0 \rightarrow cn) \{$

int c=1;

③  $\text{for}(\text{int } j=0; j < k) \{$

④ if ( $j < n-i-1$ ) { print space}

else if ( $j < n-1$ ) { print c; c++ }

else if ( $j = n$ ) { c=c-2; print c; c--; }

else { cont << c; c--; }

$k++;$   
cout << endl; }

(4) Solid half diamond

$n=5$

0 ★ 1 2 3 4

rows  $\Rightarrow i=0 \rightarrow 9$   $(2n-1)$

1 ★ ★

columns: cond? ① if ( $i < n \rightarrow \text{cond} = i$ )

2 ★ ★ ★

3 ★ ★ ★ ★

② else  $\Rightarrow \text{cond} = n - (i \% n) - 2$

4 ★ ★ ★ ★ ★

$j=0 \rightarrow j < \text{cond} \{$

5 ★ ★ ★ ★

cont << "★";

6 ★ ★ ★

}

7 ★ ★

8 ★

$i=5 \rightarrow 4$

$(i \% N) \Rightarrow 0$

$N - (i \% S) \Rightarrow 5 - 2 = 3$

$i=6 \rightarrow 3$

$i \% S \Rightarrow 1$

$4 - 2 = 2$

$i=7 \rightarrow 2$

2

$3 - 2 = 1$

$i=8 \rightarrow 1$

3

$2 - 2 = 0$

### ⑤ Fancy Pattern 1

(This pattern can go from  $N=1$  to  $N=9$  only)

\*\*\*\*\* 1 \* \* \* \* \*  
 \* \* \* \* \* \* 2 \* \* \* \* \*  
 \* \* \* \* \* \* 3 \* 3 \* 3 \* \* \* \*  
 \* \* \* \* \* 4 \* 4 \* 4 \* \* \* \*  
 \* \* \* \* 5 \* 5 \* 5 \* 5 \* \* \* \*

col  $\rightarrow$  17 items

$N=5$

now  $\rightarrow i=0 \rightarrow i < N$

col  $\rightarrow j=0 \rightarrow j < 17$

$i=0 \rightarrow 8^{\text{th}}$  index  $\Rightarrow$  printing

$i=1 \rightarrow 8-1 \rightarrow 7^{\text{th}}$  index

$i=2 \rightarrow 8-2 \rightarrow 6^{\text{th}}$  index ---

↓  
start  $\rightarrow 8-i$

digit printing  
 $i=0 \rightarrow i+1=1$       times  
 $i=1 \rightarrow i+2=2$

### ⑥ Fancy Pattern 2

$N=4$

0 1 2 3 4 5 6

2 \* 3

2 4 \* 5 \* 6

3 7 \* 8 \* 9 \* 10

7 \* 8 \* 9 \* 10

4 \* 5 \* 6

2 \* 3

1

#### ① growing phase

0 1 2 3

2 4 5 6

3 7 8 9 10

7 8 9 10

0 1 2 3

1 4 5 6

2 3

1

now  $\rightarrow 0 \rightarrow c_n$

col  $\rightarrow 0 \rightarrow i$

int c=1  $\rightarrow$  c++

#### ② shrinking phase

$c=11 \Rightarrow$  start  $= n - N$

0 1 2 3

1 4 5 6

2 3

1

$j=1 \rightarrow$  start=4

update  $\Rightarrow$  start  $- (n-i-1)$

### ⑦ Fancy Pattern 3

$N=5$

8

\* 1 \*

\* 1 2 1 \*

\* 1 2 3 2 1 \*

\* (2 1 \*

\* 1 \*

\*

now:  $0 \rightarrow c_n$

col:  $i=0 \rightarrow j=0$  <sup>index</sup>

$i=1 \rightarrow j=1$

$i=2 \rightarrow j=2$

$i \rightarrow j=2*i$

growing

### ⑧ Floyd's Triangle

$N=7$

1

2 3

4 5 6

7 8 9 10

11 12 13 14 15

16 17 18 19 20 21

22 23 24 25 26 27 28

row:  $0 \rightarrow < 7$

col:  $0 \rightarrow < i$

int count=1  $\rightarrow$  count << count.

count++

### ⑨ Pascal's Triangle

: binomial coefficient

1

1 2

1 3 1

1 4 6 4 1

1 5 10 10 5 1

1 6 15 20 15 6 1

$c = c * (i-j) / j;$

$j = [1, N]$

$j = [1, i]$

10

### ⑩ Butterfly Pattern

$N=5$

0 1 2 3 4 5 6 7 8 9

spaces

8

$2^{*(5-i-1)}$

$\Rightarrow 2^{*(N-i-1)}$

6

4

2

0

0

2

4

6

8

8

9

cond<sup>n</sup> (for \*)

cond<sup>n</sup> (for space)

$N+(n-i-1)$

$i-cond^n-1$

Fundam

① KM to miles  $\rightarrow 1\text{km} = 0.621371\text{ miles}$

② Print all digits of an Integer

eg:  $N=1234$

$N \% 10 \rightarrow \text{remainder} = 4$

$N / 10 \rightarrow \text{get next digit} \Rightarrow 123$

while ( $N > 0$ ) {

① one place  $= N \% 10$

② cont  $\ll$  one place;

③  $N = N / 10$ ;

}

(left to right order wrt n)

③ Display area of circle :  $a = \pi * r * r = (\pi * r)(r)$

④ no. is even or odd?

m-1:  $N \% 2 == 0 \rightarrow \text{even}$

m-2: bitwise method eg: 5  $\rightarrow 000101$

↓ even: LSB: 0 always  
odd: LSB: 1 always

if  $(N \& 1) == 0 \rightarrow \text{even}$  else odd

⑤ Find factorial of a number : eg: 5!

for ( $i=1$ ;  $i \leq 5$ ;  $i++$ ) {

fact = fact \* i;

}

$i=1 \Rightarrow \text{fact} = 1 \times 1 = 1$

$i=2 \Rightarrow \text{fact} = 1 \times 2 = 2$

$i=3 \Rightarrow \text{fact} = 2 \times 3 = 6$

$i=4 \Rightarrow \text{fact} = 6 \times 4 = 24 = --$

⑥ No. is

prime or not? : N is prime when it has only 2 factors: 1 & N.

eg:  $N=5$      $5 \mid 1$      $5 \mid 2$      $5 \mid 3$      $5 \mid 4$      $5 \mid 5$

↓

$N \oplus \Rightarrow i \in [2, \dots, (N-1)]$

if  $(N \% i == 0) \{$     optimised  $\Rightarrow$  for ( $i=2$ ;  $i \leq \sqrt{N}$ ;  $i++$ )  
    // not prime

}

⑦ Print all prime from 1 to N

for ( $i=2 \rightarrow i \leq N$ ) {

    bool isPrime = checkPrime(i);

    if (isPrime) { i };

        → created in ⑥ op 11

⑧ Reverse integer

leetcode 7. algorithm. if  $N=123$

$\Rightarrow 3 \mid 2 \mid 1$

300

20

1

(but we don't know if it's 3 digit no.)

$\Rightarrow 3 \times 10^2 + 2 \times 10^1 + 1 \times 10^0$

$\Rightarrow \text{remainder} = N \% 10 \rightarrow 3$

(whichever) ans = 0

① ans = ans  $\times 10 + \text{rem} \rightarrow 0 \times 10 + 3 = 3 \Rightarrow N = N / 10 \Rightarrow N = 12$

② ans = 3  $\times 10 + 2 = 32 \Rightarrow N = N / 10 \Rightarrow 1$

③ ans = 32  $\times 10 + 1 = 321$

if  $n$  is -ve  $\Rightarrow |-123| \rightarrow 123$

↳ return → -ve

$\Rightarrow -123 \Rightarrow n = -(-123) \Rightarrow +123$

↳ reverse

$\rightarrow \text{isNeg} = 1$

↳ -321

o) gives runtime error (signed integer overflow)

if ( $x < \text{INT\_MIN}$ ) {

return 0;

}

while (-) { --

if ( $\text{ans} > \text{INT\_MAX} / 10$ ) {

return 0;

}

⑨ Set the  $k^{th}$  bit

eg:  $N = 10 \rightarrow 1010$

eg:  $K=2 \rightarrow 1110 \rightarrow 0/p + 14$

$$\begin{array}{r} \text{eg: } 1010 \\ \text{Binary} \quad | \\ \text{0100} \\ \text{OR} \\ \hline 1110 \end{array}$$

①  $N = 1010$

② Value  $\Rightarrow 1 < K$

③  $N \mid \text{value}$

eg:  $K=2 \rightarrow 1 \ll 2 \Rightarrow 100$

⑩ Convert the temperature

Lecture 24/69:  $i/p \rightarrow$  Celsius

$$K = C + 273.15$$

$$F = C * 1.80 + 32$$

LOR  
95

⑪ Count all set bits

Given an integer 'N', count no. of set bits in it.

eg:  $N = 34 \quad \text{Binary} = 100010$

eg:  $N = 7 \Rightarrow 111 \Rightarrow \text{set bit} = 3$

$\Rightarrow$  convert into binary and find ones in it.

M-1 ①  $\text{bit} = N \% 2;$

② if ( $\text{bit} == 1$ ) {count++;}

③  $N = N / 2;$

M-2 Bitwise method

$$T = "111"$$

W.Ko bitwise AND Kringentab us wo, ki

$$T \& 1 = 001$$

LSB mil jayegi then right shift. again AND with 1.

⑫ Create number using digits

eg: 1, 2, 3, 4, 5, 6  $\rightarrow 123456$

$$\begin{aligned} \text{num} &= 1 \rightarrow \text{num} * 10 \rightarrow 1 * 10 \rightarrow 10 + 2 = 12 \\ &\rightarrow 12 * 10 \rightarrow 120 + 3 = 123 \dots \end{aligned}$$

①  $\text{int num} = 0$   
 $\rightarrow "1" \rightarrow 0 \times 10 + 1 = 1 = \text{num}$

②  $\text{num} = \text{num} \times 10 + \text{digit};$

let's learn Arrays (live class)

15 May 2024

Arrays: fixed container which store SAME type items.

\* Creation of an array

syntex: datatype arrname [size];

Allocation of array (percentage value allocated by arr[1])

\* array elements must have continuous memory

eg:  $\text{int a}[5];$



\* Memory allocation: symbol table

(done by address,  $a \rightarrow 104$  (address)  
 not by array name)

BAD practice

\* Initialization of array

Method:  $\text{int arr}[5] = \{1, 2, 3, 4, 5\}$

\* if array size is large and elements given is less than

eg:  $\text{int arr}[5] = \{1, 2, 3\}$



syntex: datatype arrname [size];

\* fill (")

\* Indexing

Counting:  $1 \rightarrow n$  (has n numbers)

$0 \rightarrow (-1) ("")$

eg: int marks[6];, starting memory address 104, array size: 6, index: 0-5

marks	1	2	3	4	5
-------	---	---	---	---	---

⇒ 0 based numbering indexing in arrays.

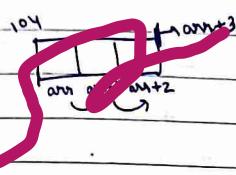
\* \* (Start base + i) + array size - 1  
arr: 0-n-1

\* fill:

eg: int arr[3] = {10, 20, 30}

syntax: fill (starting address, ending address, value)

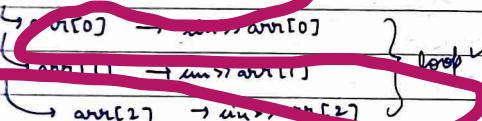
→ fill (arr, arr+3, 23)



\* Taking input

eg: int arr[3]

→ declare



for (int i=0; i<5; i++)

    arr[i] = cin>arr[i];

}

\* arr → 

104	105	106
-----	-----	-----

size of arr = 24 (104)

→ array ka number of elements kisne hai ye hum kisi formula se find out kri skte.

like like, agar ek variable create karne padega jo carry total hum lega kiske element array ke andar hain. (int n=2)

\* Why indexing start from 0?

arr[i] → value present at [base address + size\*i]

arr[i] → array size hai

eg: int arr[3]

if datatype (int = 4)

104 base address

105 106

arr 0 1 2 3 4

+ + +

value loc + at (104 + 4 \* 0)

: value at 104

arr[3]: = + (104 + (4 \* 3))

: value at 116

\* arr[i] ⇒ i[n]

↓ centre  
compiler (compiler) \* (i+n)

value present at base

eg: arr

104 1

→ value present at address (104+1)

→ .. ..

(104+12)

" .. .. "

116

size of datatype Kbase add base + i  
depends on Datatype  
10 → 107  
but me + one extra lagay  
base me + one extra lagay  
(byte)

Functions with Arrays

eg: int main()

    int arr[5];

    int size;

    cout << arr[0];

    size = arr[0];

}

    int val = arr[0];  
    int re;

}

\* arr → h → pointer

pass by reference ✓ → call ↓ value, it know larger

size → pass by value

## ① Algorithm → linear search



array [ ] = { 10, 20, 30, 40, 50 }



target  
find 53 → element not found

40 → element found

for (int i=0; i<5; i++)  
if (array[i] == target) {

else:

for (int i=0; i<5; i++)  
if (array[i] == target) {

## Q. Find max no. present in array.

To find max no.  
initialize  
array INT-MIN



int

range

$-2^{31} \rightarrow 2^0 - 1$

$\rightarrow 2^{31} \rightarrow \text{INT-MIN}$

To find min no.  
initialize  
array INT-MAX

INT-MIN

INT-MAX

## Q. count 0's and 1's in array



zeroCount = 0;

oneCount = 0 + 1 + 1 + 1 + 1 → 9

## 2 pointer technique

\* i/p → arr [ ] = { 20, 30, 40, 50, 60 }  
 $i=0$        $j=n-1$   
 $i=1$        $j=4$   
 $i=2$        $j=3$   
 $i=3$        $j=2$   
 $i=4$        $j=1$   
 $i=5$        $j=0$   
 $\rightarrow i < j \rightarrow \text{stop}$

o/p → 10 80 60 50 30 40    (reverse printing)

odd no. of elem → [ ] = { 10, 20, 30, 40, 50, 60, 70 }  
 $i=0$        $j=6$   
 $i=1$        $j=5$   
 $i=2$        $j=4$   
 $i=3$        $j=3$   
 $i=4$        $j=2$   
 $i=5$        $j=1$   
 $i=6$        $j=0$

while ( $i < j$ ) → algorithm second kaga deye i=j while use  
redundancy.

## (HW) Q

- ① Swap (swapping)  
 $\downarrow \downarrow \rightarrow \text{swap}()$   
 $\left[ \begin{array}{cc} 10 & 11 \\ 11 & 10 \end{array} \right]$  → algorithm  
 5 times  
 (swapping)
- ② reverse array

101      110  
 $a=a^{\wedge}b; b=b^{\wedge}a$   
 $a=a^{\wedge}b; b=b^{\wedge}a$   
 $a=a^{\wedge}b; b=b^{\wedge}a$   
 $\rightarrow a=a^{\wedge}b; b=b^{\wedge}a$

## ③ Watch Time & Space complexity recording

### An introduction to Time and Space complexity (recording)

#### What is Time Complexity?

- amount of time taken by an algorithm to run as a function of length of input.  $\rightarrow$  CPU operations (not actual time)

e.g.: for (int i=0; i<N; i++) {

    cout << "hi";

}

$N \uparrow \rightarrow$  time taken  $\uparrow$  or  
no. of operations  $\uparrow$

$\Rightarrow TC: O(N)$

#### Why to study Time and Space complexity?

- good computer engineer always thinks about the complexity of code written.  
 ◦ resources are limited.  
 ◦ measure algorithm to make efficient programs.  
 ◦ Asked by interviewer after ~~every~~ every solution you give.

What is space complexity?

- amount of space taken by an algorithm to run as a function of length of input.

eg: `int a=1; // variable`

`int b[5]; // array`

`for(int i=0→n);`

$O(1) \rightarrow \text{constant space}$

3

length n  
using n words

eg: `int n;`

`int *a=new int[n];`

$\text{f} \rightarrow \text{print array } b \Rightarrow \text{for}(int i=0 \rightarrow n; i++) \{$

`cout << b[i];`

eg:  $n=2^2$   
 $b[2]$

eg:  $n=2^{2000}$   
 $b[2^{2000}]$

3

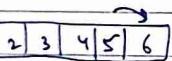
SC:  $O(n)$

units to represent complexity

1) **Big O:** upper bound  $\rightarrow$  (jada se jyada kitna time legi)  $\rightarrow$  worst case

2) Theta  $\Theta$ : average case

3) Omega  $\Omega$ : lower bound (Kam se kam kitna time lega)

eg: search: 

$\rightarrow$  item find  $\rightarrow$  ①  $\rightarrow$  omega :  $O(1)$

⑥  $\rightarrow$  Bigo :  $O(n)$

worst case

Big O : complexities

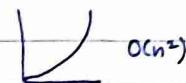
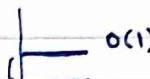
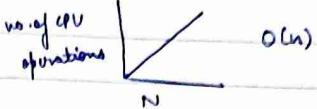
1. Constant time:  $O(1)$   $\rightarrow$  `int a=5;`

2. Linear time:  $O(n)$   $\rightarrow$  `for(int i=0→N) { cout << i; }`

3. Logarithmic time:  $O(\log N)$   $\rightarrow$  binary search

4. Quadratic time:  $O(N^2)$   $\rightarrow$  `for(i=0→N) { for(j=0→N) { } }`

5. Cubic time:  $O(N^3)$   $\rightarrow$  3 level nesting



$$\text{eg: } f(n) = (2n^2 + 3n) \rightarrow O(2n^2) \rightarrow O(n^2)$$

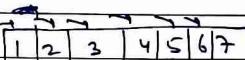
↑  
upper bound dekho

$$\text{eg: } N^2 + \log N \Rightarrow O(N^2)$$

$$\text{eg: } 200 \Rightarrow O(1)$$

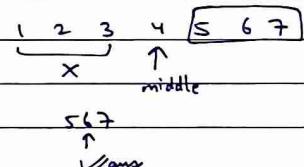
\* least complexity

most complexity  
 $O(1), O(\log n), O(\sqrt{n}), O(n), O(n \log n), O(n^2), O(n^3), O(2^n), O(n!)$   
 $\longrightarrow O(n^n)$

eg: 

① linear search  $\Rightarrow O(n)$

② binary search  $\Rightarrow O(\log n)$



$$N \xrightarrow{2} \frac{N}{2} \xrightarrow{4} \frac{N}{4} \xrightarrow{8} \dots \xrightarrow{1}$$

$$\frac{N}{2^k} = 1$$

$$\log_2 N = \log_2 k \Rightarrow K = \log_2 N$$

\* for(i){

$$3 \quad O(N) + O(M) \Rightarrow O(N+M)$$

for(j){

3

(not nested loop)

→ space

eg: ① int a=5;  
 $O(1)$

② int \*a = new int[N]  $\Rightarrow O(N)$

### Arrays - Class-2 (live class)

19 May 2024

lecture 136 → hashing method → megarray class  
loop  $i=0 \rightarrow N$   $\rightarrow O(N)$  : TC  
int ans=0;  $\rightarrow O(1)$  : SC  
Set of 0's & 1's

[Ques.] 0 1 1 0 0 1

MW → 0 0 1 1 0 0 1 1 0

(flip) 0 → 1      1 → 0  
1's complement

Q. 1 → -1      -1 → 1  
2's complement

0 0 0 1 1 0 0 0 0  
on set 0's and 1's  
MW

algorithms

① counting:  
zeroes = 3; ones = 5;  
3 zeroes start → one insert  
 $TC: O(N) + O(N) = O(N)$   
 $SC: O(1)$

Sort 0's and 1's

i/p 0 1 1 1 0 0 1 1  
o/p 0 0 1 1 1 1 1

eg: 0 1 1 1 0 0 1 1  
l = 0, h = 7, i = 0, j = 7  
TC: O(N)

② sorting: inbuilt sort function  
ending pointer → l = 0, h = n-1  
swap kinda until l <= h → 0-left 1-right [left part sorted]  
jobikma [right part unsorted]  
do [left part sorted] [right part unsorted]

Q. 10 20 30 40

i/p 0 1 2 3

0, 10 (0, 10) (2, 10) (0, 20) (40, 10)  
(10, 20) (20, 20)

0, 20 (0, 20) (10, 20) (20, 20) (40, 20)

0, 40 (0, 40) (10, 40) (20, 40) (30, 40) (40, 40)

print all pairs

Sol:  $i=0$  10 20 30 40  
 $j=0 \rightarrow n$   
 $i=1 \rightarrow n$   
 $i=2 \rightarrow n$   
 $i=3 \rightarrow n$

M-3 (variation)  
 $\text{for } i=0 \rightarrow n \{$   
 $\quad \text{for } (j=0; j < i; j++) \}$   
 $\quad \quad \quad \}$

M-4 (variation) upper Δ with diagonal  
 $\text{for } i=0 \rightarrow n \{$   
 $\quad \text{for } (j=0; j < i; j++) \}$   
 $\quad \quad \quad \}$

M-5  
 $\text{for } (i=0 \rightarrow n) \{$   
 $\quad \text{for } (j=i; j < n; j++) \}$   
 $\quad \quad \quad \}$

M-6 (variation) lower Δ counting  
 $\text{for } i=0 \rightarrow n \{$   
 $\quad \text{for } (j=i+1; j < i+2; j++) \}$   
 $\quad \quad \quad \}$

### Two Sum

i: 0	10	5	20	15	30
0 1 2 3 4					

target → 35  
check if pair that sums equal to target exists or not  
pairs:  
10, 10    5, 10    20, 10    15, 10    30, 10  
10, 5    5, 5    20, 5    15, 5    30, 5  
10, 20    5, 20    9, 20    15, 20    30, 20  
10, 15    5, 15    20, 15    15, 15    30, 15  
10, 30    5, 30    20, 30    15, 30    30, 20

logic:  $i=0 \rightarrow$   
 $j=20 \rightarrow$   
 $\rightarrow arr[i] + arr[j] = target$

Recursion function → int → int, int  
pair → int, int  
share → string

To do box: p.first  
p.second

Pair  
declaration  
 $\rightarrow \text{Pair<int, int>} p;$   
var.name  
initialize  
 $\leftarrow \text{pair<int, int>} = \text{make\_pair(0, 0)}$

access  
first = 100  
p.second = 200

### Print all triplets

10	10	10	10	20	30	40
0	1	2	3			
10	10	20	20	30	30	40
0	1	2	3			

$$4 \times 4 \times 4 = 64$$

64

~~to handle duplicates~~  
~~(10, 20, 30)~~  
~~(10, 20, 20)~~  
~~(10, 20, 10)~~  
~~(20, 30, 10)~~  
~~(20, 30, 20)~~

i	j	k
---	---	---

i: 0 → n  
j: 0 → m  
k: 0 → l  
TC: O(N<sup>3</sup>)  
SC: O(1)

Lecture 1

### Two sum

remove duplicate pair X  
(i-1)  
 $\text{for } (i=0 \rightarrow c) \{$   
 $\quad \text{for } (j=i+1 \rightarrow cn) \{$   
 $\quad \quad \quad \text{if } \{\text{arr}[i] == \text{arr}[j]\} \rightarrow \text{target} \}$   
 $\quad \quad \quad \}$

10	20	30	40
0	1	2	3

unique and relevant pairs  
refresh → & find all pairs  
 $\rightarrow$  clear & insert same target

TC: O(n<sup>2</sup>)  
SC: O(1)

H.W → watch vector STL recording

Three sum

Input: [10 20 30 40]

target → 70

find a triplet

non-duplicate  
 10 20 30 60  
 10 20 40 → 70  
 20 30 40 → 90

sum = target

TC: O(n<sup>3</sup>)

SC: O(1)

Leetcode 15.leet code↳ Sliding window

↳ element

↳ current

↳ window

eg: [10 20 30 40 50]

(element right side)

= [50 | 10 20 30 | 40]

eg: [10 20 30 40] → [50 | 60 | 70 | 30 | 40]

n = 2

Method 1: to b method → Step-1 (size lost in element in array)  
 Method 2: reverse add  
 n = 1-2: reverse add  
 1. reverse 1 → 1 2 3 4  
 2. first 2 → 1 2 3 4  
 3. sum reverse 1 2 3 4

Step-1: for (int i = 0; i < n; i++) {  
 Step-2: for (int j = i + 1; j < n; j++) {  
 Step-3: cout << temp array in original array printing

\* 6 places as diff Knoa → 0 place shift Knoa

7 " " " " → 1 " " " and so on...  
 modulus  
 whenever shift > size shift = digit % size

Open rule: C1 sum every arr.Vector STL (review)

- The standard Template Library (STL) provides a collection of template classes and functions that offer common data structures and algorithms to make programming more efficient and convenient.
- A vector in C++ is a dynamic array that can grow or shrink in size, making it a versatile and efficient data structure for storing and manipulating sequences of elements.

Features↳ Contiguous memory

eg: int arr[5];

↳ static array, static memory allocation

int n;

↳ dynamic array

int \*arr = new int[n];

(Dynamic memory allocation)

- In vector, there is no need to tell size of vector; just keep inserting values, STL will manage the allocation.

syntax: `vector<int> v;` variable nameTo access size: `v.size();`To insert value: `v.push_back(5);`

v.push\_back(10);

int n; size se sabhi baar

capacity size ↑ koi hi tak capacity nahi kro

1 1 1

2 8 2

4 3 1 3

48 4 1 2 3 1 4

8 5 1 1 2 3 1 7 5 1

ruhne ka capacity suna kisi suna add kar dia)

v.capacity()

Delete element: `v.pop_back();` (deleting from end)

- \* `v.at(i)` → print element at  $i^{\text{th}}$  index.
- \* `v.back()` → last element of vector (last element of contiguous memory block)

diff. ways to create vector

`vector<int> arr;`

`vector<int> arr(5);` o/p = -1 -1 -1 -1 -1 (from push and pop vector requirement)

`vector<int> arr = {1, 2, 3, 4, 5};`

`vector<int> arr(4) {{1, 2, 3, 4}, {5}};`

copy vector  
vector can be short, other datatype too

Eg: `vector<int> arr = {1, 2, 3, 4, 5};`

`vector<int> arr1(arr);`

\* Front element = `v[0]`

Front element: `v[v.size() - 1]`

OK  
 $\rightarrow v.front()$   
 $\rightarrow v.back()$   
 $\rightarrow v[v.size() - 1]$   
end element:  $v[2]$

another method to print elements of vector

```
for( auto it : vector<some> )  
    cout << *it << endl;  
}
```

### Features of vector:

1. contiguous memory
2. dynamic sizing
3. automatic reallocation
4. size and capacity
5. array-like access

### array class-3

(live class)  
20/May/2024

1D array: [10 20 30 40]

#### 2D arrays

(0,0)	c <sub>1</sub>	c <sub>2</sub>	c <sub>3</sub>
n <sub>0,0</sub>	(0,1)	(1,2)	(0,3)
n <sub>1,0</sub>	(0,1)	(1,2)	(1,3)
n <sub>2,0</sub>	(2,1)	(3,2)	(2,3)

arr[]  
memory



\* formula:  $i + \frac{c}{\text{total number of columns}}$  (convert 2D indexing to 1D)  
i: row index ; j: col index  
eg:  $4 \times 2 + 2 = 10$

#### creation

\* declare: `int arr[n][m];`  
→ garbage value (only in case of static array)  
→ zero (in case of dynamic array)

\* initialization: `int arr[4][3] = {{10, 20, 30},`

{11, 12, 13},

{14, 15, 16},

{20, 21, 22}};

{20, 21, 22}}

\* access: `arr[i][j]`  
rowIndex

\* print array:  
row0  
  | col0 col1 col2  
row1  
  | c1 c2  
row2  
  | c0 c1 c2

```
for(row0=0→<3){  
    for(col0=0→<3){  
        cout << arr[row][col];  
    }  
}
```

TC:  $O(n^2)$

Q. fill 2D array? = fill (2D arr[0] or n-odd + column\*col), value)

### Traversing

#### ① row-wise

10	20	30
110	20	130
210	220	230

if  $i = 10, 20, 30$   
 $110, 120, 130$   
 $210, 220, 230$

```
for (i=0 → < rowsize) {
    for (j=0 → colsize) {
        arr[i][j]
    }
}
```

TC:  $O(n^2)$   
or  
 $O(m \times n)$   
( $m \neq n$ )

#### ② col-wise

10	20	30
110	120	130
210	220	230

if  $j = 10, 20, 30$   
 $110, 120, 220$   
 $130, 210, 230$

```
for (col=0 → cn) {
    for (row=0 → cn) {
        arr[row][col]
    }
}
```

→ square matrix

#### ③ diagonal traversal

```
for (row=0 → cn) {
    for (col=0 → cn) {
        if (row=col) {
            cout << arr[row][col]
        }
    }
}
```

④ diagonal  
int j=nob[i];  
for (i=0; i < rows; i++) {  
 cout << arr[i][j];  
 j--;
}

### Input

eg: int arr[3][3] → for (i=0 → rowsize) {  
 for (j=0 → colsize) {  
 arr[i][j]
 }
 }

→ row wise

Q. Search an element (if it's present or not)  
if  $arr[i][j] == target$   
→ return true

10	20	30	40
110	120	130	140
210	220	230	240

target → 77  
target not legal but

void solve (int arr[2][2], int rowsize,  
int colsize) {

int arr[2][2]

### 2D array with function

```
int main() {
    int arr[2][2] = {0};
    int rowsize = 2, colsize = 2;
    solve (arr, rowsize, colsize);
}
```

void solve (int arr[2][2], int rowsize,  
int colsize) {

int arr[2][2]

gives error

### 2D array using vectors

int arr[4][3]

vector<vector<int>> arr(4, vector<int>(3, 0))


→ 2D array  
name  
no. of rows  
no. of columns  
value initialize

int rowsize = arr.size()

int colsize = arr[0].size();

\* array jab bhi ap pass kerte ho wo by default pass by reference hota hai,  
vector jab bhi ap pass kerte ho wo pass by value hota hai.

Q. find minimum value  
int minValue = INT\_MAX

```
for(i=0 → nS){  
    for(j=0 → cS){  
        minValue = min(minValue, arr[i][j]);  
    }  
}
```

70	23	41
2	69	42
56	1	18

→ final ans

nS: rowSize  
cS: colSize

TC: O(nxm)

SC: O(1)

Q. find maximum value  
int maxValue = INT\_MIN

1	20	30 → 60
4	50	60 → 150
70	80	90 → 240

Q. find sum

① row-wise sum

row0 int sum=0  
→ col0 + col1 + col2 → print sum

row1  
int sum=0  
→ col0 + col1 + col2 → print sum

row2  
int sum=0  
→ col0 + col1 + col2 → print sum

10	20	30
0	80	80
20	40	60

↓  
70 140 170

② col-wise sum

col0  
int sum=0  
→ row0 + row1 + row2 → print sum

col1  
int sum=0  
→ row0 + row1 + row2 → print sum

col2  
int sum=0  
→ row0 + row1 + row2 → print sum

### ③ Diagonal sum

for (i=0 → j){

sum = sum + arr[i][i];

}

10	20	30
15	20	50
25	10	10

HW → 40

### ④ Transpose of a matrix

m-① new empty array

→ new loop

→ old loop

→ arr[i][j]

10	11	12
20	21	22
30	31	32

10	20	30
11	21	31
12	22	32

m-② without making new array

→ swap (arr[i][j], arr[j][i]) → original array hi aajegi

(0,0)	0,1	(0,2)
10	20	30
30	21	32

dry run:  
do baat swap ho  
nhi hai

ek baat swap kro  
(upper triangle)

for (i=0; i<row; i++) {

    for (j=i; j<col; j++) {

        swap ✓

}

:

## Lecture 26.

### Week-3 assignment

①

Remove Duplicates from sorted array.

0	0	1	1	1	2	2	3	3	4
0	1	3	4	5	6	7	8	9	

$N=10$

0	1	2	3	4
---	---	---	---	---

$K=5$  (unique elements)

convert

0	1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---	---

unique

ANS → rearrangement return K

doesn't matter



Two pointer

$i =$

$j =$

fraction of unique elements

0	0	1	1	2	2	3	3	4
j	j							

$\text{if } (a[i] == a[j]) \rightarrow \text{duplicate}$

$i++$

else → non-duplicate

{  $i++$ ;  $a[j] = a[i]$ ;  $i++$  }

↓  
i ko j me store kardo (for rearrangement)

$\Rightarrow K=?$

$K = j+1$

TC:  $O(n)$

SC:  $O(1)$

Lecture 7.24.

## (2) Find Pivot index

num	1	7	3	6	5	6
sum	11					11

Incase of multiple pivot index,  
jo left me naga wala  
return karao hui

## (M1) → Brute force

loop  $\rightarrow i \rightarrow [0 \rightarrow 5]$ 
~~for (int j=0; j < i; j++) {~~  
~~leftsum += a[j];~~

(j index ke bare mei  
inlude kro)

~~for (int j=i+1; j < n; j++) {~~  
~~rightsum += a[j];~~
~~i=0, lsum=0; rsum=17~~
~~i=1, lsum=1; rsum=20~~
~~i=2, lsum=8; rsum=80~~

outer loop  
 $Tc: O(n)$   
 inner loop  
 $O(n) - O(n)$   
 $Tc \Rightarrow O(n^2)$   
 $Sc: O(1)$

~~i=3, lsum=11; rsum=11 ✓  $\Rightarrow$  return i~~

0	1	2	3	4	5
lsum	0	1	8	11	17

~~rsum~~ 2 + 20 17 11 ← 6 0
 $Tc: O(n)$ 
~~for (i = ; i < nums.size(); i++) {~~
~~lsum[i] = lsum[i-1] + num[i-1];~~

}

~~for (i = ~~n-2~~; i >= 0; i--) {~~
~~rsum[i] = rsum[i+1] + num[i+1];~~

}

## (3) Key Pair // Two sum

(M-1) Page 59

(M-2) Two pointer approach

$$\begin{bmatrix} 1 & 4 & 4 & 5 & 6 & 10 & 8 \end{bmatrix} \xrightarrow{\text{sort}} \begin{bmatrix} 1 & 4 & 6 & 8 & 10 & 15 \end{bmatrix}$$
 $i = 0$  $j = n - 1$ while ( $i < j$ ) {     $csum = a[i] + a[j]$     if ( $csum == \text{target}$ )

return true;

    else if ( $csum > \text{target}$ )         $j--$ 

else {

 $i++$ 

}

(1)  $i = 0, j = 5$  $a[i] + a[j] = 16$  $csum = 16 \Rightarrow j--$ i.e.  $\text{target} = 16$ (2)  $i = 0, j = 4$  $csum = 11 \Rightarrow i++$ sort:  $O(n \log n)$ loop:  $O(n)$ TC:  $O(n \log n)$ TC:  $O(n \log n)$ SC:  $O(1)$ 

## (4) Leetcode 268.

## Missing Number (done in searching &amp; sorting class-1)

another method:  $\text{sort}(\text{arr.begin()}, \text{arr.end()})$   
 $\Rightarrow (i=0; i<\text{arr.size()};)$   
 $\quad \text{if } (\text{arr}[i] == \text{arr}[i+1]) \quad \text{continue}$   
 $\quad \text{else}$   
 $\quad \quad \text{return } i$   
 $\}$   
 $\text{return } \text{arr.size();} \rightarrow \text{corner case}$

XOR method:  $9^6^4^2^3^5^7^0^1$   
 $(\text{XOR with index}) \quad 0^1^2^3^4^5^6^7^8^9$   
 $\text{TC: } O(n) \rightarrow \text{optimized}$   
 $\text{SC: } O(1)$

 $(A^A = 0)$ 

## Leetcode 643.

## (5) maximum average subarray

$$\begin{bmatrix} 1 & 22 & -5 & -6 & 50 & 3 \end{bmatrix}$$
 $0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5$ 
 $K = 4 \quad (\text{length})$   
 $\frac{1}{4} \text{ of subarray}$ 

(M-1) ~~Brute force~~ ~~Brute force~~  
 find all subarray sum of length K

$$\begin{bmatrix} 1 & 12 & -5 & -6 & 50 & 3 \end{bmatrix}$$
 $i \quad j \quad k$ (1)  $i = 0; j = 3; \text{sum} = 2$ (2)  $i = 1; j = 4; \text{sum} = 51$ (3)  $i = 2; j = 5; \text{sum} = 42$ 
 $\Rightarrow \text{average} = \frac{\max \text{sum}}{\text{(max)}} = 12.75$ 
TC:  $O(N^2)$ 

## (M-2) Sliding Window Method

(1)  $i = 0, j = k - 1, \text{sum} = 2$ (2)  $i = 1, j = 1, \text{sum} = 12 - 6 + 50 = 56$ (2)  $\text{sum} = 2 - 1 = 1, \text{sum} = \text{sum} - \text{num}[i]$  $\text{sum} = 1 + 50 = 51$  $\text{sum} = \text{sum} + \text{num}[j]$  $\text{sum} = \text{sum} + \text{num}[i+1]$  $\text{sum} = \text{sum} + \text{num}[j+1]$  $i++; j++$ (3)  $\text{sum} = 51 - 12 = 39$  $\text{sum} = 39 + 3 = 42$ 

$$\begin{bmatrix} 1 & 12 & -5 & -6 & 50 & 3 \end{bmatrix}$$

## Leetcode 75.

## Sort colors (Sort an array of 0, 1, 2)

$$\begin{bmatrix} 2 & 0 & 2 & 1 & 1 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 0 & 0 & 1 & 1 & 1 & 2 \end{bmatrix}$$

(M-1) sorting (using STL) TC:  $O(n \log n)$  SC:  $O(n)$

(M-2) counting method → not sorting in place (ignore this method)

$$\text{eg: } \begin{bmatrix} 2 & 0 & 2 & 0 & 1 & 1 & 0 \end{bmatrix}$$

zero: 2 → ①

one: 2 → ②

two: 0 → ③

step 1

step 2

step 3

→ put zeros then ones then two in array

TC:  $O(n)$ SC:  $O(1)$

### M-3 (in-place) 3-pointer approach



(m should point at 1)

```
if (nums[m] == 0) swap(nums[l], nums[m])
l++, m++;
```

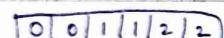
```
else if (nums[m] == 1) {m++;}
else {swap(nums[m], nums[h]); h--}
```



$m \leftarrow m + 1$



$m \leftarrow m + 1$



$m \leftarrow m + 1$

stop loop when ( $m > h$ )

### M-7 Move all zeros to one side of an array

eg:  $[1|2|-3|4|-5|6]$  → order maintenance not required  
 ① sort :  $[-3|-5|1|2|6]$  → STL wala TC:  $O(n \log n)$

### ② Dutch National Flag algorithm (2 pointer approach)

$l \downarrow$   
 $h \downarrow$   
 maintain zero, one, two.

while ( $l < h$ ) {



(0)

if ( $a[l] < 0$ ) { $l++$ ;



$l \leftarrow l + 1$

else if ( $a[h] > 0$ ) { $h--$ ;



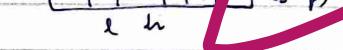
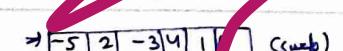
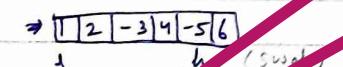
$h \leftarrow h - 1$

else {swap( $a[l], a[h]$ )}}

}

T.C:  $O(n)$

SC:  $O(1)$



(stop)

Lecture 28.7

### (8) Find duplicate number

eg:  $[1|2|2|2|2|2|2]$   
 $\downarrow$   
 $1|2|2|2|2|2|2$

$N+1=5$   
 $\downarrow$   
 $N=4$

$m = a[i] \in [1, n] \Rightarrow [1, 4]$

M-① sort →  $[1|2|2|2|2|2|2]$   
 $\downarrow$   
 $1|2|1|2|2|2|2$

b)  $i+1 \rightarrow$  same: duplicate

T.C:  $O(n \log n)$   
 SC:  $O(n)$

### M-② Negative marking method

$[1|3|4|2|2] \rightarrow N+1 \Rightarrow N=4$   
 $\downarrow$   
 $1|2|3|4|2|2$

$\rightarrow [1|3|4|2|2]$   
 $\downarrow$   
 $1|2|3|4|2|2$

①  $nums[nums[i]]$ , mark -ve

$nums[i] \rightarrow$  index  
 elements behave as index  
 ① iterate index  
 ② mark visited  
 ③ already visited  
 $\downarrow$   
 return duplicate

$[1|-3|4|2|2]$   
 $\downarrow$

$(-3) \text{ abs} \rightarrow 3 ; i++$

$[1|-3|4|-2|2]$   
 $\downarrow$

$i ; i++$

$[1|-3|4|-2|-2]$   
 $\downarrow$

$\text{return } \downarrow$

### M-③ Positioning method

$[1|3|4|2|2]$   
 $\downarrow$   
 $0|1|2|3|4$

$[1|3|4|2|2] \rightarrow [3|1|4|2|2] \rightarrow [2|1|4|3|2] \rightarrow [4|2|1|3|2]$

$\downarrow$

T.C:  $O(n)$   
 SC:  $O(1)$

$\boxed{2|1|2|3|4}$

extra element

⑨ Missing elements from an array with duplicates

$\rightarrow 1|3|5|3|4$        $N \rightarrow \text{size of array}$   
 $\begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{array}$        $i$   
 $\forall i, j \in [1, N]$

TC:  $O(n)$ SC:  $O(1)$ (M-1) Brute force method $\boxed{1|3|5|3|4}$  $\rightarrow 1|3|5|3|4$  $i$  $\rightarrow 1|3|5|3|4$  $i$  $\Rightarrow 1|3|5|3|4$ elements not visited  $\Rightarrow$  duplicate missing element(M-2) Sorting + swapping method $\boxed{1|3|5|3|4}$  $\begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{array}$ 

L sort

 $\boxed{1|3|3|4|5}$  $\begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{array}$ TC:  $O(n)$ SC:  $O(1)$ a[i]  $\rightarrow$  index
 $\begin{array}{c} 1|3|5|3|4 \\ \downarrow \quad \downarrow \quad \downarrow \\ 1|3|5|3|4 \end{array} \rightarrow \begin{array}{c} 1|5|3|3|4 \\ \downarrow \quad \downarrow \quad \downarrow \\ 1|5|3|3|4 \end{array} \Rightarrow \begin{array}{c} 1|4|3|3|5 \\ \downarrow \quad \downarrow \quad \downarrow \\ 1|4|3|3|5 \end{array}$ 
 $\Rightarrow 1|3|3|4|5$ 

## ⑩ Find first repeating element

 $\boxed{1|5|3|4|3|5|6}$  $0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6$ 

## (M-1) Iterate and check if element repeats

~~TC:  $O(n^2)$~~ SC:  $O(1)$ (M-2) Optimized solutionhashing① Traverse:  $O(n)$ 

store

1  $\rightarrow$  15  $\rightarrow$  2 ✓ (return)3  $\rightarrow$  24  $\rightarrow$  16  $\rightarrow$  1② Iterate  $\rightarrow$  check each element if it has occurrence later on.TC:  $O(n)$ SC:  $O(n)$ 

(11)

## \* Common elements in 3 sorted arrays

A  $\rightarrow 1|5|10|20|40|80$ B  $\rightarrow 6|7|20|80|100$ C  $\rightarrow 3|4|15|20|30|70|80|120$ ① if ( $A[i] == B[j] == C[k]$ )  $\rightarrow$  common found  
 $i++ ; j++ ; k++$ ② else if ( $A[i] < B[j]$ )  $\rightarrow i++$ ③ else if ( $B[j] < C[k]$ )  $\rightarrow j++$ ④ else  $k++$ \* if common elements are duplicate  
 $\rightarrow$  use setNote  $\rightarrow$  without using another data structureA, B, C  $\rightarrow$  remove duplicates.
 $T_C: O(n_1 + n_2 + n_3)$   
 $SC: O(\min(n))$   
 $n_1, n_2, n_3$  are lengths of arrays

 $A \rightarrow 3 \ 3 \ 3$   
 $B \rightarrow 3 \ 3 \ 3$   
 $C \rightarrow 3 \ 3 \ 3$ 

## (12) Wave Print a Matrix

0	1	2	3
1	2	3	4
2	5	6	7
3	9	10	11

output: 1 5 9 10 6 2 3 7 11 12 8 4

col  $\rightarrow$  0 1 2 3

TB BT TB BT

Top to Bottom Top to Bottom

(even col) (odd col)

lecture 54

## (13) Sprint + Print A matrix

0	1	2	3
0	1	2	3
1	4	6	

2 7 8 9

1 2 3 6 9 8 7 5

 $\rightarrow$  Printing:  
① starting row ;  
② ending col ;  
③ starting Row ;  
④ ending col ;  
update ;  
; - ;  
; + + ;

- (14) Add two numbers represented by two arrays. <sup>\* \*</sup>  
→ store no. in array

Q. add 2 no represented by array

$$A \rightarrow [9|5|4|9]^{+i}$$

$$B \rightarrow [2|1|4]$$

$$\begin{array}{r} A \\ 9 | 5 | 4 | 9 \\ \hline B \\ 0 | 2 | 1 | 4 \end{array} \quad i \quad j$$

assume  
output  $[9|7|6|3]$

array

Q. factorial.

$$7! \rightarrow 1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7$$

$\hookrightarrow 5040$

vector/array →

$$\text{array} \rightarrow [1|1|1|1|2|1]$$

carry = 0

i = 2

$$\text{int } x = \text{ans}[i] * i + \text{carry};$$

$$\text{ans}[i] = x \% 10;$$

$$\text{carry} = x / 10;$$

① ans.size = 1,  $x = 1 * 2 + c \rightarrow 2$

$$j=0 \quad a[j] \neq x \% 10 \rightarrow 2$$

$$\text{carry} = 2 / 10 = 0$$

if (carry) {  
    push carry; }

②  $i=3$ , int  $x = 2 * 3 + 0 = 6$

$$a[j] = 6 \% 10 = 6, c=0$$

③  $i=4$ ,  $x = 6 * 4 + 0 = 24$

→ reverse

$$a[j] = x \% 10 = 4, c = 24 / 10 = 2$$

④  $i=5$ ,  $x = 4 * 5 + 0 = 20$

$$a[j] = x \% 10 = 0, c=2$$

⑤  $i=6$ ,  ~~$x = 2 * 0 + 0$~~   $x = 7 * 20$

⑥  $i=7$ ,  $7 * 20 * 7 = 5040$

## SEARCHING AND SORTING

Searching and sorting class - 1 (live class)

22 May 2024

Linear search → linear search → T.C.: O(n)

(LS) S.C.: O(1)

Binary search → T.C.: O(log n)

(BS) S.C.: O(1)

Element search → T.C.: O(n)

S.C.: O(1)

### Binary search

(agar monotonic for do tab binary search se ha skta hoga a wo sikhna ek baar)

concerned basic function (element in ↑ or ↓ order)

i/p  $\rightarrow [2|8|10|20|30|34|46|78]^{n \text{ size}}$

start = 0, end = 7, mid = 3, target/key = 46

step 1: divide in 2 parts [mid = start]

mid =  $\frac{s+e}{2} = \frac{0+7}{2} = 3$   
② if arr[mid] == target {

    return true

    } L mid R

③ if mid val is not target then decide which part to choose (left or right) and go step again. (start = mid + 1)

o size:  $n \rightarrow n - n / 2 \rightarrow \dots \rightarrow 1$  (end = mid + 1)

if (target < arr[mid]) {

    s = mid + 1

    }

if (target > arr[mid]) {

    e = mid - 1

    }

invalid array  $\Rightarrow$  while(s < e) →isme chlne hai bas (invalid array, e nkt ja)

if (s > e) {

Leetcode 704.

\* int mid =  $\frac{s+e}{2}$  → out of range  
 INT-MAX BY INT-MIN

error free: int mid =  $s + \frac{e-s}{2}$

Time complexity:  $O(a) = O(\log n)$

→ size:  $n = \frac{1}{2^0} \rightarrow \frac{n}{2^1} \rightarrow \dots \rightarrow \frac{n}{2^{a-1}} = 1$   
 (a<sup>th</sup> iteration)

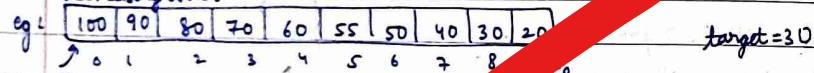
$$n = 2^{a-1}$$

$$n = 2^a$$

apply log.  $\Rightarrow \log n = \log_2(2^a)$

$$\log n = a$$

decreasing order

eg:   
 target = 30

$$\text{mid} = \frac{9}{2} = 4$$

\* if (target < arr[mid])

$$s = \text{mid} + 1$$

3

\* if (target > arr[mid]) {

$$e = \text{mid} - 1$$

}

STL (Standard template library)

binary\_search('array address, ending address, target')  
 binary-search(arr, arr+n, target);

Q. find first occurrence (return index)

20	20	20	30	40	50	60	70
s	0	1	2	3	4	5	e

target = 20

\* Store and compare (Bhayankar technique) → ans will make store karta  
 (it can be finalAns or ans blhi)  
 use local blhi operation  
 jaani rkho

20	20	20
mid	1	e

ans found → first occurrence  
 $e = m - 1$  → not first occurrence

⇒ Store index : ansIndex = ~~m~~ 0

left [20]	right
0	
mid	e

TC:  $O(\log n)$   
 SC:  $O(1)$

Q. find last occurrence

10	20	20	20	20	20	20	20	30
s	0	1	2	3	4	5	6	e

ansIndex = ~~m~~ 8

$$s = \text{mid} + 1$$

20	20	20	20	30
5	6	7	8	9

20	30
8	9

Leetcode 34:

Q. find total occurrence

10	20	20	20	20	20	30	40	50
0	1	2	3	4	5	6	7	8

target → 20

$O(\log n) \rightarrow$  first occ. → index

$O(\log n) \rightarrow$  last occ. → index + 5

$$\text{occurrence} = \text{last occ} - \text{first occ} + 1$$

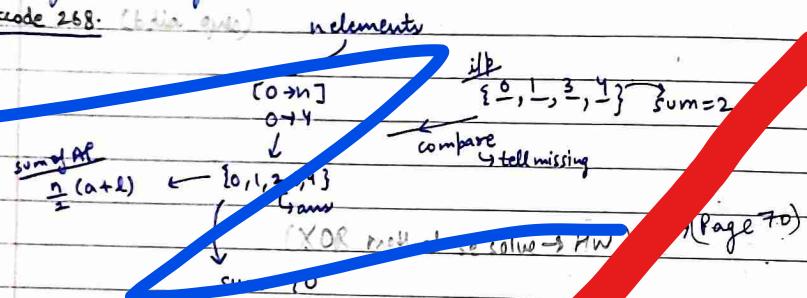
$$= 5 - 1 + 1$$

$$= 5$$

Ans: 5

\* Q. find Missing

Leetcode 268. (Editorial)



using binary search,

co. [3 4 0 1 2 1 8]  
arr [0 1 2 3 4 5 6 7]  
↓  
sort [arr, arr+n] → TC:  $O(n \log n)$

co.	[3 4 0 1 2 1 8]
arr	[0 1 2 3 4 5 6 7]
↓	
sort [arr, arr+n]	[0 1 2 3 4 5 6 7 8]

(Page 7.0)

if (number > index) {

// left

if (number == index) {

// right

discard this method

→ arr[mid] + 1 → missing no.

if (arr[mid] + 1 != arr[mid + 1]) → (or) if (arr[mid + 1] - arr[mid] != 1)

if (arr[mid] - 1 != arr[mid - 1]) → (or) arr[mid] + 1 → ans: arr[mid] + 1

arr[mid] - 1 → missing no. (or) if (arr[mid] - arr[mid - 1] != 1)

(extreme penultimate case)

return: arr[mid]

0	1	3	4	5	6
s	0	mid	3	4	e

observation: if diff → 0 → ans in right: s = mid + 1

else if diff → 1 → ans → store → mid  
 $e = mid - 1$ .

eg: extreme 0 wala case

1	2	3	4	5	6
s	0	1	2	3	e

ans = X

X 0

1	2
s	0

mid e

TC:  $O(n \log n)$   
SC:  $O(1)$

eg: extreme n wala case

0	1	2	3	4	5
s	0	1	mid	3	e

ans = -1

return my flag or handle  
this case

3	4	5
s	mid	e

s mid e

another method

(live class)  
Mega Class - Arrays  
26 May 2024

Hash maps (�द्वारा बनाए गए)

↳ tables

Key	value
1	53
2	54
3	55
4	56

unique (non-duplicating) ↳ jisko dhundhna hai

To implement:  
↳ unordered\_map <int, string> table-name;  
" " <int, int> " ;

insertion: table-name[key] = value;

eg: table[1] = 53;

iterator: unordered\_map <int, int> :: iterator i;

For each loop: for loop:

for (it = desk-map.begin(); it != desk-map.end(); it++) {

    int key = it->first;

    int value = it->second;

}

for-each loop:

for (auto it : desk-map) {

    int key = it.first;

    int value = it.second;

}

→ very fast in for-each loop → TC: O(1) in average case

Find an entry:

if (table-name.find(2) != table-name.end()) {

    // found

    int val = table-name[2];

}

else {

    // not found

}

deletion: table-name.erase(2);

Questions

1) 2's complement : 1's complement + 1

Q: array given having binary number.

eg: 

0	1	0	1	0
---	---	---	---	---

0 1 2 3 4 5

step1: 

1	0	1	0	0
---	---	---	---	---

0 1 2 3 4 5

step2: 

1	0	1	0	1
---	---	---	---	---

0 1 2 3 4 5

TC: O(n)  
O SC: O(n)

i=n-1 → 0  
① sum = a[i] + c  
carry

② a[i] = sum % 2  
(2%2=0)

③ c = sum/2  
(2/2=1)

\* if → binary array

\* p → complement array → size: binary array size+1  
(if sum = 0, 0, 0)  
↑ p → 111111

→ after all iterations, if (carry = 1) → a[0] = 1

leetcode 136

2) Single number : hashing method

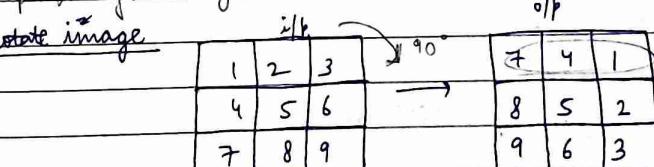
eg: 

4	1	2	1
---	---	---	---

no.	freq
4	1
1	2
2	2

leetcode 48 (Implementation of 2D arrays)

③ rotate image



↓ transpose

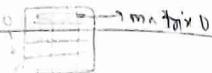
2) row wise reverse

(back transpose को दे

में लगा जाता है)

3) column wise reverse

```
vector<vector<int>> matrix () {
    int rows = matrix.size();
    int cols = matrix[0].size();
}
```



TC:  $O(n^2)$

Lecture 53. (that imp. ques) directly asked in interviews

#### Q) Maximum subarray

-2	1	-3	4	-1	2	1	-5	-4
0	1	2	3	4	5	6	7	8

① Brute force: find sum of all sub-arrays.  $\rightarrow$  TLE  $\Rightarrow$  TC:  $O(n^3)$

-2	-2 1	-2 1 -3	-2 1 -3 4	-2 1 -3 4 -1	-2 1 -3 4 -1 2	-2 1 -3 4 -1 2 1	-2 1 -3 4 -1 2 1 5	1
-2 1	-2 1 -3	-2 1 -3 4	-2 1 -3 4 -1	-2 1 -3 4 -1 2	-2 1 -3 4 -1 2 1	-2 1 -3 4 -1 2 1 5	1 -3	
-2 1 -3	-2 1 -3 4	-2 1 -3 4 -1	-2 1 -3 4 -1 2	-2 1 -3 4 -1 2 1	-2 1 -3 4 -1 2 1 5	1 -3 4		

② Kadane's Algo

for (int i=0; i<n; i++) {  
 for (int j=i; j<n; j++) {  
 if (sum == 1) {  
 sum = 1;  
 } else if (sum < 0) {  
 sum = 0;  
 }  
 sum += arr[j];  
 }  
}

③ Divide and conquer  
(bottom up)

Kadane's algo

TC:  $O(n)$

④ iterate KRO

sum KRO

ans ko update KRO

sum < 0

reset sum = 0

ans = -10  $\rightarrow$   $\frac{1}{2} \times 6$   $\rightarrow$  1 -1 -3 4 -1 2 1 5  
sum = 0  
Step ① sum =  $\frac{1}{2} \times 6$   $\rightarrow$  1 -1 -3 4 -1 2 1 5  
Step ② update ans  
Step ③ sum reset if sum < 0

TC:  $O(n)$

SC:

eg: if all elements are  $\neq$  then sum will be ans.

if all elements are  $\neq$  some badi element jo hoga wo ans ayega.

week-3 assignment: ① missing element from an array with duplicates.

eg: [1 3] -5 3 4 1 2 3 4 5

N=5

$a[i] \in [1, N]$

step ①  $a[i]$  index mando

step ② waha jisko ve kro

$\rightarrow a[a[i]] = -ve$  (agar  $> 0$  hai toh)  
eg: a[1], a[3], a[5]

→ jo index wo bach jayega wo ans. (jo ve hoi notes  
debara ve hui kro)

\* zero index ke random value daldo eg: v.insert(v.begin(), 757);

Q. (left in class)

single no. 2

single no. 3

now with max-1

majority element 1 ]  $\rightarrow$  Moore's voting algorithm

C++ STL containers (recording)  
27/ May / 2024  
↳ standard template library

### What is STL?

- It implements many popular and commonly used algorithms and data structures.

### Why we need STL?

- efficiency, productivity, safety, performance optimization, consistency, maintainability.

### Common components in STL

- Containers: vector, list, queue, stack, set, map etc.
- Algorithms: sort(), binary-search(), reverse(), etc.
- Iterators
- Functors

### Containers

- are classes or data structures that are designed to store and manage collections of objects. They provide a standardized way to store, retrieve and manipulate data in various ways.

### VECTOR

- Dynamic array that can grow or shrink in size.
- Allows fast random access to elements.
- Inception and removal of elements at the end is efficient.
- Suitable for most scenarios when elements need to be stored in a linear sequence.

### Member Functions

- begin(): returns an iterator pointing to the first element in the vector.  
↳ standard way to traverse over container  
↳ it → value at it ; it++

- end(): returns an iterator pointing to the position just after the last element in the vector.
- size(): returns the number of elements in the vector.
- push-back(): adds an element to the end of the vector.
- pop-back(): removes the last element from the vector.
- empty(): checks if the vector is empty (i.e. whether its size is 0).
- front(): accesses the first element in the vector.
- back(): accesses the last element in the vector.
- operator []: accesses the element at the specified index without bounds checking. (प्राप्त की जाने की वजह से इसका उपयोग किया जाता है) eg: marks[0]
- at (): accesses the element at the specified index with bounds checking. (मार्क्स[0]) eg: .
- capacity(): returns the number of elements that the vector can hold before needing to allocate more space.
- reserve (n): requests that the vector capacity be increased to atleast n elements, potentially reducing the no. of reallocations.
- max-size(): returns the maximum no. of elements that the vector can hold due to system or library limitations.
- clear(): removes all elements from the vector, which are destroyed, and leaves it with a size of 0.

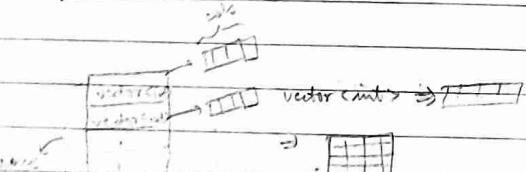
- insert (iterator position, value): Insert a new element before the specified pos.
- erase (iterator position) or erase (iterator first, iterator last): removes one or more elements from the vector starting at the specified position.
- swap (vector base): swap the contents of the vector with those of another vector of same type, including their sizes and capacities.

For-each loop

for each integer i inside vector v

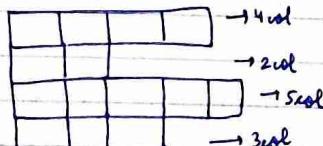
```
for(int i:v){  
    cout<<i;  
}
```

Iterator: `vector<int>::iterator`, `iterator.name = vector.name.begin()`,  
 e.g. `vector<int>::iterator it = distances.begin();`  
`while (it != distances.end()) {`  
 `cout << it; }`

2-D array using vector`vector<vector<int>>`

Syntax: `vector<vector<int>> arr (no. of rows, vector<int>(4,0))`  
 size  
 4  
 arr[2] row me kya loga?

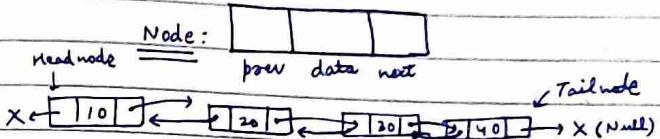
```
int totalRows = arr.size();
int totalcols = arr[0].size();
```

Jagged array : 4 rows

```
vector<vector<int>> arr(4)
arr[0] = vector<int>(4)
arr[1] = vector<int>(2)
```

LIST : linked-list → collection of nodes

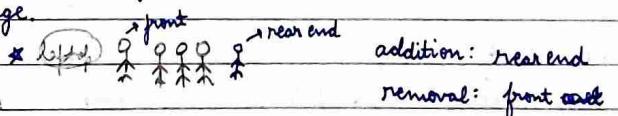
- Doubly-linked list
- Allows fast insertions and removals anywhere in the list.
- No random access like vectors.

Member functions

- same as vector.
- begin(), end(), size(), empty(), front(), back(), push\_back(), pop\_back(), erase(), clear(), insert(), swap().
- pop\_front(): removes the first element from list.
- push\_front(value): adds an element to the beginning of list
- remove(n): removes all elements from the list that are equal to the specified value.

QUEUE : → cannot iterate

- Adaptor or class that provides a First-In, First-out (FIFO) data structure.
- Implemented using other containers (e.g. deque, list) as the underlying storage.

Member functions (clear, etc. not listed).

- empty(): checks if queue is empty.
- size(), front(), back(), swap().
- front(): accesses the first element in queue, which is next element to be removed.
- back(): " " " last element, which is most recently added element.
- push(n): push to end of queue, pop(): removes first element.

 $O(1)$

STACK:

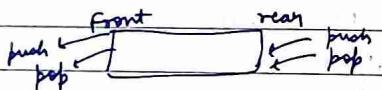
- Adapter class that provides a Last-In, First-Out (LIFO) data structure.
- Implemented using other containers (e.g.: vector, deque, list) as the underlying storage.

Member functions

- `empty()`, `size()`, `swap()`
- `top()`: accesses the top element of stack, which is most recently added.
- `push()`: adds an element to top of stack.
- `pop()`: removes the top element from stack.

DEQUE:

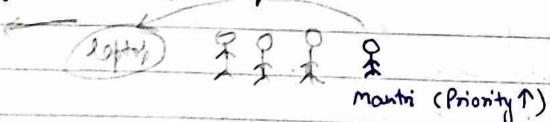
- Double-ended queue
- Similar to vectors but allows efficient insertion and removal at both ends.
- Suitable when elements need to be inserted or removed frequently from the front or back.

Member functions

- `begin()`, `end()`, `size()`, `empty()`, `front()`, `back()`, `operator[]`, `at()`, `push_back()`, `push_front()`, `pop_back()`, `insert()`, `erase()`, `clear()`, `swap()`.

PRIORITY QUEUE

- Adapter class that provides a priority queue (~~tree~~ (heap)).
- Elements are stored in a way that allows the retrieval of the highest-priority element efficiently.

Member functions

- `empty()`, `size()`, `swap()`.
- `top()`: accesses the element at the top of priority queue, which is largest or highest priority element, depending upon comparator used.
- `push()`: adds an element to priority queue and reorders it to maintain the heap property.
- `pop()`: removes the top element.

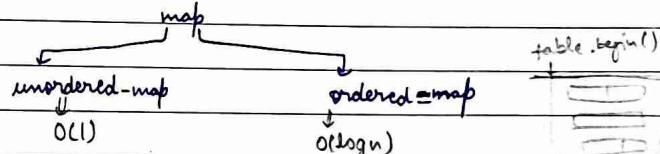
\* max-heap → max no. is highest value-priority.

\* min-heap → min no. is highest priority.

↳ Syntax: `priority_queue < int, vector<int>, greater<int> > pq;`  
badme p[adme]

MAP

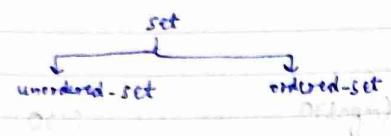
- Associative container that stores key-value pairs.
- Allows efficient retrieval and modifications of value based on keys.
- Keys are unique.

Member functions

- `begin()`, `end()`, `empty()`, `size()`, `operator[]`, `at()`, `insert()`, `erase()`, `clear()`
- \* `find()`: returns an ~~integer~~ iterator to the element with the given key, or `end()` if key not found.
- \* `count()`: returns the number of elements with the specified key (1 or 0) since `std::map` does not allow duplicate keys.

SET

- Sorted collection of unique elements.
- Elements are sorted in sorted order and duplicates are automatically removed.
- Provides efficient insertion, deletion and search operations.



### Member functions

→ begin(), end(), empty(), size(), insert(), erase(), clear(), find(), count()

## (LIVE) SEARCHING And SORTING Class-2 29/May/24

(Q) Find Binary search (Contd.) peak → first → rotated array

\* (Kakai imp)

Lectcode 852. Peak index in a Mountain array in  $O(\log N)$  BS

Ques

eg:  $0 \ 10 \ 5 \ 2$

eg:  $\begin{matrix} 10 & 20 & 70 & 60 & 50 & 30 & 15 & 5 \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \end{matrix}$

$s=0, e=7, mid=3$

⇒ if ( $arr[mid] < arr[mid+1]$ ) → line(A)

{  $s = mid + 1;$  }

else { mid line(B)

↓  
 $ans$  ↓  
 $e = mid$

$e = mid;$  ✓

}

dbt class:  $arr[mid] < arr[mid+1] \{$   
    → right  
         $mid + 1;$  }  
    else if ( $arr[mid] > arr[mid+1]$ ) {  
        left  
         $e = mid + 1;$  }  
    else {  $ans = mid;$  }

\* method-2: store and compare ✓

HW → multiple peaks/ mountains.

Lectcode 33. Pivot index. (Search in rotated sorted array)

↑ jaha orden change ho jaye.

$arr = 10, 20, 30, 40, 50, 60, 7 \rightarrow$  sorted

$70, 10, 20, 30, 40, 50, 60$

$60, 70, 10, 20, 30, 40, 50$

$50, 60, 70, 10, 20, 30, 40$  → sorted & rotated array

P

ans	50	60	70	10	20	30	40
	0	1	2	3	4	5	6

(A) → right  
(B) → left

\* if ( $\text{arr}[\text{mid}] > \text{arr}[\text{mid}+1]$ ) → pivot ✓ → return mid

if ( $\text{arr}[\text{mid}] < \text{arr}[\text{mid}-1]$ ) → mid - 1 ✓

?  $\text{arr}[\text{mid}] = \text{arr}[\text{mid}+1]$  ?  
return mid

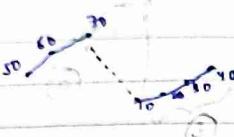
?  $\text{arr}[\text{mid}] = \text{arr}[\text{mid}-1]$  ?  
return mid

→ for yahan se done line (A) & (B) ↑ order me hoi

if ( $\text{arr}[\text{start}] \geq \text{arr}[\text{mid}]$ ) → line (B) → left jao.

else: line B element < line A element

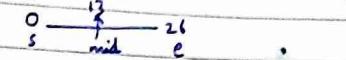
e.g. target = 20



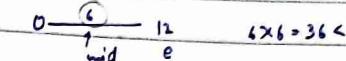
②  $\sqrt{54}$



$$27 \times 27 = 54 \times$$

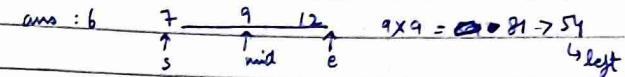


$$13 \times 13 = 169 > 54$$



$$6 \times 6 = 36 < 54$$

right (store)



$$9 \times 9 = 81 > 54$$

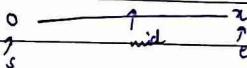
left



$$7 \times 7 = 49 < 54$$

(store)

int  $x \rightarrow \sqrt{x}$



### \* Search space pattern

↳ answer space → B.S → store and compute

①  $\text{sqrt}(x)$ : 0 → 100  
 $\sqrt{100} = 10$

while () {

if (predicate()) → return ans

if → left

else → right

}

while ( $s <= e$ ) {

if ( $\text{mid} * \text{mid} == x$ )  
↳ return mid

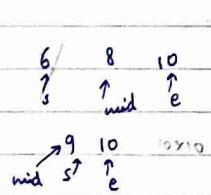
if ( $\text{mid} * \text{mid} > x$ )  
↳ left ⇒  $c = \text{mid} - 1$

else  
↳ right ⇒  $s = \text{mid} + 1$   
ans = mid

\* ans in float → caste

### Lecture 69

①  $\sqrt{100} = 10$   
0 → 100  
mid = 50  
s = 0  
end = 100



ans ↓  
5 ↓  
↓  
10 ↓

10 ✓

### 2D array searching

\* 2D → 1D →  $[c * i + j]$

\* 1D → 2D →  $i = \text{mid} / c$   
 $j = \text{mid} \% c$

### Lecture 74

O(logn)  
⇒ O(log(logn \* col))

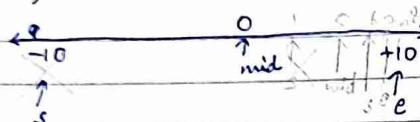
# (Line)

## Searching and sorting Class-3

30 May 24

- Q. if  $\neq$  divisor and dividend  $\rightarrow$  given  
 find quotient without using "/" or "%"  
 $\text{divisor} \times \text{quotient} + \text{remainder} = \text{dividend}$

Eg: dividend = 10, divisor = 2



$\text{mid} \rightarrow 0$   
 $\text{divisor} \times \text{q} + r = \text{dividend}$

$$2 \times 0 \leq \text{dividend}$$

$$0 \leq \text{dividend}$$

store and compute ans  $\rightarrow 0 \rightarrow 10 \rightarrow 5$

$$2 \times 8 \leq 10$$

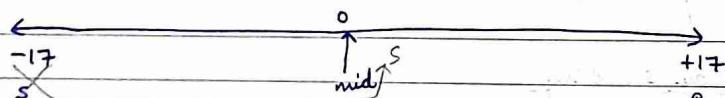
$16 \leq 10$   
 false

Eg: dividend = 17, divisor = 4

$$\max\text{-ans} = +17$$

$$\min\text{-ans} = -17$$

search space  $\rightarrow$  ans  $\rightarrow$  quotient  
 ↓  
 mid



$\text{divisor} \times \text{quotient} \leq \text{dividend}$

$$4 \times 0 \leq 17$$

$$0 \leq 17$$

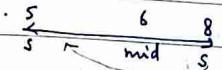
ans  
 ↓  
 0 (0 ke liye true hain toh s)  
 ↓  
 next jisko wale ke liye kisi 1 (true koga)  
 4  
 $4 \times 9 \leq 17$

$36 \leq 17$   
 false  $\rightarrow$  left



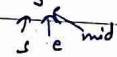
$$4 \times 4 \leq 17$$

$16 \leq 17$   
 T



$$4 \times 6 \leq 17$$

$24 \leq 17 \rightarrow F$

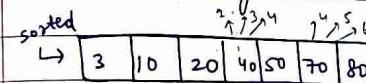


$$4 \times 5 \leq 17$$

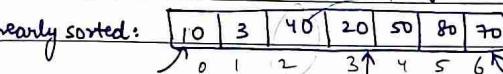
$20 \leq 17 \rightarrow F$

4 ans

- Q. \* Search in a nearly sorted array



arr[i]  $\rightarrow$  arr[i+1]  
 arr[i]  $\rightarrow$  arr[i+1]



nearly sorted:  
 ↓  
 10 3 40 20 50 80 70  
 ↑ 0 1 2 3 4 5 6  
 left ans mid right  
 (10 is already checked w/ its mid-1) left  $\Rightarrow$  e = mid-2  
 (50 .. mid+1) right  $\Rightarrow$  s = mid+2

target = 70

Leetcode 540.

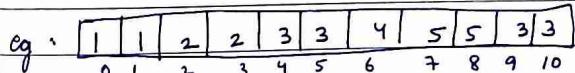
- Q. Odd occurring element.

(A) all element occurs even no. of times except one.

(B) element repeats itself in pairs.

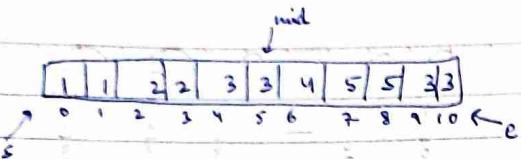
(C) no pair repeats itself, no number can occur more than 2 times in a single stretch.

(D) find element that occurs odd times.



Algo  $\rightarrow$  XOR  $\Rightarrow$  TC: O(n)

map  
 {  
 1 → 2  
 2 → 1  
 } even  $\Rightarrow$  TC: O(n),  
 3 → 1  
 5 → 2  
 4 → 1 odd



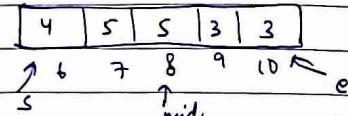
3 → pair → ✓ → 1<sup>st</sup> element index = 2 (even)  
↳ ans right me hai.

3 element → 1<sup>st</sup> element index = 9 (odd)  
↳ ans left me hai.

mid = 5;

↳ pairIndex = 4 (even)  
↳ move right

TC: O(log n)  
SC: O(1)

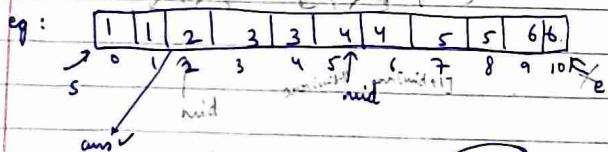
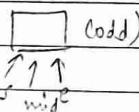
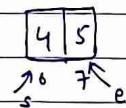


mid = 8

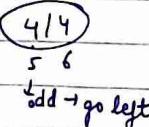
↳ pairIndex = 7 (odd)  
↳ move left

mid = 6

↳ pair which is  
↳ ans mil gaya



mid + 5 index  
↳ element = 4



↳ odd → go left

Case I → single element

Case II → no duplicate

Case III → left side duplicate

Case IV → right side duplicate

## SORTING ALGORITHMS

[recorded]

Bubble Sort → Torden me sort kro

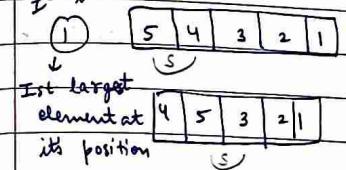
eg: N=5



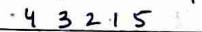
→ sort: [1, 2, 3, 4, 5]  
      0 1 2 3 4

7) Swap the adjacents if needed till we get all the array sorted.

1<sup>st</sup> iteration



② 2<sup>nd</sup> largest at its position



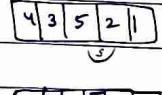
3 4 2 1 5

3 4 2 1 5

3 2 4 1 5

3 2 4 1 5

(3 comparisons)



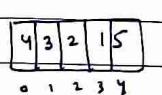
③ 3<sup>rd</sup> largest at its position

3 2 1 4 5

2 3 1 4 5

2 1 3 4 5

(2 comparisons)



④ 4<sup>th</sup> largest at its position

2 1 3 4 5

1 2 3 4 5

(1 comparison)

N=5

outer loop: 0 --- (n-1) → [0, 4)

comparisons: (n-1), (n-2) --- 1

→ Sum = 1 + 2 + 3 --- (n-2) + (n-1)

$$S_n = \frac{n(n-1)}{2}$$

$$O(n) = O\left(\frac{n^2 - n}{2}\right) = O(n^2) \rightarrow \text{TC (not good)}$$

$$\text{SC: } O(1)$$

Selection Sort

What if I select the minimum element & put it at <sup>left</sup> position.

eg: 44 33 55 22 11

- ① 11 33 55 22 44
- ② 11 22 55 33 44
- ③ 11 22 33 55 44
- ④ 11 22 33 44 55

→ for its iteration, pick smallest element from i to (n-1) index & swap it with  $i^{th}$  element.

$i \rightarrow 0 \rightarrow n-1$

$i \in [0, n-1]$

Step 1. [0, 4]

min index = 4

Step 2. swap( $v[i]$ ,  $v[minIndex]$ )

swap( $v[0]$ ,  $v[4]$ )

repeat the steps....

$N=5$

comparison

I.  $i=0$       4

TC:  $O(n^2)$

II.  $i=1$       3

SC:  $O(1)$

III.  $i=2$       2

IV.  $i=3$       1

↓  
outer loop      inner loop  
(n-times       $j=i+1$  to  $n$ )

Insertion Sort

eg: 4 5 X 3 2 1

(left me dekho 4 se bader koi hai)

3 4 5 2 1

↑

3 4 5 2 1

2 3 X 5 X

1 2 3 4 5 ✓

eg: 44 33 55 22 11

33 44 55 22 11

33 44 55 22 11

22 33 44 55 11

11 22 33 44 55 sorted ✓

o

$i=1$ , key =  $v[i] \Rightarrow Key = 4$   
 $j = i-1$

[5 9 3 2 1]  
↓ ↓ ↓ ↓

while ( $j \geq 0$  &  $v[j] > Key$ ) {  
 $v[j+1] = v[j];$

↓      j --;  
 $v[j+1] = Key;$

TC:  $O(n^2)$   
SC:  $O(1)$

$i=2$ , Key = 3  $\Rightarrow$  3 4 5 2 1

$i=3$ , Key = 2  $\Rightarrow$  2 3 4 5 1

$i=4$ , Key = 1  $\Rightarrow$  1 2 3 4 5

Custom Comparator

sort( $v.begin()$ ,  $v.end()$ ); : ↑ order

arr  $\Rightarrow$  sort( $a, a+n$ );

↓ order  $\Rightarrow$  sort( $v.begin()$ ,  $v.end()$ , mycomp);

vector of vector:  $\begin{bmatrix} [1, 44], [0, 55], [0, 22], [0, 11] \\ [2, 33], \dots \end{bmatrix}$

↓ ↓ ↓ ↓

[a, b]

1st  
sort by index of vector  $\Rightarrow$  use comparator.

(by default sort 0<sup>th</sup> index ke basis pe hoga)

## C++ STL Containers [Cont'd]

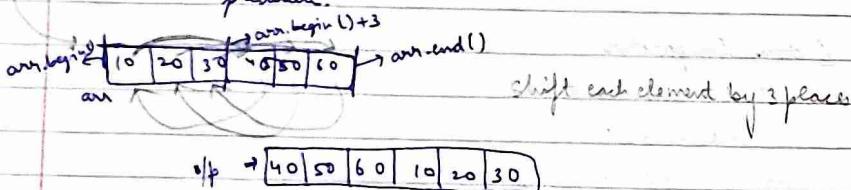
### C++ STL Algorithms

#### Algorithms

The C++ STL includes a wide range of algorithms that operate on various container types and provide essential functionality for data manipulation. These algorithms are defined in the `<algorithm>` header and are part of the STL's core functionality.

#### Iterators and iterating algorithms

- `std::for_each`: applies a function to each element in a range. for  
function
- `std::find`: searches for a specific element in a range. condition in "
- `std::find_if`: " " the first " that satisfies a given predicate. ?
- `std::count`: counts the occurrences of a value in a range.
- `std::count_if`: " " element that satisfy a given predicate.
- `std::sort`: sorts the elements in ascending order.
- `std::reverse`: reverses the order of elements in a range.
- `std::rotate`: rotates elements in a range. rotate
- `std::unique`: removes duplicate elements from a sorted range.
- `std::partition`: divides elements in a range into two groups based on a predicate.

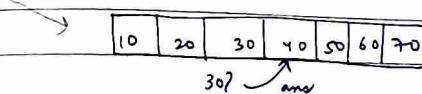
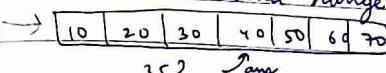


#### Numeric Algorithms

- `std::accumulate`: computes the sum of elements in a range. value jisse initialize karna  
lai wo bhi den loagi
- `std::inner_product`: " " inner product of two ranges. [1, 2], [3, 4, 5]  $\Rightarrow 1 \cdot 3 + 2 \cdot 4 + 5 = 17$
- `std::partial_sum`: " " partial sums of a range. 26
- `std:: iota`: fills a range with incrementing values. iota(1)  $\Rightarrow$  1 second start karte fill krega  
 $\Rightarrow$  iota(1)  $\Rightarrow$  [1, 2, 3, 4]

#### Searching and finding Algorithms

- `std::binary_search`: checks if a value exists in a sorted range! is it present
- `std::lower_bound`: finds the first element greater or equal to a value in a sorted range.
- `std::upper_bound`: finds the first element greater than a value in a sorted range.
- `std::equal_range`: finds a range of elements equal to a value in a sorted range.



#### Min and max algorithm

- `min`: returns smaller of 2 values
- `max`: " " larger " "
- `min_element`: finds smallest element in a range.
- `max_element`: " largest " "

#### Heap Algorithm

- `make_heap`: converts a range into a max-heap  $\rightarrow O(n)$
- `push_heap`: inserts an element into a max-heap  $\rightarrow O(2\log n)$
- `pop_heap`: removes the largest element from a max-heap  $\rightarrow O(n)$
- `sort_heap`: sorts a range that represents a max-heap.

#### Set Algorithm

- `set_union`: computes union of two sorted ranges 1, 2, 3, 4, 5, 6, 7, 8, 9  $\Rightarrow$  1, 2, 3, 4, 5, 6, 7, 8, 9
- `set_intersection`: " intersection 1, 2, 3, 4, 5, 6, 7, 8, 9  $\Rightarrow$  1, 2, 3, 4
- `set_difference`: " difference btw two sorted ranges. 1, 2, 3, 4, 5, 6, 7, 8, 9  $\Rightarrow$  1, 3, 5, 6, 7
- `set_symmetric_difference`: computes symmetric difference of 2 sorted ranges 1, 2, 3, 4, 5, 6, 7, 8, 9  $\Rightarrow$  1, 3, 5, 6, 7

C++ STL: Iterators

- An iterator is a pointer-like object representing an element's position in a container. It is used to iterate over elements in a container.
- Suppose we have a vector named `nums` of size 4. Then, `begin()` and `end()` are member functions() that return iterators pointing to the beginning and end of the vector.
  - `nums.begin()` points to the first element in the vector, i.e  $0^{\text{th}}$  index.
  - `nums.begin() + i` points to the element at  $i^{\text{th}}$  index
  - `nums.end()` points to one element past the final element in vector

Iterating and Traversing Iterators

```
vector<int>::iterator it; (OR) it = arr.begin();
while (it != arr.end()) {
    cout << *it;
    it++;
}
```

Initialise Kodai `arr.begin()`  
`arr.begin()`      `arr.end`  
`( ) [ 10 | 20 | 30 | 40 ]`

Iterator operations

- `*itr` : returns the element at the current position.
- `++itr` : moves iterator to next position. (`itr++` or `itr = itr + 1`)
- `--itr` : " " " " previous".
- `itr + i` : moves " " by  $i$  position.
- `itr1 == itr2` : (comparison) returns true if the pos<sup>n</sup> pointed by iterators are same.
- `itr1 != itr2` : return true if pos<sup>n</sup> pointed by iterators are not same.
- `itr = itr1` : assigns the position pointed by `itr1` to `itr` pointer.
- `itr->m` or `(*itr).m` : returns the member value 'm' of the object pointed by the iterator.



`pair<int, int>` (OR) `(itr).first`  
`p1, p2`      `l, r`  
`(itr).first`      `(itr).second`  
`(itr).second`

Iterator Types (not needed much)

Input Iterator  
 (read only, forward moving)

Output Iterator  
 (write only, forward moving)

Forward Iterator  
 (read/write, forward moving)

Bidirectional Iterator  
 (read/write, forward/backward moving)

Random Access Iterator

(read/write, forward/backward, random access)

Input iterator

- Typically used for algorithms that need to read data from container, such as `std::find` or `std::for_each`.

eg: `istream iterator<int> input_itr (cin)`

Output iterator

- Less used as compared to other iterator types.

eg: `ostream & iterator`

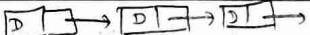
Forward Iterator

- Have combined capabilities of i/p iterator and o/p iterator. For eg: lists support forward iterator.

eg : `forward_list<int> nums = {1, 2, 3, 4};`

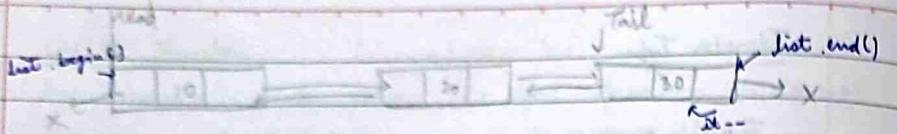
`forward_list<int>::iterator its = nums.begin();`

$\hookrightarrow$  singly linked list

Bidirectional Iterator

- Supported by containers like lists, double-ended queues (deques).

eg : `list<int>::iterator it = nums.begin();`

Random Access Iterator

- Vectors, arrays & deque provide random access iterators.
- eg: `vector<int>::iterator itr-first = vec.begin();`
- eg: `" "`  
`itr.last = vec.end() - 1;`

`random = arr.begin() + i;`Operations supported by iteratorinput : `+, *, -, ==, !=`output : `++, ++*, +=`forward : `++, ++*, -, ==, !=`Bidirectional : `++, --, *, -, ==, !=`Random access : `++, --, *, -, [], +, -, <, <=, >, >=, ==, !=`Why use Iterators?

- saves memory.
- uniform approach: code is more consistent and easier to manage.
- simpler code.
- working with algorithms

C++ STL: Function objects

- Functors are objects that behave like functions and can be called with the same syntax as regular functions. They are implemented as classes or structs that overload the operator().
- In context of C++ STL, functors are often used as custom comparators or custom operations when working with various algorithms and containers.

Usage in algorithms

- Functors are commonly used as arguments to STL algorithms, providing custom behaviour for sorting, searching and other operations.
- For example: when sorting a container of custom objects, you can provide a functor that defines the sorting criteria based on specific object attributes.

Function call operator():

- Functors define the behaviour of their function call operator()
- When a functor functor object is called like a function, the operator() is executed, allowing you to encapsulate custom behaviours within functors.

`eg: bool operator() (Student a, Student b) {`

{}

Custom Comparators

- Functors are frequently used to provide custom comparison logic when sorting or searching in STL containers.
- For example: std::sort algorithm, you can pass a custom functor to specify sorting order.

Advantages of Function

- Provide flexible way to customize behaviour compared to fix pointers.
- type-safe, allowing the compiler to catch type-related errors at compile-time.
- It can carry additional data or state, making them versatile.

Mega Class (line)

2 June 2024

Q1. Solve with precision

$$\sqrt{63} = 7.93725393319$$

(Brute force approach)



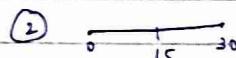
31 is my answer?

Easily find :  $31 \times 31 = 961 \leq 63$

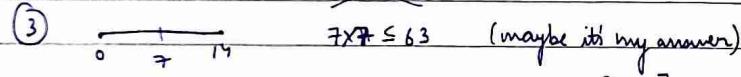
When can I apply search space pattern?

↪ If asked ans find search-space/range we gotta do determine

② mid Ko easily prove fir baaki wo ans hoi ya nahi.

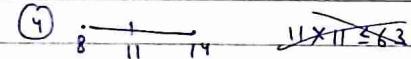


$$15 \times 15 \leq 63$$

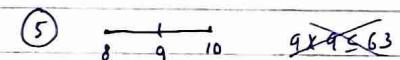


$$7 \times 7 \leq 63 \quad (\text{maybe it's my answer})$$

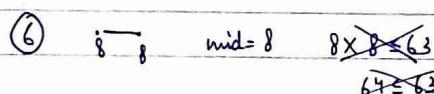
ans = 7



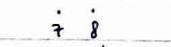
$$11 \times 11 \leq 63$$



$$9 \times 9 \leq 63$$



$TC: O(\log n) + O(\text{precision})$

⑦   
start > end ⇒ stop  
end < start

ans = 7 → 7.9

precision 

store and compute

$$7.0 \rightarrow 49 \leq 63 \checkmark$$

$$7.1 \rightarrow 50.41 \leq 63 \checkmark$$

$$7.2 \rightarrow 51.84 \leq 63 \checkmark$$

$$7.3 \rightarrow 53.29 \leq 63 \checkmark$$

$$7.4 \rightarrow 54.76 \leq 63 \checkmark$$

$$7.5 \rightarrow 56.25 \leq 63 \checkmark$$

$$7.6 \rightarrow 57.76 \leq 63 \checkmark$$

$$7.7 \rightarrow 59.29 \leq 63 \checkmark$$

$$7.8 \rightarrow 60.84 \leq 63 \checkmark$$

$$7.9 \rightarrow 62.41 \leq 63 \checkmark$$

⑦.9 → 1 precision (0.1 step)

$$7.90 \rightarrow 2 \text{ precision } (0.01 \text{ step})$$

$$7.91 \rightarrow 62.56 \leq 63 \checkmark$$

$$7.92 \rightarrow 62.77 \leq 63 \checkmark$$

$$7.93 \rightarrow 62.98 \leq 63 \checkmark$$

$$\rightarrow 63.04 \leq 63 \checkmark$$

step = step / 10

ans = 7.93

3 precision (0.001 step)

$$7.930 \rightarrow 62.88 \leq 63 \checkmark$$

$$7.931 \rightarrow 62.90 \leq 63 \checkmark$$

$$7.932 \rightarrow 62.91 \leq 63 \checkmark$$

$$7.936$$

$$7.9367 \rightarrow 62.99 \leq 63 \checkmark$$

$$7.938$$

$$7.938$$

Method - 2

start ≤ end &  $0 \leq \text{mid} - \text{start}$

while ( $\text{end} - \text{start} \geq 0$ )

↪ Old B.S non-precision cond "⇒ mid: (s+e)/2" { integers (starting se non-precision to the +ve) }

(new method)

while ( $\text{end} - \text{start} \geq 0.1$ ) {

} now consider double values.

(dry run)

TC: Same complexity as Method 1

① 

$$31.5 \times 31.5 = 992.25 \leq 63.0$$

end = mid;

end = mid - 1 ⇒ 0 → 30.5

start = mid;

Q2. Precision Division (Div)

Method 1: BS (non-precision integer) + linear search (precision)

Method 2: fully binary Search

Leetcode 29. Divide 2 integers. (without using \*, /, %)

INT\_MIN → INT\_MAX

$$-2^{31} \quad 2^{31}-1$$

$$-2^{147483648} \quad 2^{147483647}$$

-INT\_MIN  $\Rightarrow$  2147483648  $\Rightarrow$  INT\_MAX se badha hai  
 -1      Lio case to large se handle kro

(Bitwise multiplication : badme Krnge)

(Imp)

Leetcode 875. Koko eating bananas

o N piles      N=4      banana       $\Rightarrow$  h hours (given) : guard  
 $\downarrow$  (eg: 8 hours) gone

3	6	7	11
---	---	---	----

$\uparrow \downarrow \uparrow \downarrow$

banana eaten in 4 hours  
 $\uparrow \downarrow \uparrow \downarrow$  = 2 bananas eaten in 8 hours

$\cancel{K=6}$   $\Rightarrow$  each hour she can eat only K bananas.

$\cancel{K=2, h=8}$

3	6	7	11
1	4	5	9

$\downarrow \downarrow \downarrow \downarrow$  : first 4 hours (8 eaten)

0 2 3 7 : couldn't eat all of bananas.

g:    

3	6	7	11
---	---	---	----

    K=11, h=8  
 hour:  $\cancel{h_1}$   $\downarrow$   $\cancel{h_2}$   $\downarrow$   $\cancel{h_3}$   $\downarrow$   $\cancel{h_4}$

eg: K=7      

3	6	7	11
---	---	---	----

  
 $\downarrow \downarrow \downarrow \downarrow$   $\downarrow$   $\downarrow$

(constraint)  
 o files.length  $\leq$  h

search space:      1 ——— 11

$$K=2^3$$

how many hours koko will take to finish all bananas with K bananas eaten speed per hour?

3	6	7	11
---	---	---	----

$\downarrow \downarrow \downarrow \downarrow$

hours:  $\frac{3}{2}$   $\frac{6}{2}$   $\frac{7}{2}$   $\frac{11}{2}$

hours:  $\frac{3}{2} + \frac{6}{2} + \frac{7}{2} + \frac{11}{2}$

$$\frac{3}{2} = 1.5$$

$$\frac{6}{2} = 3$$

$$\frac{7}{2} = 3.5$$

$$\frac{11}{2} = 5.5$$

$$g: 7 \\ h: 4 \\ w: 1 \\ u: 0$$

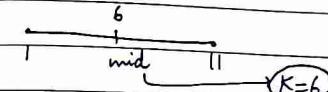
$$\Rightarrow 1 + 2 + \lfloor \frac{3}{2} \rfloor + \lfloor \frac{7}{2} \rfloor \\ \Rightarrow 1 + 2 + 3 + 4 = 10 \text{ hr}$$

$$\left[ 2.5 \rightarrow \lfloor \frac{3}{2} \rfloor \rightarrow 3.0 \right]$$

$$\left[ 2.5 \rightarrow \lfloor \frac{7}{2} \rfloor \rightarrow 4.0 \right]$$

$$\cancel{10 \leq 8}$$

①



$$\text{total hour} = \frac{3}{6} + \frac{6}{6} + \frac{7}{6} + \frac{11}{6} = 1 + 1 + 2 + 2 = 6 \text{ hours}$$

$$6 \leq 8$$

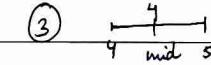
ans = 6  
 ans = 8

To minimise K, move left



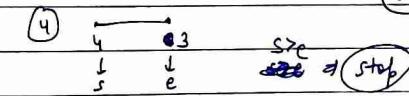
$$K=3 \text{ hours} = 10 \text{ hours}$$

$$\cancel{10 \leq 8}$$



$$K=4; \text{hours} = \frac{3}{4} + \frac{6}{4} + \frac{7}{4} + \frac{11}{4} = 1 + 2 + 2 + 3 = 8 \text{ hours}$$

$$8 \leq 8$$



Recurse  
 TC:  $O(\log(\max(\text{piles})) * O(n))$

TC:  $O(n * \log(\max(\text{piles})))$

Leetcode 1482. Minimum no. of days to Make m Bouquets.

$$[1|0|3|1|0|2] \rightarrow \text{Bloombday}$$

m = 3  
 K=2  
 adjacent

1	10	3	10	2
---	----	---	----	---

 $N=5$ day 1:  $\underline{x \ 9 \ 2 \ 9 \ 1}$  : flowers leftday 2:  $x \ \underline{8} \ 1 \ 8 \ x$ day 3:  $x \ \underline{3} \ x \ \underline{3} \ x$ day 4:  $x \ 6 \ x \ 6 \ x$ day 5:  $x \ 5 \ x \ 5 \ x$ day 6:  $x \ 1 \ x \ 1 \ x$ day 7:  $\underline{x \ x \ x \ \underline{\wedge} \ x}$ ①  $\underline{\text{② bouquet}} \Rightarrow \text{return } -1$  ~~$N=mk \Rightarrow 5 \neq 6$~~ 

7	7	7	7	12	7
---	---	---	---	----	---

 $N=7$ ~~726 ✓~~

bouquet  
 $m=2, K=3$   
 $\downarrow$   
 $mk=6$

7	7	7	7	11	12	7	7
---	---	---	---	----	----	---	---

 $m=2$  $K=3$  $\circlearrowleft$  $826 \checkmark$ 

day 1:

day 7:  $\underline{x \ x \ x \ x \ 4 \ 5 \ x \ x}$ day 11:  $\underline{x \ x \ x \ x \ x \ 1 \ x \ x}$ day 12:  $\underline{x \ x \ x \ x \ x \ x \ x \ x}$ 

↑ search space

monotonic ↑

 $1 \quad 30$ eg:  $K=3, m=4$ day D:  $\underline{x \ x \ x, x \ x \ x \ x \ x \ x}$  $c \leftarrow 1 \ 2 \ 3 \ 0 \ 1 \ 0 \ 0 \ 1 \ 2 \ 0 \ 0 \ 1 \ 2 \ 3$ Counter = 0,  $c=0,$ if ( $c == K$ ) {  $\rightarrow$  bouquet } $c=0;$  $m--;$ 

3

if (non-bloomed) {  $c=0;$  }

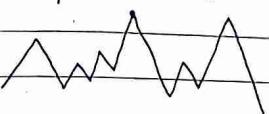
① Search space: days

② monotonic

③ given days: predicate fx

 $\downarrow$   
m: bouqueteg:  $\underline{2 \ 3 \ 4 \ 7 \ 7 \ 7 \ 8 \ 2 \ 1 \ 10 \ 11}$ ①  $\rightarrow$  end = max  $\rightarrow$  element array(start = 1  $\rightarrow$  start  $\neq$  flower\_bloomed)

start = min (array) ✓

lecture 16.2: Find peak element

$\log n + \log m$   
 $N \times \log n \rightarrow \text{Binary search}$

 $\rightarrow$  bottom On  $O(0.1 \log n)$ 

$a[i+1] \leq a[i]$   
 $a[i+1] \geq a[i+2]$   
 $O(n)$

 $\rightarrow$  linear search worse method best nlog n same

Leetcode - (Medium)

## Week-4 Assignments

- ① \* K-diff Pairs in an array

1	4	15
0	3	4

K=2

M-1: Brute force consider each and every pair & take difference

```
for (i=0; i<n; i++) {
```

```
    for (j=i+1; j<n; j++) {
```

```
        if (abs(A[i] - A[j]) == K) { count++; }
```

```
}
```

TC: O(n<sup>2</sup>)

M-2: 2 pointer approach

1	1	3	4	5
0	1	2	3	4

K=2

① diff = A[j] - A[i]

```
if (diff == K) {
```

```
    — i++; j++;
```

```
}
```

```
else if (diff > K) { i++; j++ }
```

```
else { j++; }
```

Dry run: ① 1 | 1 | 3 | 4 |

i j ↗

② diff = 0  $\Rightarrow$  j++ (diff < K)

② 1 | 1 | 3 | 4 | 5

i j

diff = 3 - 1 = 2 ans ✓ ; i++ ; j++

③ diff = 4 - 1 = 3 > K ; i++

④ diff = 4 - 3 = 1 < K ; j++

⑤ diff = 5 - 3 = 2 ; j++ ; i++ ans ✓

Set: to store unique pair.

~~Q-3 : binary search~~

arr: 1 | 1 | 3 | 4 | 5

$\rightarrow k=1$

$a[i]$

$k=2$

$a[i]$

$a[i]$

$a[i] = k$

$a[i] = k$

①  $i=0, a[0]=1, k+a[i]=3$   
search(3)  $\rightarrow$  2nd index  
prior  $\in (1, 3)$

②  $i=1, a[1]=3, k+a[i]=5$   
search(5)  $\rightarrow$  ✓  
prior  $\in (3, 5)$

③  $i=2, a[2]=4, k+a[i]=6$

IC:  $O(\log n)$

TC:  $O(\log n)$

leetcode 658. (medium)

② Find K- closest elements

eg: 

1	2	3	4	5
---	---	---	---	---

$k=4, x=3$

diff: 2 1 0 1 2

$\rightarrow$  close  
 $3 \rightarrow 3, 2, 4, 1, *$

q: 12 | 16 | 22 | 30 | 35 | 39 | 42 | 45 | 48 | 50 | 53 | 55 | 56       $k=4, x=35$

diff: 23 19 15 5 0 4 7 10 13 15 18 20 21

$|x-a[i]|$

M-① sol<sup>n</sup>  $\rightarrow$  sort wrt difference

35 | 39 | 30 | 42 | 45 | 22 | 48 ---

ans

Two pointer      12 | 16 | 22 | 30 | 35 | 39 | 42 | 45 | 48 | 50 | 53 | 55 | 56  
M-② L  $\downarrow$   $\nearrow$  H

$\rightarrow$  jo difference bada hai use age move kro

while(h-l > k){if ( $x - a[l] > a[h] - x$ ) {

TC:  $O(n-k)$

l++; } else { h--; }}

SC:  $O(1)$

}

M-3 ① find smallest element in array which is  $\geq x$ :

lower bound: closest element to x

② H  $\rightarrow$  index of closest element (35)

L  $\rightarrow$  H-1

③ [L, H] window form, size  $\rightarrow k$

$\hookrightarrow$  expand window to k.

if ( $x = arr[0] \geq arr[i] > x$ )  $\{ i++ \}$

else  $\{ i-- \}$

Not 0 index  $\rightarrow i+1$

Not last index  $\rightarrow i-1$

e.g. 3|5|8|10  $\quad k=2, n=15$

$\rightarrow$  binary search +  $arr[i-1] \rightarrow ans=end$

### ③ Exponential Search and unbounded Binary search

- exponential search aka doubling search, application for large array
- gallupping " "
- stack " "

→ sorted

3|4|5|6|11|13|14|15|56|70  $\quad x=13$  (find)

$\rightarrow$  step  $\leftarrow$  if ( $a[0] == x$ ) return 0;

int i=1;

while ( $i < n$  &  $a[i] <= x$ ) {

$i = i * 2;$

}

return BS( $arr, \frac{i}{2}, \min(1, n-1), x$ )

TC:  $O(\log m)$ . while loop

(2) BS on subarray

$$\hookrightarrow 2^4 - 2^3 = 8$$

$$\Rightarrow 2^{\log m} - 2^{\log m - 1}$$

$$= 2^{\log m} (1 - 2^{-1})$$

$$= 2^{\frac{\log m}{2}}$$

$$TC: O(\log (2^{\frac{\log m}{2}}))$$

Application: ① Search in  $\infty$  arrays  
 $\hookrightarrow$  unbounded array

② Better than B.S. ( $x$  is near in beginning)

### ④ unbounded binary

→ find element in an  $\infty$  array (sorted)

(M-1) → use exp search, optimised

(M-2) → brute force

$i=0, \quad$  while( $i < n$ ) { if ( $a[i] > x$ ) break;  
 if ( $a[i] == x == n$ )  $ans = i;$   
 $i++$  }

exp search

X26

1|2|3|4|5|6|7|8|9|10|11  
 0 1 2 3 4 5 6 7 8 9 10  
 $x \quad | \quad | \quad | \quad |$

while ( $a[j] < x$ ) {  $i = j; j = j * 2; }$

algo:  $i = 0; j = 1;$

while ( $a[j] < x$ ) {  $i = j;$   
 $j = j * 2;$   
 }

start =  $i$ ; end =  $j$   
 B.S. ~~for~~ (with value  $x$ )

gfg: hard

### ④ Book Allocation Problem

Simpl

array of books  
 12|34|67|90  $\rightarrow A_i \rightarrow$  no. of page in that book

0 1 2 3

M → no. of students  
 $M=2$

① 12|34|67|90 → max: 90

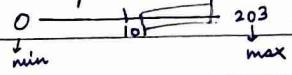
② 12|34|67|90 → max: 157

③ 12|34|67|90 → max: 113

b) if no. of students > no. of books  $\rightarrow$  return -1;

① Brute force

② better soln  $\rightarrow$  define search space  $(12+34+67+90 = 203)$



①  $\rightarrow i=1 \rightarrow$  set  $^m$   
 i=2  $\rightarrow$  "  
 i=113  $\rightarrow$  "  
 "  
 "

$$\text{int mid} = 0 + 203 / 2 = 101$$

Try to allocate each student atmost 101 pages (mid)

$$I \rightarrow 12+34+67=113$$

$$II \rightarrow 67+90=157$$

101 is not a possible soln

c) if (possible soln) {  
 1/minimize pages  
 end = mid - 1;

}

$$I \rightarrow 12+34+67+90=203$$

$$II \rightarrow 90$$

### ⑤ <sup>Inp</sup> Painters Partition Problem

$S | 10 | 30 | 20 | 15 \rightarrow N=5$ ,  $K \rightarrow$  painters  
 $A[i] \rightarrow$  length of  $i^{th}$  board  
1 unit time to paint 1 unit board

$$\text{eg: } N=4, K=2$$

$10 | 20 | 30 | 40$

$$\text{① } 10 | 20 | 30 | 40 \rightarrow \text{Total time together} = 90$$

$$\text{② } 10 | 20 | 30 | 40 \rightarrow 70 \quad \min \rightarrow 60$$

$$\text{③ } 10 | 20 | 30 | 40 \rightarrow 60$$

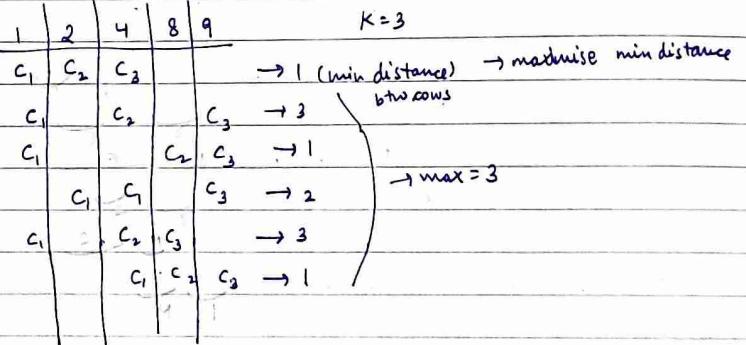
<sup>gives to book allocation problem</sup>

### ⑥ Aggressive Cows

stalls:  $\boxed{1 | 2 | 4 | 8 | 9}$   
(position)  $0 | 1 | 2 | 3 | 4$

$$N=5 \\ K(\text{cows})=3$$

0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 ...



Suppose ans is 1

ans 1  $\rightarrow 1 | 2 | 4 | 8 | 9$

$C_1 | C_2 | C_3$

ans 2  $\rightarrow \underline{\underline{C_1}} | C_2 | C_3$

ans 3  $\rightarrow C_1 | \underline{\underline{C_2}} | C_3$

ans 4  $\rightarrow$  not possible to place 3 cows with min distance 4.

① Binary search  $\checkmark \rightarrow$  search space : min: 0 ; max: maxPos - minPos  $= 9 - 1 = 8$

mid = 4  $\rightarrow$  at least 4 distance for 3 cows place known. not possible

if (not possible) { end = mid - 1; }

②  $0 \rightarrow 3$  ✓ if (possible sol<sup>n</sup>) { start = mid + 1; }

③  $2 \rightarrow 3$  ✓

④  $3 \rightarrow 3$  ✓

⑤ start > end  $\rightarrow$  stop

### ⑦ EKO SPOJ

20 | 15 | 10 | 17

M = 7m

No. of trees = 4



sawblade height = ?

let sawblade height = 15m  $\Rightarrow$  10m wall tree back jayega  $\Rightarrow 5 + 0 + 0 + 2 = 7m$

(M-1)

Brute force

sawblade height = 1m  $\checkmark$  but minimise the sol<sup>n</sup>

sawblade height = 2m  $\checkmark$  " " " "

start = 0 ; end = max heighted tree  
(max wood) (min wood)

(M-2)

binary search

① start = 0 end = 20

$$\text{mid} = 20 + 0 / 2 = 10 \text{ m} \geq 7 \text{ m? } \checkmark$$

if (possible sol<sup>n</sup>) {

ans = mid;

start = mid + 1;

}

②  $\overbrace{\hspace{2cm}}$  20

$$\text{mid} = 15 \checkmark$$

③  $\overbrace{\hspace{2cm}}$  20

$$\text{mid} = 18 X$$

if (not sol<sup>n</sup>) {

end = mid - 1; }

### ⑧ PRATA SPOJ

p  $\rightarrow$  proto  $< 1000$

L cooke  $< 50$

Rank  $\rightarrow [1, 8]$

$C_i \rightarrow$  1st prota 2nd 3rd ... 1000  
Rmine 2R 3R 1000R

M-1 Brute force

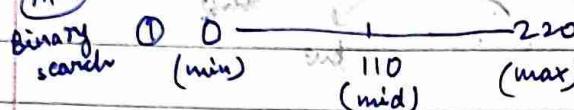
$$NP = 10, 4 cooks, \boxed{1 \ 2 \ 3 \ 4} \rightarrow R$$

for ( $i=0$  min;  $i < \max$ ;  $i++$ )  
}

$$C_4 \rightarrow \text{all } 10 \text{ prata } 1 \times 4 + 2 \times 4 + 3 \times 4 + 4 \times 4 \dots 10 \times 4 \text{ mins}$$

$$\Rightarrow 4[1+2+3+\dots+10] = 4 \left[ \frac{10 \times (0+1)}{2} \right] = 220 \text{ m}$$

M-2



Time taken by cook with highest rank value.  
all prata are given to him  
can cooks cook order of 10 prata in mid = 110 min?

$$C_1 = 55 \text{ min} \leq 110 \checkmark$$

if (possible soln) {

$$\text{ans} = \text{mid}; \text{end} = \text{mid} - 1;$$

}



$$C_1 = 1+2+\dots+9+10 = 55 \text{ min} = 45 \text{ min} \leq 54 \checkmark$$

$$C_2 = 1 \times 2 = 2 \text{ min}$$



$$C_1 = 1+2+\dots+6 = 21 \text{ min} \leq 26$$

$$C_2 = 2+4+6+8 = 20 \text{ min}$$

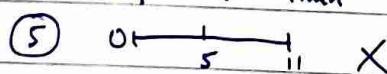


$$C_1 = 1+2+3+4 = 10 \text{ min}$$

$$C_2 = 2+4+6 = 12 \text{ min}$$

$$C_3 = 3+6 = 9 \text{ min}$$

$$C_4 = 4 = 4 \text{ min}$$



$$C_1 = 1+2 = 3 \text{ min}$$

$$C_2 = 2 \text{ min}$$

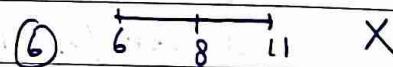
$$C_3 = 3 \text{ min}$$

$$C_4 = 4 \text{ min}$$

if (not Possible) {

$$\text{start} = \text{mid} + 1;$$

}

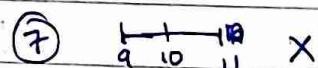


$$C_1 \rightarrow 1+2+3 = 6 \text{ min} \rightarrow 3P$$

$$C_2 \rightarrow 2+4 \rightarrow 2P$$

$$C_3 \rightarrow 3 \rightarrow 1P$$

$$C_4 \rightarrow 4 \rightarrow 1P$$



$$\text{time} = 12$$