

Artificial Intelligence Lab Report



Submitted by

Ayush Aditya(1BM23CS057)

Batch: A3

Course: Artificial Intelligence

Course Code: 23CS5PCAIN

Sem & Section: 5A

**BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING**



B. M. S. COLLEGE OF ENGINEERING

(Autonomous Institution under VTU)

BENGALURU-560019

2025-2026

Table of contents

Program Number	Program Title	Page Number
1	Tic-Tac-Toe	3-10
2	Misplaced tiles – Manhattan distance	11-15
3	8-Puzzle IDDFS	16-20
4	8-Puzzle A*	21-27
5	Vacuum Cleaner	28-32
6	4 queens using hill climbing	33-36
7	4 queens using simulated annealing	37-41
8	Knowledge Base - Propositional Logic	42-47
9	Unification in First Order Logic	48-55
10	Resolution Program	56-60
11	Forward Chaining inference	61-65
12	Alpha Beta Pruning	66-70

Program 1 - Tic Tac toe

Algorithm

Tic Tac Toe - n algorithm

is fullied (arr)

for i in (0, m - 1)

for j in (0, m - 1)

if arr [i] == 0 :

return False

return True

haswon (arr)

$x_1, y_1 = 0, 0$

$x_2, y_2 = 0, 0$

for i in (0, m - 1)

for j in (0, m - 1)

if arr [i][j] == 'x' :

x_1++

elif arr [i][j] == 'o' :

x_2++

if arr [j][i] == 'x' :

y_1++

elif arr [j][i] == 'o' :

y_2++

if $x_1 == 3$ or $y_1 == 3$:

return 'x'

if $x_2 == 3$ or $y_2 == 3$:

return 'y'

for i in range(0, m-1)
 $n_1, n_2 = 0, 0$
 $y_1, y_2 = 0, 0$

if arr[i][i] == 'x':

n_1++

elif arr[i][i] == 'y':
 y_1++

if arr[02-i][2-i] == 'x':

y_1++

elif arr[2-i][2-i] == 'y':
 y_2++

if $n_1 == 3$ or $y_1 == 3$:
 return 'x'

if $n_2 == 3$ or $y_2 == 3$:
 return 'y'

return 'No'

function()

arr = [[0]*3]*3

display to show (arr)

l.m = Input("Enter X or O: ")

Comp i, (1, j) : i = 0, 0, 0, 0

while human(arr) == No and
 l.m filled:

~~l.m = input("Enter your mark")~~

while arr[i][j] != 0:

(j) = Input ("Enter y axis")

arr[i][j] = Tm

if Tm == 'x':

comp = " "

if Tm == 'x':

comp = 'O'

else

comp = 'x'

while arr[i][j] != ' ' and i < 8 and j < 8:

i = random.randint(0, 2)

j = random.randint(0, 2)

arr[i][j] = comp

show(arr)

if haswon(arr) == 'In':

display("Player has won")

if haswon(arr) == 'Comp':

display("Player has lost")

if haswon(arr) == 'No' and isfilled(arr)

display("It was a draw")

show(arr)

for item in arr:

for item1 in item:

if item1 == ' ':

print("-")

Pseudocode :-
Vacuum cleaner
else:
print(item)

Output :

~~0 0 0~~ - - -
~~0 0 0~~ - - -
~~0 0 0~~ - - -

Enter x or 0 : ~~X~~ 0

Enter n ans: 0

Enter y ans: 0

0 - -
- - -
X - -

Enter n ans: 0

Enter y ans: ~~0~~ 1

0 0 -
- X -
X - -

Enter n ans: 0

Enter y ans: 2

0 0 0
- X -
X X -

Tic Tac Toe output:

Enter X or O here : X

— — —
— — —
— — —

Enter m units : 0

x y u : 0

x — 0
— — —
— — —

Enter n units : 1

Enter y u : 1

x — 0
— x —
0 — —

Enter m units : 2

Enter y units : 2

x — 0
— x —
0 - x

Player won.

Code

```
import random

def filled(arr):
    for i in range(len(arr)):
        for j in range(len(arr)):
            if arr[i][j] == 0:
                return False
    return True

def haswon(arr):
    # rows and cols
    for i in range(3):
        if arr[i][0] == arr[i][1] == arr[i][2] != 0: # row
            return arr[i][0]
        if arr[0][i] == arr[1][i] == arr[2][i] != 0: # col
            return arr[0][i]

    # diagonals
    if arr[0][0] == arr[1][1] == arr[2][2] != 0:
        return arr[0][0]
    if arr[0][2] == arr[1][1] == arr[2][0] != 0:
        return arr[0][2]

    return 'No'

def show(arr):
    for row in arr:
        for item in row:
            if item == 0:
                print('_', end=" ")
            else:
                print(item, end=" ")
        print()
```

```

print()

arra = [[0 for _ in range(3)] for _ in range(3)]

In = input("Enter X or 0 here : ").upper()

comp = '0' if In == 'X' else 'X'

show(arra)

while haswon(arra) == 'No' and not filled(arra):

    # Player move

    i = int(input("Enter x axis (0-2): "))

    j = int(input("Enter y axis (0-2): "))

    while arra[i][j] != 0:

        print("Cell already taken, try again.")

        i = int(input("Enter x axis (0-2): "))

        j = int(input("Enter y axis (0-2): "))




arra[i][j] = In

if haswon(arra) != 'No' or filled(arra):

    break

i1, j1 = random.randint(0, 2), random.randint(0, 2)

while arra[i1][j1] != 0:

    i1, j1 = random.randint(0, 2), random.randint(0, 2)

arra[i1][j1] = comp


show(arra)

winner = haswon(arra)

show(arra)

if winner == In:

    print("Player won ")

elif winner == comp:

    print("Player lost ")

else:

    print("It was a draw ")

```

Output Snapshot

```
Enter X or O here : X
- - -
- - -
- - -
Enter x axis (0-2): 0
Enter y axis (0-2): 0
X _ 0
- - -
- - -
Enter x axis (0-2): 1
Enter y axis (0-2): 1
X _ 0
_ X -
0 _ -
Enter x axis (0-2): 2
Enter y axis (0-2): 2
X _ 0
_ X -
0 _ X
Player won
Process finished with exit code 0
```

Program 2 – Misplaced Tiles Manhattan Distance

Algorithm

③

Stop

④

Solve misplaced tiles using
manhattan distance

⑤

Manhattan distance heuristics -

① The number of tiles that are
unplaced

② The distance of each misplaced
tile from where it should be

① Introducing valid moves
 $\text{moves} = [(0, -1), (1, 0), (-1, 0), (0, 1)]$

② Define a function get() that
checks and returns index for
blank tiles

for i = 0 to m:

 for j = 0 to m:

 if A[i][j] == '0':

 return [i, j]

③

Define a function that will
return new iteration of
state

④ new states (state₀) :

for all don, dy

dn, dy ← moves

$$mn, my = x + dn, y + dy$$

state[mn], state[my] = state[my],
state[mn]

④ Use manhattan distance to find out nearness of the current state to the final state

⑤ If the final state is reached return path + [state]

⑥ Else if man

① Do IDDFS iteration of new states and new states to write and do new-state operation on them

⑦ ~~If man define manhattan function as:~~

manhattan (state) :

val = state[i][i] $i \leq 0, j \leq 0$

$$ri = (\frac{val}{3} - 1) // 3$$

$$rj = (val - 1) \% 3$$

$$dist = (i - rri) + (j - rj)$$

return dist

- (B) use manhattan distance & figure out nearness of current state to final state.

~~g = g'~~

- (C) store states and f and g value in min priority heap to figure out the minimum distance state

heap = [(g, f, state)]

- (D) Continue until we reach min depth or final state is reached

8/2

2/9

Code

```
def manhattan(state):
    dist = 0
    for i in range(3):
        for j in range(3):
            val = state[i][j]
            if val != 0:
                target_x = (val-1) // 3
                target_y = (val-1) % 3
                dist += abs(i - target_x) + abs(j - target_y)
    return dist

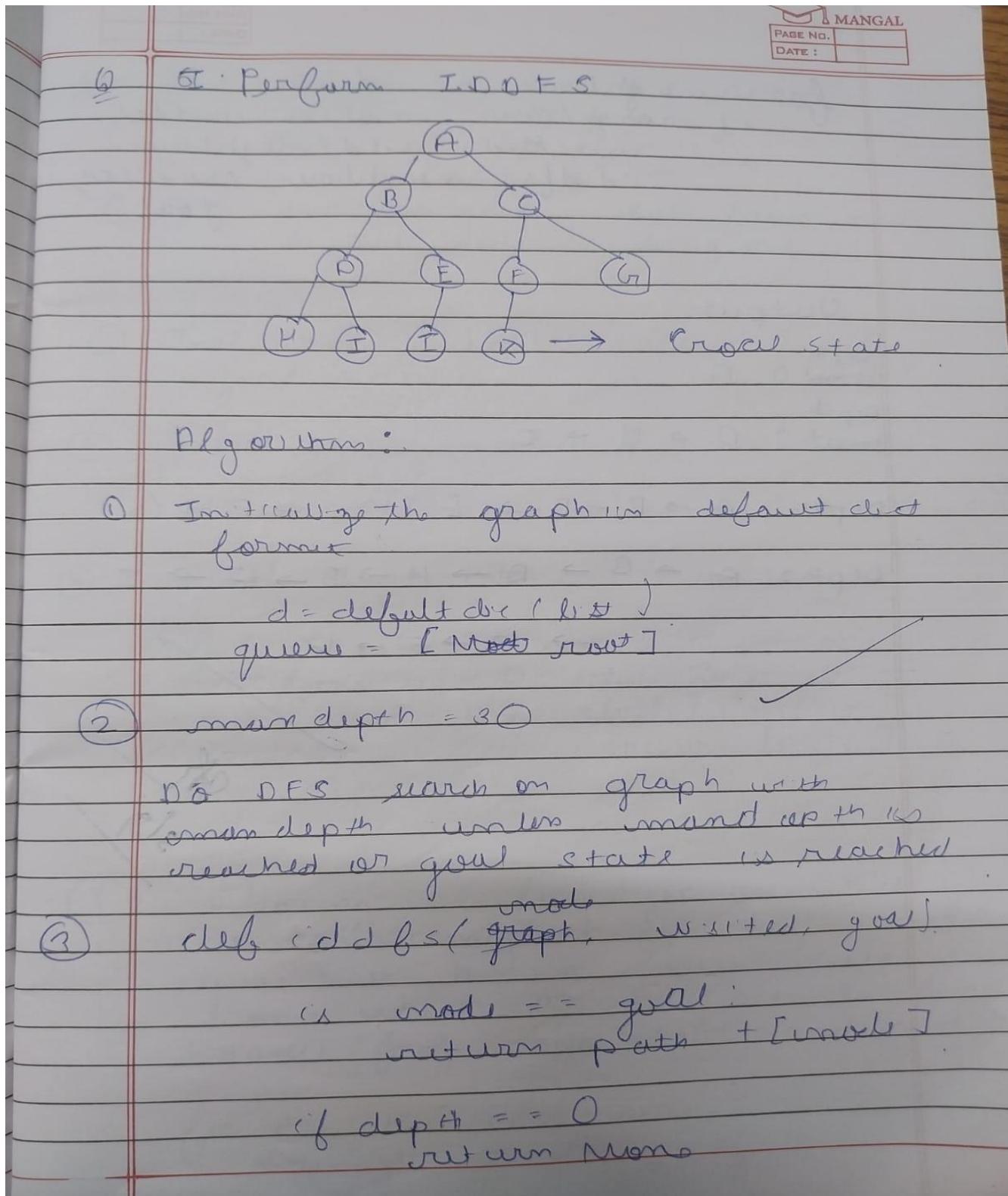
def ida_star(start):
    def search(path, g, bound):
        state = path[-1]
        f = g + manhattan(state)
        if f > bound:
            return f
        if is_goal(state):
            return "FOUND"
        min_threshold = float("inf")
        for neighbor in get_neighbors(state):
            if neighbor not in path:
                path.append(neighbor)
                result = search(path, g+1, bound)
                if result == "FOUND":
                    return "FOUND"
                if result < min_threshold:
                    min_threshold = result
                path.pop()
        return min_threshold
    bound = manhattan(start)
    path = [start]
    while True:
        result = search(path, 0, bound)
        if result == "FOUND":
            return path
        if result == float("inf"):
            return None
        bound = result
```

Output Snapshot

Start State:	Action: right [[8 1 3] [2 0 4] [7 6 5]]
Goal State:	Action: right [[8 1 3] [2 4 0] [7 6 5]]
States Explored: 358	Action: up [[8 1 0] [2 4 3] [7 6 5]]
Solution Path:	Action: left [[8 0 1] [2 4 3] [7 6 5]]
Action: left [[0 1 3] [8 2 4] [7 6 5]]	Action: left [[0 8 1] [2 4 3] [7 6 5]]
Action: down [[8 1 3] [0 2 4] [7 6 5]]	Action: down [[2 8 1] [0 4 3] [7 6 5]]
	Goal Reached Successfully!

Program 3 - 8 puzzle using IDDFS

Algorithm



for neighbour in d :

if neighbour not in visited
visited added (neighbour)
iddfs (neighbours / visited
goal)

Output:

Depth
Level 0: A

Depth
Level 1: A → B → C

Depth 2: A → B → D → E → C → F → G

Depth 3: A → B → D → H → I → L → I

→ C → F → K

8/8

3/9

Code

```
import copy
inp=[[1,2,3],[4,-1,5],[6,7,8]]
out=[[1,2,3],[6,4,5],[-1,7,8]]
def move(temp, movement):
    if movement=="up":
        for i in range(3):
            for j in range(3):
                if(temp[i][j]==-1):
                    if i!=0:
                        temp[i][j]=temp[i-1][j]
                        temp[i-1][j]=-1
    return temp
if movement=="down":
    for i in range(3):
        for j in range(3):
            if(temp[i][j]==-1):
                if i!=2:
                    temp[i][j]=temp[i+1][j]
                    temp[i+1][j]=-1
    return temp
if movement=="left":
    for i in range(3):
        for j in range(3):
            if(temp[i][j]==-1):
                if j!=0:
                    temp[i][j]=temp[i][j-1]
                    temp[i][j-1]=-1
    return temp
if movement=="right":
    for i in range(3):
        for j in range(3):
            if(temp[i][j]==-1):
                if j!=2:
                    temp[i][j]=temp[i][j+1]
                    temp[i][j+1]=-1
    return temp
def ids():
    global inp
    global out
```

```

global flag
for limit in range(100):
    print('LIMIT -> '+str(limit))
    stack=[]
    inpx=[inp,"none"]
    stack.append(inpx)
    level=0
    while(True):
        if len(stack)==0:
            break
        puzzle=stack.pop(0)
        if level<=limit:
            print(str(puzzle[1])+" --> "+str(puzzle[0]))
            if(puzzle[0]==out):
                print("Found")
                print('Path cost=' +str(level))
                flag=True
                return
            else:
                level=level+1
                if(puzzle[1]!="down"):
                    temp=copy.deepcopy(puzzle[0])
                    up=move(temp, "up")


```

```

if(up!=puzzle[0]):
    upx=[up,"up"]
    stack.insert(0, upx)
if(puzzle[1]!="right"):
    temp=copy.deepcopy(puzzle[0])
    left=move(temp, "left")
    if(left!=puzzle[0]):
        leftx=[left,"left"]
        stack.insert(0, leftx)
if(puzzle[1]!="up"):
    temp=copy.deepcopy(puzzle[0])
    down=move(temp, "down")
    if(down!=puzzle[0]):
        downx=[down,"down"]
        stack.insert(0, downx)


```

```

if(puzzle[1]!="left"):
temp=copy.deepcopy(puzzle[0])

```

```
right=move(temp, "right")
if(right!=puzzle[0]):
    rightx=[right,"right"]
    stack.insert(0, rightx)
print('~~~~~ IDS ~~~~~')
ids()
```

Output Snapshot

```
~~~~~ ITERATIVE DEEPENING SEARCH ~~~~~

Trying depth limit: 1

Trying depth limit: 2

Goal Found at depth 2

Solution Path:
[1, 2, 3]
[4, -1, 5]
[6, 7, 8]

[1, 2, 3]
[-1, 4, 5]
[6, 7, 8]

[1, 2, 3]
[6, 4, 5]
[-1, 7, 8]
```

Program 04 - 8 Puzzle Using A*

Algorithm:

①

8 puzzle using A* method

$$f(m) = g(m) + h(m)$$

cost from start cost from mode
to that mode to goal

② Find all possible initial states and goal states

③ Define proper moves

$$\text{Moves} = [(0, -1), (0, 1), (1, 0), (-1, 0)]$$

④ Find blank tiles

```
for i = 0 to 3:  
    for j = 0 to 3:  
        if A[i][j] == 0:  
            return [i, j]
```

⑤

defining a function ~~or~~ which will randomly shuffle tiles and give birth to a new state on which A* will act to find distance from both start and end.

for dx, dy in moves
 $m_x, m_y = n + dx, y + dy$

if $O \leq mn < 3$ and $O = my < 3$.
 $\text{state}[mn][my]$, $\text{state}[m][y] =$

$\text{state}[n][y]$, $\text{state}[mn]$
 return state $[m][y]$.

⑤ Create a heap and push
 initial state onto it.

⑥ heap.push(f , state)

⑦ For every min state
 created using shuffling push
 it on heap alongside $f(m)$.

f , state = heap.push(heap)

if state == "final"
 return f.state + [path]

if state not in inserted:
~~for state in shuffle(state)~~
~~heap.push(heap,~~

~~(f, state)~~
 for state in shuffle(state)
 if state not in inserted:
 $f(m) - g(m) + h(m)$
~~heap.push(heap,~~
~~(f(m), state)~~

⑦ When the final state is reached we have accomplished our goal.

Output -

Initial State

2	1	7
3	4	5
6	-	8

Final State

1	2	3
4	5	6
7	8	-

2	1	7
3	4	5
6	-	8

$$g = 0, h = 9$$

8, 9

h = 7

$$g = 1, f = 8$$

2	-	7
3	1	5
6	1	8

h = 8

g = 2

f = 10

2	1	7
3	4	5
6	8	-

$$h = 6$$

$$g = 3, f = 9$$

$$g = 3, f = 9$$

2	1	7
3	4	5
6	8	-

2	1	7
3	4	5
6	8	-

1	2	3	1	2	5
4	5	6	4	3	6
7	8	—	7	8	—

Final state
Reacher

soft plan

Code

```
def print_b(src):
    state = src.copy()
    state[state.index(-1)] = ''
    print(
f"""
{state[0]} {state[1]} {state[2]}
{state[3]} {state[4]} {state[5]}
{state[6]} {state[7]} {state[8]}
"""
)
def h(state, target):
    count = 0
    i = 0
    for j in state:
        if state[i] != target[i]:
            count = count+1
    return count
def astar(state, target):
    states = [src]
    g = 0
    visited_states = []
    while len(states):
        print(f'Level: {g}')
        moves = []
        for state in states:
            visited_states.append(state)
            print_b(state)
            if state == target:
                print("Success")
                return
            moves += [move for move in possible_moves(
                state, visited_states) if move not in moves]
        costs = [g + h(move, target) for move in moves]
        states = [moves[i]
                  for i in range(len(moves)) if costs[i] == min(costs)]
        g += 1
    print("Fail")
def possible_moves(state, visited_state):
```

```
b = state.index(-1)
d = []
```

```

if b - 3 in range(9):
    d.append('u')
if b not in [0, 3, 6]:
    d.append('l')
if b not in [2, 5, 8]:
    d.append('r')
if b + 3 in range(9):
    d.append('d')
pos_moves = []
for m in d:
    pos_moves.append(gen(state, m, b))
return [move for move in pos_moves if move not in visited_state]
def gen(state, m, b):
    temp = state.copy()
    if m == 'u':
        temp[b - 3], temp[b] = temp[b], temp[b - 3]
    if m == 'l':
        temp[b - 1], temp[b] = temp[b], temp[b - 1]
    if m == 'r':
        temp[b + 1], temp[b] = temp[b], temp[b + 1]
    if m == 'd':
        temp[b + 3], temp[b] = temp[b], temp[b + 3]
    return temp
src = [1, 2, 3, -1, 4, 5, 6, 7, 8]
target = [1, 2, 3, 4, 5, 6, 7, 8, -1]
astar(src, target)

```

Output Snapshot:

```
~~~~~ ITERATIVE DEEPENING SEARCH ~~~~
```

```
Trying depth limit: 1
```

```
Trying depth limit: 2
```

```
Goal Found at depth 2
```

```
Solution Path:
```

```
[1, 2, 3]
```

```
[4, -1, 5]
```

```
[6, 7, 8]
```

```
[1, 2, 3]
```

```
[-1, 4, 5]
```

```
[6, 7, 8]
```

```
[1, 2, 3]
```

```
[6, 4, 5]
```

```
[-1, 7, 8]
```

Program 5 - Vacuum Cleaner

Algorithm



Vacuum cleaner

Algorithm :-

① Repeat step 2 to 3

② Initialize room, quadrant, dirty(0), clean(1)

③ Repeat step 3 to 7 while many quadrant is dirty

④ if quadrant == dirty (0)
quadrant = clean (1)

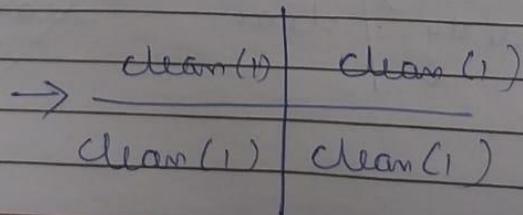
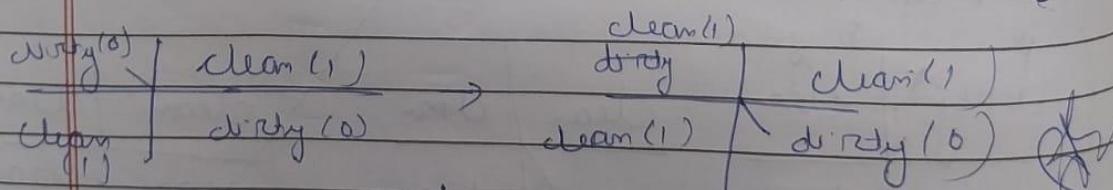
⑤ elif quadrant == 'top-left':
quadrant ← 'top-right'

elif quadrant == 'top-right':
quadrant ← 'bottom-right'

elif quadrant == 'bottom-right':
quadrant ← 'bottom-left'

elif quadrant == 'bottom-left':
quadrant ← top-right

⑥ stop



Vacuum cleaner
output :-

Quadrant 1 has been cleaned.

Current state of the room

$$\begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}$$

Quadrant 2 has been cleaned

Current state of the room

$$\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$$

Quadrant 3 has been cleaned

Current state of the room

$$\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$$

Quadrant 4 has been cleaned

Current state of the room

$$\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$

Final Room State :

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

All quadrants are clean !

Code

```
def vacuum_world():

    goal_state = {'A': '0', 'B': '0'}
    cost = 0

    location_input = input("Enter Location of Vacuum: ")
    status_input = input("Enter status of " + location_input + " : ")
    status_input_complement = input("Enter status of other room : ")
    print("Initial Location Condition {A : " + str(status_input_complement) + ","
    B : " + str(status_input) + " }")
```

23

```
if location_input == 'A':
    print("Vacuum is placed in Location A")
    if status_input == '1':
        print("Location A is Dirty.")
        goal_state['A'] = '0'

        cost += 1 #cost for suck
        print("Cost for CLEANING A " + str(cost))
        print("Location A has been Cleaned.")

    if status_input_complement == '1':
        print("Location B is Dirty.")
        print("Moving right to the Location B. ")
        cost += 1
        print("COST for moving RIGHT " + str(cost))
        goal_state['B'] = '0'
        cost += 1
        print("COST for SUCK " + str(cost))
        print("Location B has been Cleaned. ")

    else:
        print("No action" + str(cost))
        print("Location B is already clean.")

if status_input == '0':
    print("Location A is already clean ")
    if status_input_complement == '1':
        print("Location B is Dirty.")
        print("Moving RIGHT to the Location B. ")
```

```

cost += 1
print("COST for moving RIGHT " + str(cost))
goal_state['B'] = '0'
cost += 1
print("Cost for SUCK" + str(cost))
print("Location B has been Cleaned. ")
else:
    print("No action " + str(cost))
    print(cost)
    print("Location B is already clean.")

```

else:

24

```

print("Vacuum is placed in location B")
if status_input == '1':
    print("Location B is Dirty.")
    goal_state['B'] = '0'
    cost += 1
    print("COST for CLEANING " + str(cost))

```

print("Location B has been Cleaned.")

```

if status_input_complement == '1':
    print("Location A is Dirty.")
    print("Moving LEFT to the Location A. ")
    cost += 1
    print("COST for moving LEFT " + str(cost))
    goal_state['A'] = '0'
    cost += 1
    print("COST for SUCK " + str(cost))
    print("Location A has been Cleaned.")

```

else:

```

    print(cost)
    print("Location B is already clean.")

```

```

if status_input_complement == '1':
    print("Location A is Dirty.")
    print("Moving LEFT to the Location A. ")
    cost += 1
    print("COST for moving LEFT " + str(cost))
    goal_state['A'] = '0'

```

```

cost += 1
print("Cost for SUCK " + str(cost))
print("Location A has been Cleaned. ")
else:
    print("No action " + str(cost))
    print("Location A is already clean.")

print("GOAL STATE: ")
print(goal_state)
print("Performance Measurement: " + str(cost))
vacuum_world()

```

Output Snapshot

```

Enter Location of Vacuum (A/B): A
Enter status of A (1=Dirty, 0=Clean): 1
Enter status of other room (1=Dirty, 0=Clean): 0

Initial Location Condition { A : 1, B : 0 }

Vacuum is placed in Location A
Location A is Dirty. Cleaning A...
COST for SUCK = 1
Location B is already clean.

GOAL STATE: {'A': '0', 'B': '0'}
Performance Measurement (Total Cost): 1

```

Program 6 queens using hill climbing

Algorithm

① 4 Queens problem using hill climbing algorithm

Cost function: Pair of queens attacking each other.

② Initializing the board.

board = [random.randint(0, 3) for _ in range(4)]

③ Define a function that calculates conflicts between queens.

conflicts = 0

for i in range(4):

 for j in range(i+1, 4):

 if board[i] == board[j] or

 (board[i]-board[j])

 == abs(i - j):

 conflicts += 1

④ Producing new neighbours by swapping positions of queens

l = [random.randint(0, 3) for _ in range(4)]

where l[i] = s + i :
l = [random.randint(0, 3) for _ in range(4)]

④ Calculate the conflicts in new state and add it in steps array

conf = calculate - conflicts (board)

steps.appendnd (board, conf))

while True :

m neighbour = calc . merge (b card)

m conf = ~~new~~ calculate - conflicts
(b card)

(D) ∞

steps.append ((neighbour ,
m conf))

if m conf $\emptyset \geq$ conf

continue

~~if conf , steps b card = m conf
neighbour~~

~~if m conf == 0 :~~

~~return steps, board~~

(5) stop

Code

```
import random

def calculate_conflicts(state):
    """Heuristic: number of pairs of queens attacking each other."""
    conflicts = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
                conflicts += 1
    return conflicts

def generate_neighbors(state):
    """Generate all neighbor states by moving one queen in its column."""
    neighbors = []
    n = len(state)
    for col in range(n):
        for row in range(n):
            if state[col] != row:
                new_state = state.copy()
                new_state[col] = row
                neighbors.append(new_state)
    return neighbors

def hill_climbing(n=4):
    # Initial random state
    state = [random.randint(0, n - 1) for _ in range(n)]
    current_cost = calculate_conflicts(state)

    steps = []
    steps.append((state.copy(), current_cost))

    while True:
        neighbors = generate_neighbors(state)
        best_neighbor = min(neighbors, key=calculate_conflicts)
        best_cost = calculate_conflicts(best_neighbor)

        steps.append((best_neighbor.copy(), best_cost))
```

```
if best_cost >= current_cost: # Local optimum
    break
state, current_cost = best_neighbor, best_cost

return state, current_cost, steps

# Run for 4-Queens
solution, cost, steps = hill_climbing(4)

print("Final State:", solution)
print("Final Cost:", cost)
print("\nSteps (state, cost):")
for s, c in steps:
    print(s, "Cost:", c)
```

Output Snapshot

```
Final State: [1, 2, 0, 3]
Final Cost: 1

Steps (state, cost):
[2, 2, 0, 0] Cost: 4
[2, 2, 0, 3] Cost: 2
[1, 2, 0, 3] Cost: 1
[1, 3, 0, 3] Cost: 1

Process finished with exit code 0
```

Program-07 4 queens using simulated annealing

Algorithm

~~Q~~ n Queens using Simulated Annealing

① Define a board:

board = [random.randint(0, 3)
for _ in range(4)]

② calculate conflicts

calc_conflicts(board):

conflicts = 0

for i in range(4):

 for j in range(i+1, 4):

 if board[i] == board[j]
 or abs(i - j) == abs(board[i] - board[j])

 conflicts += 1

return conflicts

③ Generate New Neighbours

new -

calc_neigh(board):

l = [random.randint(0, 3)

for _ in range(4)]

while l != board:

 l = [random.randint(0, 3)]
 for _ in range(4):

④ regenerate new states and
replace existing state if it
has less $\Delta E > 0$ or
 $P \leq e^{-\Delta E/T}$

• conf = calc_conflict(boards)

$$T = 1000$$

$$\text{steps} = 17$$

steps.append((board, conf))

~~while~~

$$\text{step done closer} = 0.99$$

~~steps.append~~

while $T > 0$

unigh = calc_mergh(board)

mconf = calc_conflicts(unigh)

$\Delta E = (\text{conf} - \text{unigh})$

steps.append((unigh, mconf))

if $\Delta E > 0$ or random
random() <
math.exp($\Delta E / T$)

conf = unigh
board = unigh

if $\text{rcnf} == 0$;
return steps, board

$$T^* = \text{step_down}$$

Output →

board = [0, 1, 2, 3],
conflicts = 6.

board = [0, 2, 1, 3],
conflicts = 1

$$\Delta E = \Delta E = 6 - 1 = 5$$

$$\Delta E > 0$$

$$\text{conflicts} = 1$$

board = [0, 1, 3, 1] \Rightarrow , conflicts = 3

$$\Delta E = 1 - 3 = -2$$

$\Delta E < 0 \Rightarrow$ No swap

∴ board = [0, 2, 4, 1], conflicts = 0

$$\Delta E = 1 - 0 = 0$$

$$\therefore \text{mconf} = 0$$

Code

```
import random
```

```
import math
```

```
# Define the size of the board (4x4)
```

```
N = 4
```

```
# Generate a random state (a random arrangement of queens on the board)
```

```
def random_state():
```

```
    return [random.randint(0, N - 1) for _ in range(N)]
```

```
# Calculate the number of conflicts (attacking pairs of queens)
```

```
def calculate_conflicts(state):
```

```
    conflicts = 0
```

```
    for i in range(N):
```

```
        for j in range(i + 1, N):
```

```
            if state[i] == state[j]: # Same column
```

```
                conflicts += 1
```

```
            if abs(state[i] - state[j]) == abs(i - j): # Same diagonal
```

```
                conflicts += 1
```

```
    return conflicts
```

```
# Perform a random move (a small change to the state)
```

```
def random_move(state):
```

```
    new_state = state[:]
```

```
    row = random.randint(0, N - 1)
```

```
    new_state[row] = random.randint(0, N - 1)
```

```
    return new_state
```

```
# Simulated Annealing algorithm
```

```
def simulated_annealing():
```

```
    current_state = random_state()
```

```
    current_temp = 1000 # Initial temperature
```

```
    min_temp = 1 # Minimum temperature to stop
```

```
    cooling_rate = 0.95 # Rate at which the temperature decreases
```

```
# Loop until the temperature is low enough
```

```
while current_temp > min_temp:
```

```
    # Calculate the current number of conflicts
```

```
    current_conflicts = calculate_conflicts(current_state)
```

```

# If no conflicts, we've found a solution
if current_conflicts == 0:
    return current_state

# Generate a new candidate by making a random move
new_state = random_move(current_state)
new_conflicts = calculate_conflicts(new_state)

# If the new state is better or if we accept it probabilistically
if new_conflicts < current_conflicts or random.random() < math.exp(
    (current_conflicts - new_conflicts) / current_temp):
    current_state = new_state

# Cool down the temperature
current_temp *= cooling_rate

# Return the best state found
return current_state

```

```

# Run the simulated annealing algorithm
solution = simulated_annealing()

# Display the solution
print("Solution: ", solution)
print("Conflicts: ", calculate_conflicts(solution))

```

OUTPUT

```

Solution: [1, 3, 0, 2]
Conflicts: 0

Process finished with exit code 0
|
```

Program-08 Knowledge Base -Propositional Logic

Algorithm

Q Create a KB using propositional logic, and show that the given query ends with the KB or not
pseudo code:

① construct a dictionary to store values and variables

{'P': True, 'Q': False, 'R': True}

② create a list containing the operations

L = ['n', 'v']

③ do the operation

if op == '
for i in range(m):

operator(n, y, op):

if op == 'n':

return n and y

elif op == 'v':

return m or y

elif op == '¬':

return not y

elif op == '⇒':

return xor(n, y)

```

else:
    if n <= mdy:
        return True
    elif n > mdy:
        return False
    else:
        return True

```

①

Operate on the variables
~~ans~~ = ~~True~~ True

for i in range (~~(0,)~~ 1, m):

~~ans~~ = ans and operate(d[i], d[i], L[i]).

Inference:

Endowment

VB | L

VB | L is true if L is true
 every single ~~model~~ model in
 which VB is true.

For . by

if n > 0 & then m > 0
 (K) (n)

(Q) Considering a KB that contains the following propositional logic sentences.

$$\begin{array}{l} Q \rightarrow P \\ P \rightarrow \neg \neg Q \end{array}$$

$$Q \vee R \rightarrow \text{KB}$$

i) Construct truth table and show value of each sentence in KB and find out models in which the KB is true.

ii) Does KB entail $P \rightarrow R$?

iii) Does KB entail $R \rightarrow P$?

iv) Does KB entail $\neg Q \rightarrow R$?

~~Truth Table~~

Truth Table

P	Q	R	$Q \rightarrow P$	$P \rightarrow \neg Q$	$Q \vee R$	$Q \rightarrow R$
F	F	F	T	T	F	FT
F	F	T	T	T	T	FT
F	T	F	F	T	T	F
T	T	F	T	F	T	F
F	T	T	F	T	T	FT
T	F	F	T	T	F	TT
T	F	T	T	T	T	TT
T	T	T	T	F	T	TT

	$R \rightarrow P$
	T
	F
	T
	T
	F
	T
	T
	T
	F

(ii) Even though R is true, $K \cdot B$ is also true, $K \cdot B$ does not necessarily entail R

(iii) Since $R \rightarrow P$ is not always true when $K \cdot B$ is true

$$K \cdot S \nmid R \rightarrow P$$

(iv) Since $Q \rightarrow R$ is true always when $K \cdot B$ is true

$$K \cdot B \models Q \rightarrow R$$

soft
relations

Code

```
import itertools

# Evaluate a propositional logic sentence in a given model (dictionary of symbol →
# True/False)
def pl_true(expr, model):
    if isinstance(expr, str): # atomic symbol
        return model[expr]
    op = expr[0]
    if op == 'not':
        return not pl_true(expr[1], model)
    elif op == 'and':
        return pl_true(expr[1], model) and pl_true(expr[2], model)
    elif op == 'or':
        return pl_true(expr[1], model) or pl_true(expr[2], model)
    elif op == 'implies':
        return (not pl_true(expr[1], model)) or pl_true(expr[2], model)
    elif op == 'iff':
        return pl_true(expr[1], model) == pl_true(expr[2], model)
    else:
        raise ValueError("Unknown operator: " + op)

# The truth table enumeration function
def tt_entails(kb, query, symbols):
    for values in itertools.product([True, False], repeat=len(symbols)):
        model = dict(zip(symbols, values))
        if pl_true(kb, model):
            if not pl_true(query, model):
                return False # Found a counterexample
    return True

# Example Knowledge Base and Query
# Example:  $(P \wedge Q) \rightarrow R$ , and  $(P \wedge Q)$  is true, does  $R$  follow?

symbols = ['P', 'Q', 'R']

# Knowledge Base:  $(P \wedge Q) \rightarrow R$ 
kb = ('implies', ('and', 'P', 'Q'), 'R')
```

```
# Query: R
query = 'R'

# Check entailment
result = tt_entails(kb, query, symbols)

print("Does KB entail Query? →", result)
```

Output Snapshot

```
Does KB entail Query? → False

Process finished with exit code 0
```

Program-09 Unification in first order logic

Algorithm

Unification Algo.

DATE : _____

if Ψ_1 or Ψ_2 is a variable or const and

① if Ψ_1 or Ψ_2 is identical
return NIL

② if Ψ_1 is a variable:

if Ψ_1 in Ψ_2 :

return Failure

else

return $\{\{\Psi_2 / \Psi_1\}\}$

③ if Ψ_2 is a variable:

if Ψ_2 in Ψ_1 :

return Failure

else:

return $\{\{\Psi_1 / \Psi_2\}\}$

④ else

return Failure

⑤ if Ψ_1 or Ψ_2 have different predicate return Failure

⑥ if Ψ_1 and Ψ_2 have different number of variables:

return Failure

⑦ set $Pset(SUBST) = NIL$

⑧ for $i = 1$ to number of variables
in Ψ_1 :

call unify on i^{th} variable of
 P_1 with i^{th} variable of
 P_2 .

if $S = \text{Failure}$, return Failure.

~~if $S \neq \text{NIL}$~~

if $S \neq \text{NIL}$:

Apply S on remaining 21 or 22

$\text{SUBS} = \text{append}(S, \text{SUBS})$

return SUBS

Eg.

$$\textcircled{1} \quad \text{BEATS}(n, f(x)) \neq \text{EATS}(n, y)$$

Different pred. rates: Failure.

$$\textcircled{2} \quad \text{EATS}(n, y, z) \neq \text{EATS}(n, y)$$

Different number of variables
Failure.

$$\textcircled{3} \quad \text{EATS}(n, f(x), f(x)) \neq \text{EATS}(n, g(b), g(b))$$

~~subs { }.~~

$\emptyset = \text{subs}\{x/g(b)\}$
 \emptyset is the universal unifier

$$\textcircled{1} \quad P(z/y), g(y), \varphi(y)$$

$$P(\varphi(g(z)), g(\varphi(0)), \varphi(0))$$

Find $\theta(M_{60})$

$$\theta_1 = \text{subs}\{n/g(z)\}$$

$$P(\varphi(g(z)), g(y), y)$$

$$+ P(\varphi(g(z)), g(\varphi(0)), \varphi(0))$$

$$\theta_2 = \text{subs}\{y/\varphi(y)\}$$

$$\theta_3 = \text{subs}\{y/a\}$$

$$P(\varphi(g(z)), g(\varphi(0)), \varphi(a))$$

$$= P(\varphi(g(z)), g(\varphi(0)), \varphi(a))$$

θ_1, θ_2 and θ_3 are most general

~~Q (x, f(y), g(y))~~

→ Failure since they both have different pre

→ Failure since they both have different pre

② ~~H (n, g (n)),~~

~~H (g (y), g (g (z)))~~

② ~~G (n, f (n)), G (f (y), f (y))~~

Failure since the same variable in same variable appears in different position

③ ~~H (n, g (n))~~

~~H (g (y), g (g (z)))~~

∅, = subs (n / g (g))

~~H (g (z), g (g (z))) and~~

~~H (g (y), g (g (y)))~~

$\phi_2 = \text{subs}(y/z)$

$u(g(z)), g(g(z))$ and

$u(g(z)), g(g(z))$

ϕ_1 and ϕ_2 are $\cap G \cup$

② $q(u, f(y)), \phi(f(y), y)$

$\phi_1 = \text{subs}(u/y)$.

$\phi_2 = \text{subs}(f(y)/y)$

Since g_n want it be used $f(y)$ and
 y at the same time the unfication
 union is a failure

Code

```
import re

def getAttributes(expression):
    inside = expression[expression.index("(")+1 : expression.rindex(")")]
    return inside.split(",")

def getInitialPredicate(expression):
    return expression.split("(")[0]

def isConstant(x):
    return len(x) == 1 and x.isupper()

def isVariable(x):
    return len(x) == 1 and x.islower()

def replaceAttributes(exp, old, new):
    predicate = getInitialPredicate(exp)
    attributes = getAttributes(exp)
    attributes = [new if x == old else x for x in attributes]
    return f'{predicate}({",".join(attributes)})'

def apply(exp, substitutions):
    for (new, old) in substitutions:
        exp = replaceAttributes(exp, old, new)
    return exp

def checkOccurs(var, exp):
    return var in exp

def getFirstPart(expression):
    return getAttributes(expression)[0]

def getRemainingPart(expression):
    predicate = getInitialPredicate(expression)
    attributes = getAttributes(expression)[1:]
    return f'{predicate}({",".join(attributes)})'

def unify(exp1, exp2):
    # Rule 1: identical
    if exp1 == exp2:
        return []

    # Rule 2: constants
    if isConstant(exp1) and isConstant(exp2):
        if exp1 != exp2:
            print(f'{exp1} and {exp2} are different constants → FAIL')
        return []

    # Rule 3: variables
    if isVariable(exp1) and isVariable(exp2):
        if exp1 == exp2:
            return []
        else:
            print(f'{exp1} and {exp2} are different variables → FAIL')
            return []

    # Rule 4: predicates
    if len(exp1) > len(exp2):
        if exp1[:len(exp2)] == exp2:
            return [exp1[len(exp2):]]
        else:
            print(f'{exp1} and {exp2} are different predicates → FAIL')
            return []
    else:
        if exp2[:len(exp1)] == exp1:
            return [exp2[len(exp1):]]
        else:
            print(f'{exp1} and {exp2} are different predicates → FAIL')
            return []
```

```

return []

# Rule 3: variable cases
if isVariable(exp1):
    return [(exp2, exp1)] if not checkOccurs(exp1, exp2) else []

if isVariable(exp2):
    return [(exp1, exp2)] if not checkOccurs(exp2, exp1) else []

# Rule 4: predicates must match
if getInitialPredicate(exp1) != getInitialPredicate(exp2):
    print("Predicates do not match → FAIL")
    return []

args1 = getArguments(exp1)
args2 = getArguments(exp2)

if len(args1) != len(args2):
    print("Argument lengths do not match → FAIL")
    return []

# Recursive unification
head1 = args1[0]
head2 = args2[0]

s1 = unify(head1, head2)
if s1 == [] and head1 != head2:
    return []

if len(args1) == 1:
    return s1

t1 = apply(getRemainingPart(exp1), s1)
t2 = apply(getRemainingPart(exp2), s1)

s2 = unify(t1, t2)
if s2 == [] and t1 != t2:
    return []

return s1 + s2

if __name__ == "__main__":
    print("\n==== UNIFICATION PROGRAM (FIXED) ====")
    e1 = input("Enter first expression: ").strip()
    e2 = input("Enter second expression: ").strip()

    substitutions = unify(e1, e2)

    print("\nRESULT SUBSTITUTIONS:")
    if substitutions:
        print([f"{var}/{val}" for (val, var) in substitutions])

```

```
else:  
    print("UNIFICATION FAILED")
```

Output Snapshot

```
==== UNIFICATION PROGRAM (FIXED) ====  
Enter first expression: P(x,y)  
Enter second expression: P(a,b)  
  
RESULT SUBSTITUTIONS:  
[ 'x/a' , 'y/b' ]
```

Program-10 Resolution Program

Algorithm:

First Order Logic - Resolution.

Resolution works by building refutations proofs, proofs by contradiction.

Algorithm :-

(1) Convert all sentences to CNF

(i) Eliminate biconditionals and implication

$$S \Rightarrow B \text{ becomes } (S \Rightarrow B) \wedge (B \Rightarrow C)$$

$$S \Rightarrow B \text{ becomes } \neg S \vee B$$

(ii) Now \neg wards :

- $\neg (\forall x p) \equiv \exists x \neg p$
- $\neg (\exists x p) \equiv \forall x \neg p$

(iii) Standardizing variables by renaming them, we define variable for each quantifier

(iv) Skolemizing : Each existential variable is replaced by skolem constant or skolem function of universally quantified variables

(V) prop universal quantifiers.

$\forall n \text{ Person}(n)$ becomes $\text{Person}(n)$

(VI) distribute \forall over \vee :

$$\cdot (\ell \wedge B) \vee Y = (\ell \vee Y) \wedge (B \vee Y)$$

(1) Negate conclusion S and convert result to CNF

(2) Add Negated conclusion S to The premise clauses

(3) repeat steps ① to ② until contradiction or no progress is made:

i) select any 2 clauses

ii) resolve them

iii) if empty clause is result, contradiction has been found

(4) also add the resultant to the premises

(5) If step ④ succeeds, conclusion has been proved

Killed (Pmt)

→ alive (v)

V → killed (k)

{ Pmt & k }

→ alive (Pmt)

alive (Pmt)

{ } Home pruned

Code

from itertools import combinations

```
# Utility: negate a literal
def negate(literal):
    if literal.startswith('~'):
        return literal[1:]
    else:
        return '~' + literal

# Apply resolution on two clauses
def resolve(ci, cj):
    resolvents = set()
    for di in ci:
        for dj in cj:
            if di == negate(dj):
                new_clause = (ci - {di}) | (cj - {dj})
                resolvents.add(frozenset(new_clause))
    return resolvents

def fol_resolution(KB, query):
    clauses = set(KB)
    clauses.add(frozenset([negate(query)])) # add negation of query

    new = set()
    while True:
        pairs = list(combinations(clauses, 2))
        for (ci, cj) in pairs:
            resolvents = resolve(ci, cj)
            if frozenset() in resolvents:
                return True # empty clause found → proved
            new = new.union(resolvents)

        if new.issubset(clauses):
            return False # no new clauses → cannot prove
        clauses = clauses.union(new)

# -----
# Knowledge Base in CNF
# -----
KB = [
    frozenset(['~Food(x)', 'Likes(John,x)']), # John likes all food
    frozenset(['Food(Apple)']),
    frozenset(['Food(Vegetables)']),
    frozenset(['~Eats(x,y)', 'Killed(x)', 'Food(y)']),
```

```
frozensest(['Eats(Anil,Peanuts)'),  
frozensest(['Alive(Anil)'),  
frozensest(['~Eats(Anil,x)', 'Eats(Harry,x)'),  
frozensest(['~Alive(x)', '~Killed(x)'),  
frozensest(['Killed(x)', 'Alive(x)'])  
]
```

```
query = 'Likes(John,Peanuts)'
```

```
# Run the resolution  
if fol_resolution(KB, query):  
    print("Proved:", query)  
else:  
    print("Invalid — cannot be proved")
```

OutputSnapshot

```
Invalid – cannot be proved
```

Program 11: Forward Chaining inference

MANGAL
PAGE NO. _____
DATE : _____

Q

Forward

Return on my chaining

KB : Knowledge Base

S : Atom or Sentence

new = S

repeat until new is empty :

for rule in KB :

$(p_1 \wedge p_2 \wedge \dots \Rightarrow q) = \text{standardized}$
 variable (rule)

for each \emptyset such that subs(\emptyset ,

$p_1' \wedge p_2' \wedge p_3' \dots \wedge p_r'$) :-

$\text{subs}(\emptyset, p_1' \wedge p_2' \wedge p_3' \dots \wedge p_r')$

for $p_1' \wedge p_2' \wedge p_3' \dots \wedge p_r'$ in KB :

$q' \leftarrow \text{subs}(\emptyset, p)$

If q' does not unify with
some sentence in KB or
new :

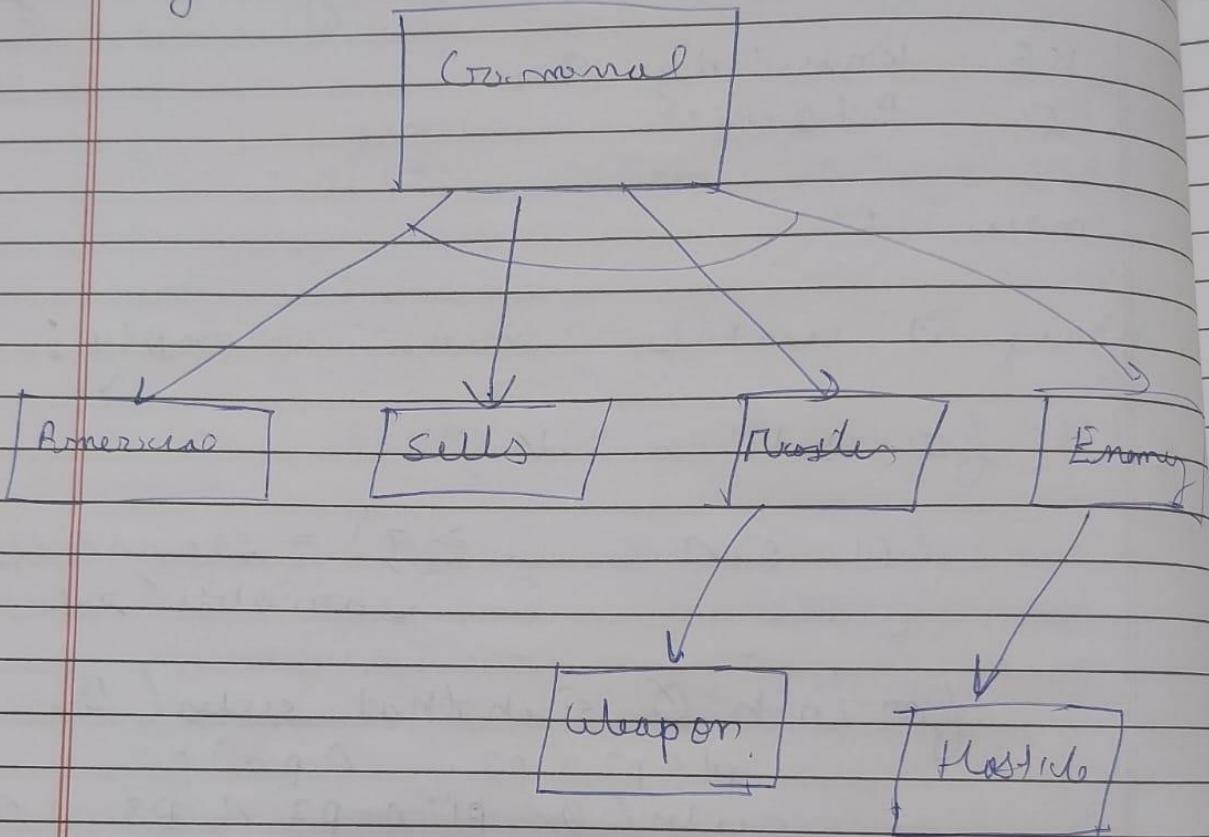
Add q' to new

$\emptyset \leftarrow \text{unify}(q', \emptyset)$

If \emptyset is not failure
return \emptyset

return false

Eg : -



Code-

```
# Forward Chaining in First-Order Logic (FOL)
# Example: Prove "Criminal(Robert)"

# Knowledge Base (KB)
KB = [
    # Rule 1: It is a crime for an American to sell weapons to hostile nations
    {"if": ["American(p)", "Weapon(q)", "Sells(p, q, r)", "Hostile(r)"], "then": "Criminal(p)"},

    # Rule 2: Country A owns some missiles (T1)
    {"fact": "Owns(A, T1)"},

    # Rule 3: Missiles are weapons
    {"if": ["Missile(x)"], "then": "Weapon(x)"},

    # Rule 4: All missiles owned by A were sold by Robert
    {"if": ["Missile(x)", "Owns(A, x)"], "then": "Sells(Robert, x, A)"},

    # Rule 5: Enemies of America are hostile
    {"if": ["Enemy(x, America)"], "then": "Hostile(x)"},

    # Rule 6: Robert is an American
    {"fact": "American(Robert)"},

    # Rule 7: Country A is an enemy of America
    {"fact": "Enemy(A, America)"}
]

# Function to extract all current known facts
def get_facts(kb):
    return {rule["fact"] for rule in kb if "fact" in rule}

# Function to perform variable substitution
def substitute(expr, var, val):
    return expr.replace(f"{{var}}", f"{{val}}").replace(f"{{var}}",
f"{{val}}").replace(f"{{var}}", f"{{val}}")

# Forward chaining algorithm
```

```

def forward_chain(kb, query):
    inferred = set()
    facts = get_facts(kb)
    new_inference = True

    print("Initial Facts:", facts)
    print("Goal:", query)
    print("\n--- Forward Chaining Process ---")
    while new_inference:
        new_inference = False
        for rule in kb:
            if "if" in rule:
                conditions = rule["if"]
                result = rule["then"]

                # Check if all conditions are satisfied
                satisfied = True
                temp_result = result
                substitution = { }

                for cond in conditions:
                    matched = False
                    for fact in facts:
                        if cond.split("(")[0] == fact.split("(")[0]:
                            # Try variable substitution
                            c_args = cond[cond.find("(") + 1:-1].split(",")
                            f_args = fact[fact.find("(") + 1:-1].split(",")

                            if len(c_args) == len(f_args):
                                for i in range(len(c_args)):
                                    if c_args[i].islower():
                                        substitution[c_args[i]] = f_args[i]
                                    elif c_args[i] != f_args[i]:
                                        break
                                else:
                                    matched = True
                                    break
                            if not matched:
                                satisfied = False
                                break
                if satisfied:
                    new_inference = True
                    temp_result = result
                    for cond in conditions:
                        if cond in substitution:
                            result = result.replace(cond, substitution[cond])
                    kb.append(result)

```

```

break

if satisfied:
    for var, val in substitution.items():
        temp_result = substitute(temp_result, var, val)

    if temp_result not in facts:
        facts.add(temp_result)
        inferred.add(temp_result)
        new_inference = True
        print(f"Inferred: {temp_result}")

    if temp_result == query:
        print("\n✓ Goal Reached!")
        return True

print("\n✗ Goal Not Reached.")
return False

# Main Execution
if __name__ == "__main__":
    query = "Criminal(Robert)"
    result = forward_chain(KB, query)
    print("\nFinal Result:", "Robert is a Criminal" if result else "Cannot prove Robert is Criminal")

```

Output-

```

Initial Facts: {'Missile(T1)', 'Owns(A, T1)', 'Enemy(A, America)', 'American(Robert)'}

Goal: Criminal(Robert)

--- Forward Chaining Process ---
Inferred: Weapon(T1)
Inferred: Sells(Robert, T1, A)
Inferred: Hostile(A)
Inferred: Criminal(Robert)

✓ Goal Reached!

Final Result: Robert is a Criminal

```

Program 12 :Alpha Beta Pruning

Algorithm-

DATE :

Alpha - Beta Search Algorithm

Alpha

① Alpha-beta - Algo (state) :

$v \leftarrow \text{Min-value} (\text{state}, -\infty, +\infty)$

return action in Actions (state)
with value v,

Min - Value (state, α , β)

if : terminal (state)
return utility (state)

$v \leftarrow -\infty$

for a in Actions (state) do :

$v \leftarrow \text{Max} (v, \text{Min-value} (\text{Results} (s, a), \alpha, \beta))$

if $v \geq \beta$ then return v

$\alpha \leftarrow \text{MAX} (\alpha, v)$

return v

~~further~~

numValue (s + ai, f, B)

if terminal (state):

return utility (state).

v ← +∞

for a in Actions (state) do:

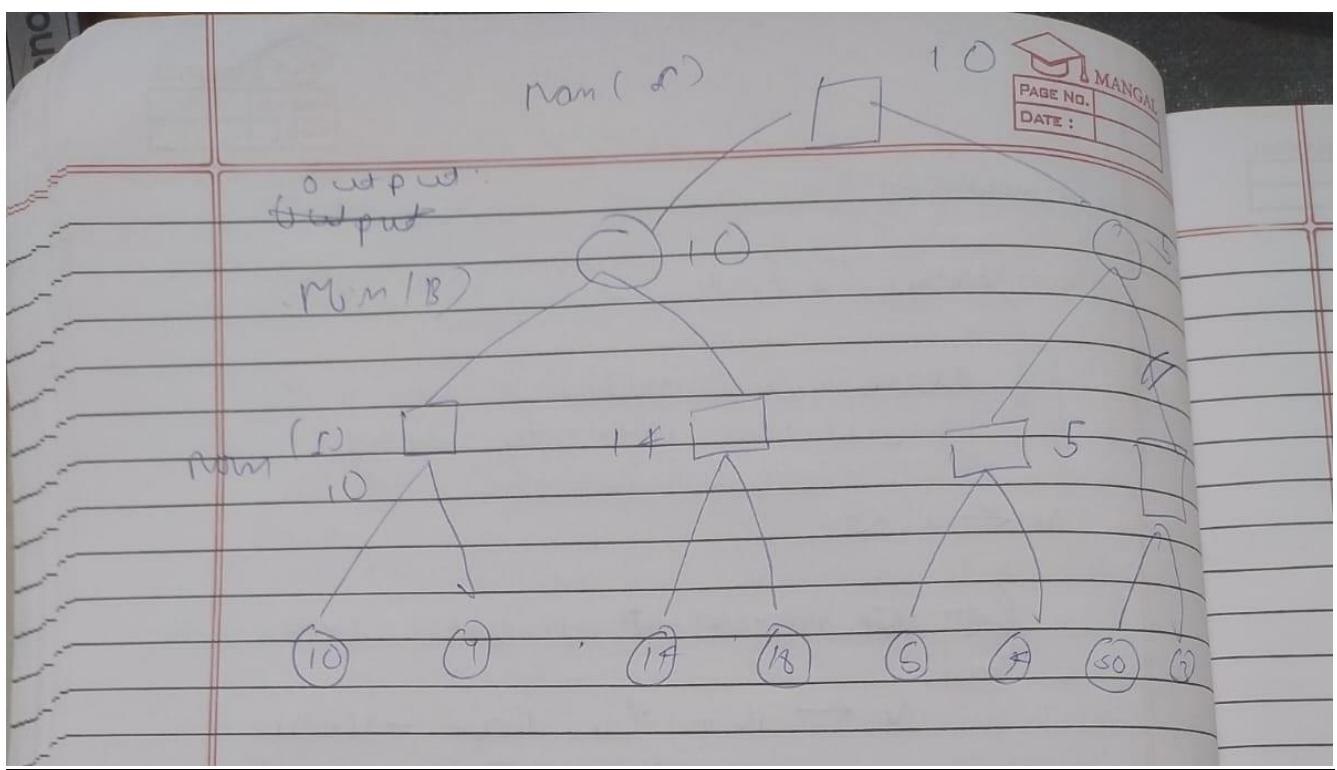
v ← numValue (s + ai, numValue (result (s, a), f, B))

if v ≤ f:

return v

B ← num (B, v)

return v



Code-

```
import math

# Alpha-Beta Pruning Function
def alpha_beta_pruning(depth, node_index, is_max, scores, alpha, beta, max_depth,
path):
    # Base case: return leaf node value
    if depth == max_depth:
        path.append(node_index)
        return scores[node_index]

    if is_max:
        best = -math.inf
        for i in range(2): # each node has 2 children
            val = alpha_beta_pruning(depth + 1, node_index * 2 + i, False, scores, alpha,
beta, max_depth, path)
            best = max(best, val)
            alpha = max(alpha, best)
            if beta <= alpha:
                print(f"Pruned at depth {depth} (MAX node): alpha={alpha}, beta={beta}")
                break # Beta cut-off
        return best

    else:
        best = math.inf
        for i in range(2):
            val = alpha_beta_pruning(depth + 1, node_index * 2 + i, True, scores, alpha,
beta, max_depth, path)
            best = min(best, val)
            beta = min(beta, best)
            if beta <= alpha:
                print(f"Pruned at depth {depth} (MIN node): alpha={alpha}, beta={beta}")
                break # Alpha cut-off
        return best
```

```
# -----
```

```

# Example tree for demonstration
#
# Binary tree leaves (depth = 3)
scores = [3, 5, 6, 9, 1, 2, 0, -1]
max_depth = int(math.log(len(scores), 2))

path = []

print("Leaf node values:", scores)
print("Applying Alpha-Beta Pruning...\n")

root_value = alpha_beta_pruning(0, 0, True, scores, -math.inf, math.inf, max_depth,
path)

print("\nResult:")
print(f"Value of the root node (best achievable for MAX): {root_value}")
print(f"Nodes explored (leaf indices): {path}")

```

Output -

```

Leaf node values: [3, 5, 6, 9, 1, 2, 0, -1]
Applying Alpha-Beta Pruning...

Pruned at depth 2 (MAX node): alpha=6, beta=5
Pruned at depth 1 (MIN node): alpha=5, beta=2

Result:
Value of the root node (best achievable for MAX): 5
Nodes explored (leaf indices): [0, 1, 2, 4, 5]

```