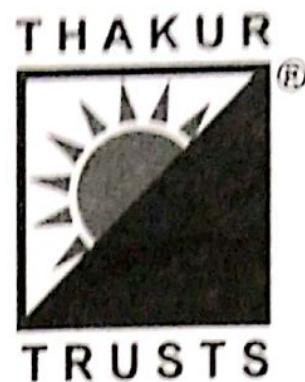


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SEMESTER Sem - II UID No. _____

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who has worked for the year 2019-20 in the Computer
Laboratory.

N. Ver

Teacher In-Charge

Head of Department

Date : 01.3.20

Examiner

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Basics of R-Software

- 1.] It is a Software of data analysis and statistical computing.
- 2.] It is a Software by which effective data handling and outcome storage is possible
- 3.] It is capable of graphical display.
- 4.] It is a free Software

Q I:]
$$\begin{aligned} & 2^2 + 1 - 51 + 4 \times 5 + 6/5 \\ & \geq 2^2 + \text{abs}(C-5) + 4 * 5 + 6/5 \\ & [1] 30.2 \end{aligned}$$

Q II:]
$$\begin{aligned} & x=20 \\ & y=2x \\ & z=2^n+y \\ & \sqrt{x+z} \\ \rightarrow & \quad x=20 \\ & \quad y=2^x \\ & \quad z=x+y \\ & \quad \sqrt{x+z} \\ & [1] 7.745967 \end{aligned}$$

Q III:]
$$\begin{aligned} & n=10 \\ & y=15 \\ & z=5 \end{aligned}$$

$\sqrt{xy^2}$
 c. J. ground \sqrt{meyz}
 d. J. ground \sqrt{meyz}

$$x = 10$$

$$y = 15$$

$$z = 5$$

$$x^2 + y^2$$

$$[1] 30$$

$$x^2 * y^2$$

$$[1] (150)$$

$$\sqrt{x^2 + y^2}$$

$$[1] (27.38613)$$

A vector in R software is denoted by the syntax

$$c(2, 3, 5, 7)^2$$

$$x = c(2, 3, 5, 7)$$

$$x^2$$

$$[1] 4 \quad 9 \quad 25 \quad 49$$

$$(2, 3, 5, 7) ^c (2, 3)$$

$$4 \quad 27 \quad 25 \quad 343$$

$$(2, 3, 5, 7, 9) ^c (2, 3)$$

Warning message

$$(1, 2, 3, 4, 5, 6) ^c (2, 3, 4)$$

$$[1] 18 \quad 9 \quad 64 \quad 25 \quad 216$$

$$(4, 6, 8, 10) * 3$$

$$12 \quad 18 \quad 24 \quad 30$$

$c(4, 6, 8, 10) * c(-1, -2, -3, -4)$

[1] -4 -12 -24 -40

$c[2, 3, 5, 7] * c[-2, -3]$

[1] 0.2500000

0.037027037

$c(2, 3, 5, 7) + 10$

12 13 15 17

$c(2, 3, 5, 7) + c(-2, -3, -1, 0)$

$c(2, 3, 5, 7) / 2$

[1] 1.0 1.5 2.5 3.5

find the sum of Product maximum and minimum

for values of

$x = c(2, 8, 4, 9, 11, 10, 7, 6)^{1/2}$

? sum(x)

[1] 455

? product(x)

[1] 4425974784

? max(x)

[1] 121

? min(x)

[1] 4

n matrix column = 4, ncol = 2, data = c(1, 2, 3, 4, 5, 6, 7, 8)

? x [1] [2]

[1] 1 5

[2] 2 6

[3] 3 7

[4] 4 8

$$\begin{bmatrix} 4 & 7 & 4 \\ 5 & 8 & 0 \\ 6 & 9 & 2 \end{bmatrix} + \begin{bmatrix} 6 & 11 & 9 \\ 4 & 12 & 7 \\ 5 & 8 & 4 \end{bmatrix} = \begin{bmatrix} 10 & 22 & 13 \\ 9 & 20 & 11 \\ 11 & 17 & 6 \end{bmatrix}$$

~~1) c-matrix C nrow = 3, ncol = 3, data = c (4, 5, 6, 7, 8, 9, 10, 12)~~

~~2) c-matrix C nrow = 3, ncol = 3, data = c (6, 4, 5, 11, 12, 8, 9, 7, 4)~~

$$\begin{array}{c} z^n \\ [1,] \end{array} \quad \begin{bmatrix} 1,1 \\ 4 \end{bmatrix} \quad \begin{bmatrix} 1,2 \\ 7 \end{bmatrix} \quad \begin{bmatrix} 1,3 \\ 4 \end{bmatrix}$$

$$\begin{array}{c} \\ [2,] \end{array} \quad \begin{bmatrix} 2,1 \\ 5 \end{bmatrix} \quad \begin{bmatrix} 2,2 \\ 8 \end{bmatrix} \quad \begin{bmatrix} 2,3 \\ 0 \end{bmatrix}$$

$$\begin{array}{c} \\ [3,] \end{array} \quad \begin{bmatrix} 3,1 \\ 6 \end{bmatrix} \quad \begin{bmatrix} 3,2 \\ 9 \end{bmatrix} \quad \begin{bmatrix} 3,3 \\ 2 \end{bmatrix}$$

$$\begin{array}{c} z^y \\ [1,] \end{array} \quad \begin{bmatrix} 1,1 \\ 6 \end{bmatrix} \quad \begin{bmatrix} 1,2 \\ 11 \end{bmatrix} \quad \begin{bmatrix} 1,3 \\ 9 \end{bmatrix}$$

$$\begin{array}{c} \\ [2,] \end{array} \quad \begin{bmatrix} 2,1 \\ 4 \end{bmatrix} \quad \begin{bmatrix} 2,2 \\ 12 \end{bmatrix} \quad \begin{bmatrix} 2,3 \\ 2 \end{bmatrix}$$

$$\begin{array}{c} \\ [3,] \end{array} \quad \begin{bmatrix} 3,1 \\ 5 \end{bmatrix} \quad \begin{bmatrix} 3,2 \\ 8 \end{bmatrix} \quad \begin{bmatrix} 3,3 \\ 4 \end{bmatrix}$$

$z^x * z$

≥ 0

	$[1,1]$	$[1,2]$	$[1,3]$
$[1,1]$	8	14	8
$[1,2]$	10	16	0
$[1,3]$	12	18	4

$\geq 9^* 2$

	$[1,1]$	$[1,2]$	$[1,3]$
$[1,1]$	12	22	18
$[1,2]$	8	24	14
$[1,3]$	10	16	8

$\geq x+y$

	$[1,1]$	$[1,2]$	$[1,3]$
$[1,1]$	10	18	13
$[1,2]$	9	20	7
$[1,3]$	11	17	6

$\geq x+y$

	$[1,1]$	$[1,2]$	$[1,3]$
$[1,1]$	24	77	36
$[1,2]$	20	96	6
$[1,3]$	30	72	8

Practical - 2

Binomial Distribution

n = total no. of trials

p = P (success)

q = P (failure)

x = no. of success out of n

$$P(x) = {}^n C_x \cdot p^x \cdot q^{n-x}, x=0, 1, \dots, n$$

$$f(x) = np$$

$$V(x) = npq$$

$d\text{binom}(n, p)$	$P(x)$
$n \neq p$	$E(x)$
$n \neq p \neq q$	$V(x)$

$$P(\text{binom}(n, p)) \quad P(x \leq k), \quad P(x > k) = 1 - P(x \leq k)$$

Q1] Toss a coin 20 times with probability of Head = 0.6

Let x be the no. of heads

Find the probability of:

(i) 7 Heads

(ii) 4 Heads

(iii) At most 4 Heads

(iv) At least 6 Heads

(v) No heads

(vi) All heads

(vii) expectation & Variance

> n = 10

> p = 0.6

> q = 0.4

> dbinom(7, 10, 0.6)

[1] 0.1449908

> dbinom(4, 10, 0.6)

[1] 0.114767

> pbisnom(4, 10, 0.6)

[1] 0.1662386

> 1 - pbisnom(6, 10, 0.6)

[1] 0.3822806

> dbisnom(0, 10, 0.6)

[1] 0.40001048576

> dbisnom(10, 10, 0.6)

[1] 0.006086618

> exp(-10 * 0.6)

> exp

[1] 6

> Var = 10 * 0.6 * 0.4

> Var

> 2.4

There are 12 mcq's in an English question paper. A question has 5 answers and only 1 of them is correct. Find the probability of having

- (i) 4 correct answer
- (ii) almost 4 correct answer
- (iii) at least 3 correct answer

$$n=12, p=1/4$$

$$(i) P(X=4)$$

$$\approx \text{dbinom}(4, 12, 1/5)$$

$$[1] 0.1228756$$

$$(ii) P(X \leq 4)$$

$$\approx \text{pbinom}(4, 12, 1/5)$$

$$[4] 0.9274445$$

~~$$(iii) P(X \geq 3) = P(X > 2)$$~~

~~$$\Rightarrow 1 - \text{pbinom}(2, 12, 1/5)$$~~

~~$$[1] 0.4416543$$~~

Q8] Find complete binomial distribution where $n=5$

$$p=0.1$$

$$\approx \text{dbinom}(0, 5, 0.1)$$

$$[1] 0.59049$$

$$\approx \text{dbinom}(1, 5, 0.1)$$

$$[1] 0.32805$$

$$\approx \text{dbinom}(2, 5, 0.1)$$

$$[1] 0.729$$

$$\approx \text{dbinom}(3, 5, 0.1)$$

$$[1] 0.0081$$

$$\approx \text{dbinom}(4, 5, 0.1)$$

$$\approx \text{dbinom}(5, 5, 0.1)$$

$$[1] 1e-05$$

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1] find Probability of exactly 10 success outcome 100

$$\text{Details} = 0.1$$

$$\Rightarrow \text{binom}(10, 100, 0.1)$$

$$[1] 0.1318653$$

] x follows binomial distribution with $n=12$,

$$p=0.25$$

$$\text{find (i) } P(X \leq 5) \quad (\text{ii) } P(X > 7)$$

$$(\text{iii) } P(5 \leq X \leq 7)$$

$$(\text{i) } P(X \leq 5)$$

$$\Rightarrow \text{pbnom}(5, 12, 0.25)$$

$$[1] 0.9455978$$

$$(\text{ii) } 1 - \text{pbnom}(7, 12, 0.25)$$

$$[1] 0.00278151$$

$$(\text{iii) } P(5 \leq X \leq 7)$$

$$[1] 0.04014945$$

(iv)

1) There are 10 members in a committee probability of any member attending a meeting 0.9 ways
Probability that 7 or more member will present in meeting

$$n=10, x=7, p=0.9$$

$$\Rightarrow 1 - \text{pbnom}(6, 10, 0.9)$$

$$[1] 0.9872048$$

Q1] A salesman has 20 trolley bags he will meet 20 customers what minimum no. of bags will be made with 88% probability

$$\therefore n = 50, p = 0.88$$

$\therefore qbinom(p, n, p)$

$\therefore qbinom(0.88, 30, 0.2)$

[Ans] 9

Q2] $n = 10, p = 0.6$ find the binomial distribution plot the graph of p.m.f & c.d.f.

$$q_n = 10, p = 0.6$$

$$\therefore n = 0.65$$

$\therefore bp = dbinom(k, n, p)$

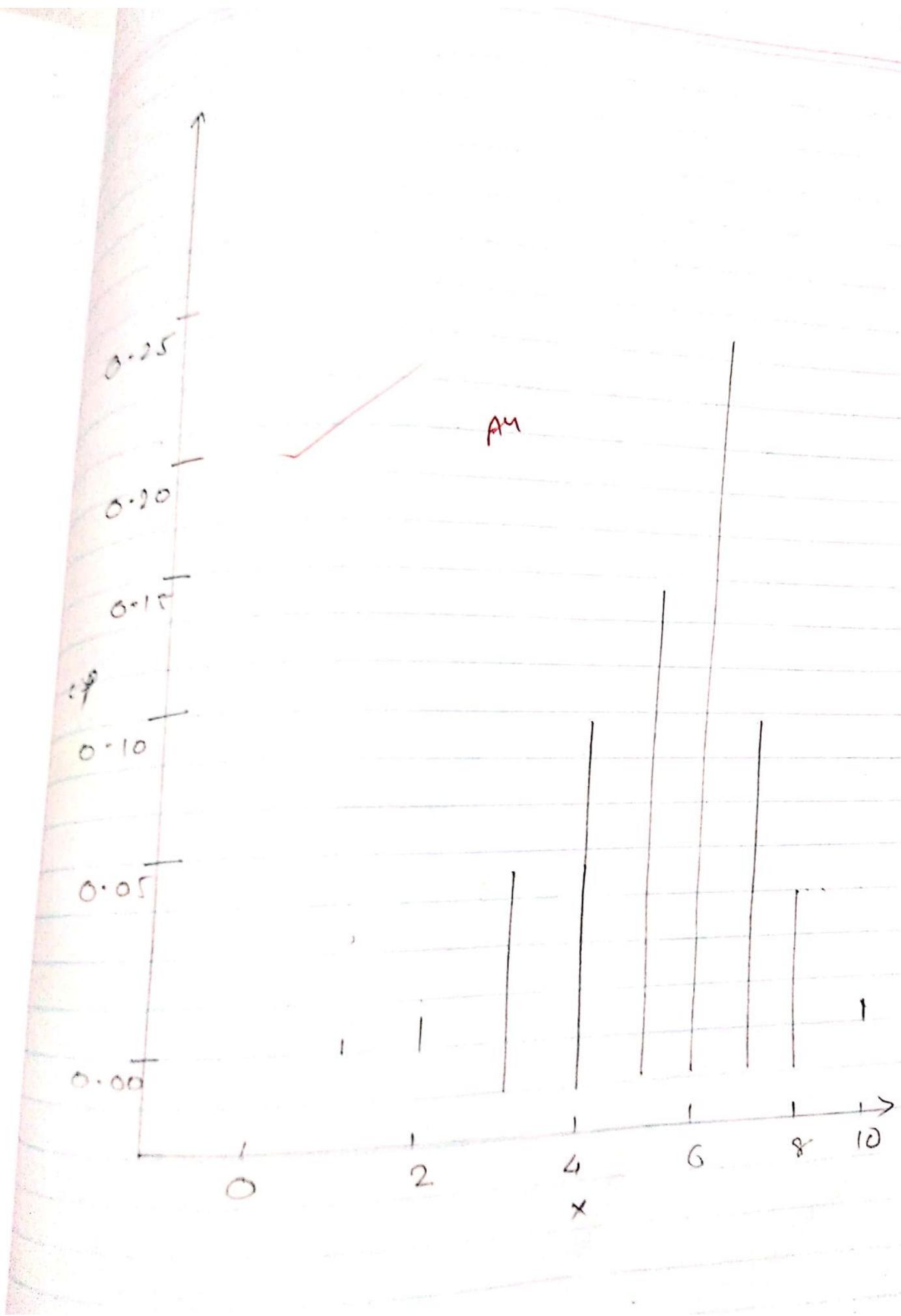
$\therefore df = data.frame("x-values" = x, "probability" = bp)$

print(df)

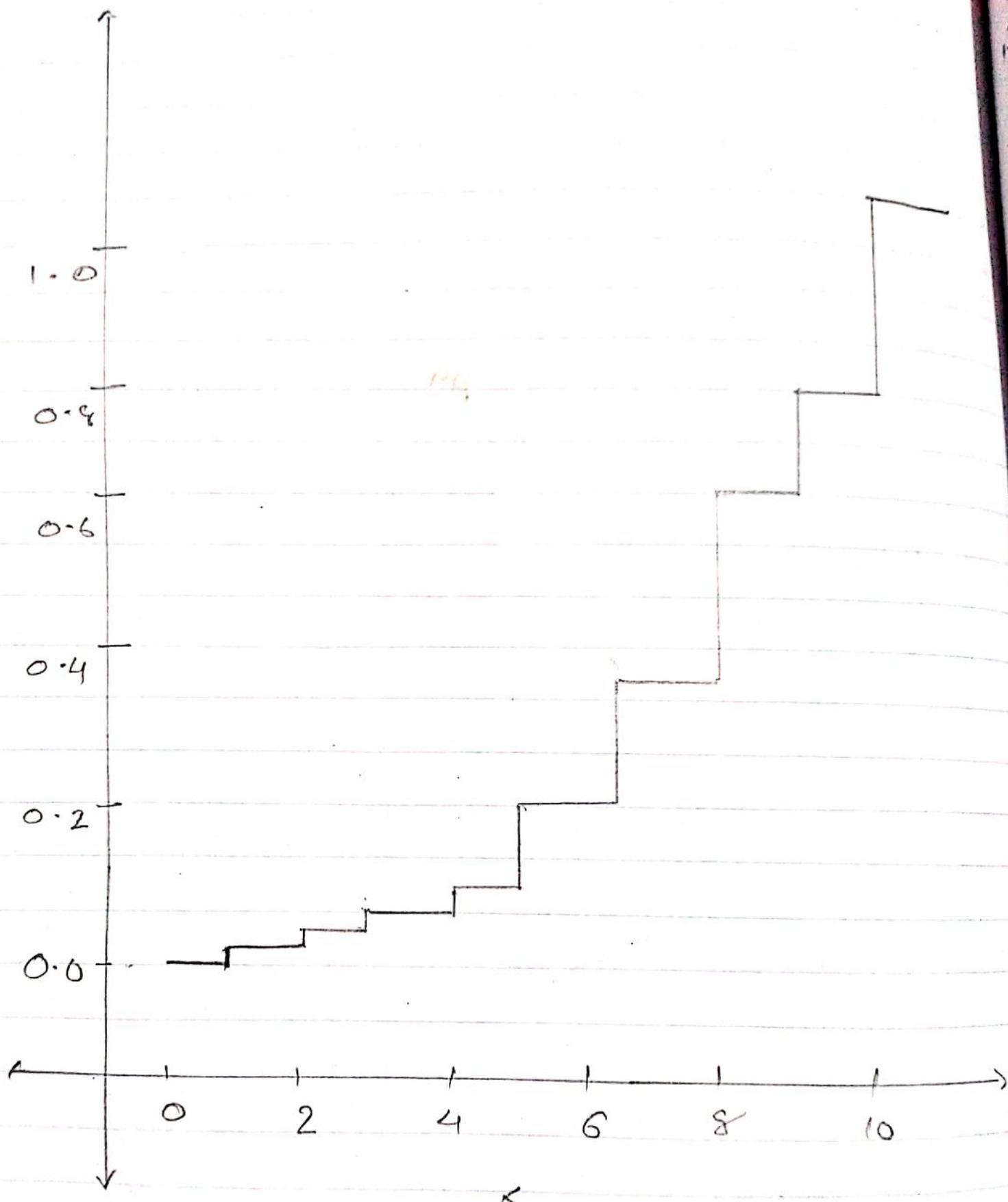
x-values	probability
0	0.0001048576
1	0.0015728640
2	0.0106168320
3	0.0424673280
4	0.1114967360
5	0.2006581248
6	0.2908226568
7	0.2149908480
8	0.1704223520
9	0.0403107340
10	0.00604641767

γραμτής (γράμπα γράμπα)
γράμπα γράμπα γράμπα
γράμτης (γράμπα γράμπα)





6a



Practical no: 8
check the following are pmf (Probability Mass Function) or not

x	1	2	3	4	5
$p(x)$	0.2	0.5	-0.5	0.4	0.4

since the Probability is negative.
 \therefore it is not a pmf.

x	10	20	30	40	50
$p(x)$	0.3	0.2	0.3	0.1	0.1

The condition for pmf is

$$\textcircled{1} \quad 0.5 p(x) \leq 1 - \textcircled{1}$$

$$\textcircled{2} \quad \sum p_x = 1 - \textcircled{2}$$

$$\therefore \text{prob} = C(0.3, 0.2, 0.3, 0.1, 0.1)$$

sum (prob)

[1] 1

Since both the conditions are satisfied it is a pmf

x	0	1	2	3	4
$p(x)$	0.4	0.2	0.3	0.2	0.1

The condition to check pmf are:

$$\textcircled{1} \quad 0 \leq p(x) \leq 1$$

$$\textcircled{2} \quad \sum p(x) = 1$$

$$\therefore \text{prob} = C(0.4, 0.2, 0.3, 0.2, 0.1)$$

sum (prob)

[1] 1.2

Here the second condition does not satisfy
Hence it is not a pmf.

Q.2] Following is a pmf of x . Find mean,
variance.

x	1	2	3	4	5
$P(x)$	0.1	0.15	0.2	0.2	0.25

x	$P(x)$	$x \cdot P(x)$	$x^2 \cdot P(x)$
1	0.1	0.1	0.1
2	0.15	0.3	0.6
3	0.2	0.6	1.8
4	0.2	1.2	4.8
5	0.25	1.25	6.25
		<u>3.45</u>	<u>13.55</u>

$$\rightarrow n = C(1, 2, 3, 4, 5)$$

$$\rightarrow p_{prob} = C(0.1, 0.15, 0.2, 0.2, 0.25)$$

$$\rightarrow a = n * p_{prob}$$

$$\rightarrow \text{mean} = \text{sum}(a)$$

$$\rightarrow \text{mean}$$

$$[1] 3.45$$

$$\rightarrow b = (x^2) * p_{prob}$$

$$\rightarrow b$$

$$[1] 0.10 \cdot 0.60 \quad 1.80 \quad 4.80 \quad 6.25$$

$$\rightarrow \text{var} = \text{sum}(b) - \text{mean} \cdot n$$

$$\rightarrow \text{var}$$

$$[1] 1.6475$$

7) following is a p.m.f of x . find mean and variance.

x	5	10	15	20	25
$p(x)$	0.1	0.3	0.2	0.25	0.15

$$x = C(5, 10, 15, 20, 25)$$

$$p_{\text{prob}} = C(0.1, 0.3, 0.2, 0.25, 0.15)$$

$$\tau_a = x * p_{\text{prob}}$$

τ_a

$$[1] 0.50 \quad 3.00$$

$$\tau_{\text{mean}} = \text{sum}(\tau_a)$$

τ_{mean}

$$[1] 15.25$$

$$\tau_b = (\tau_a^2) * p_{\text{prob}}$$

τ_b

$$[1] 2.50 \quad 30.00 \quad 45.00 \quad 100.00$$

$$\tau_{\text{var}} = \text{sum}(\tau_b) - \text{mean}^2$$

τ_{var}

$$[1] 38.6875$$

4) find cdf of the following pmf and draw the graph of cdf.

1)	x	1	2	3	4
	$p(x)$	0.4	0.3	0.2	0.1

$$\Rightarrow x = C(1, 2, 3, 4)$$

$$\Rightarrow p_{\text{prob}} = C(0.4, 0.3, 0.2, 0.1)$$

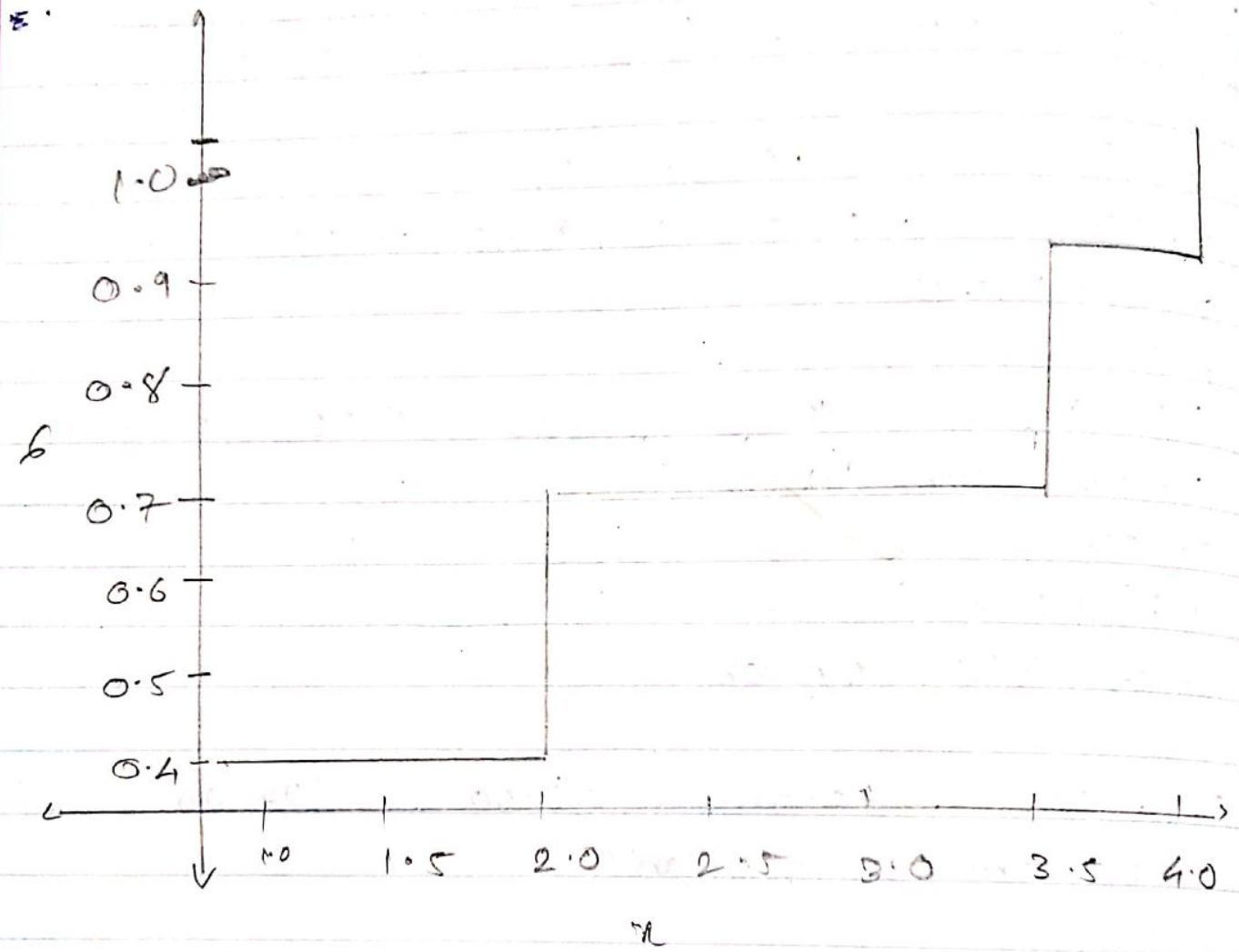
$$\Rightarrow a = \text{cumsum}(p_{\text{prob}})$$

Σa

$$\text{[1]} \quad 0.4 \quad 0.7 \quad 0.9 \quad 1.0$$

$\Sigma_{\text{plot}} \quad (x, a, "1s")$

*



$$f(n) = 0 \quad , \quad n \leq 1$$

$$= 0.4 \quad 1 \leq n \leq 2$$

$$= 0.7 \quad 2 \leq n \leq 3$$

$$= 0.9 \quad 3 \leq n \leq 4$$

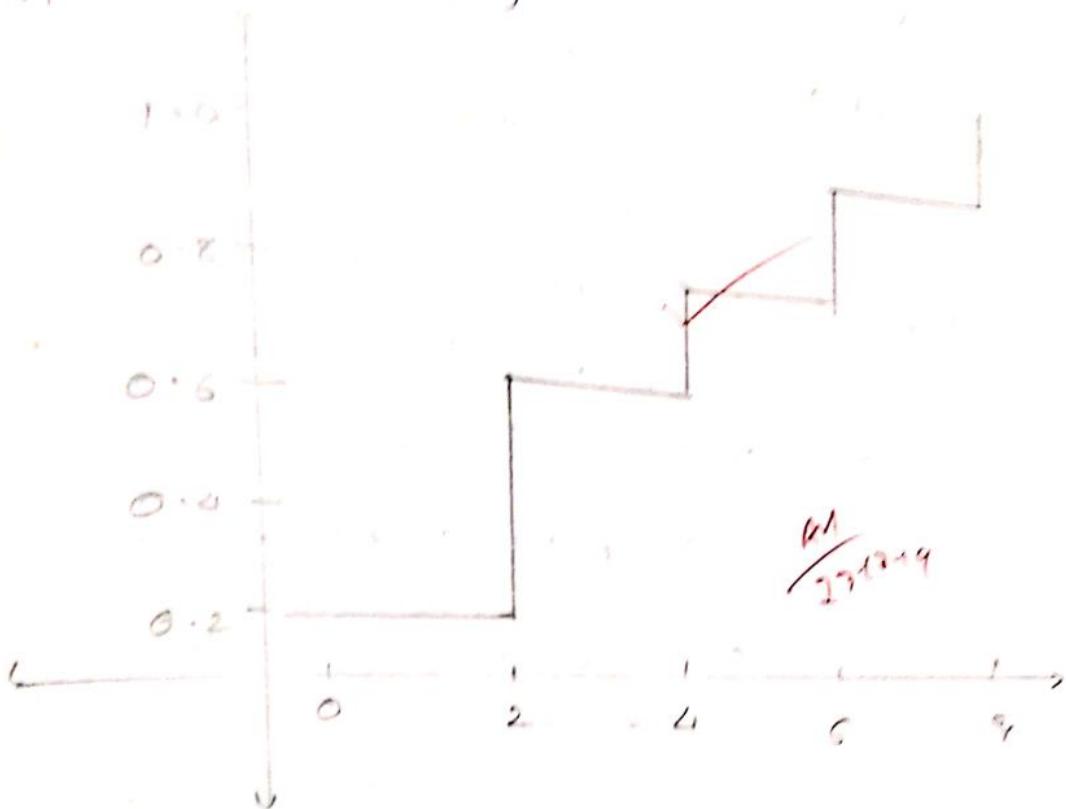
$$= 1.0 \quad n \geq 4$$

2.J

	0	1	2	3	4	5	6	7
$P(n)$	0.2	0.3	0.2	0.2	0.2	0.1		

$\rho_A = (0.2, 0.5, 0.3)$
 $\rho_B = (0.2, 0.2, 0.2, 0.3, 0.4)$
 ρ_A
 $\rho_A \in \text{convex}(\rho_B)$,
 ρ_A
 $\rho_A \in (0.2, 0.5, 0.3)$
 $\rho_A \in \text{convex}(\rho_B)$

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ρ_A
 $\rho_A \in \text{convex}(\rho_B)$

$$\begin{aligned}
 F(x) &= 0 & n \leq 0 \\
 &= 0.2 & 0 \leq n \leq 2 \\
 &= 0.5 & 2 \leq n \leq 4 \\
 &= 0.7 & 4 \leq n \leq 6 \\
 &= 0.9 & 6 \leq n \leq 8 \\
 &= 1.0 & n \geq 8
 \end{aligned}$$

Practical No. 4

Practise:-

Q.] X follows binomial distribution with $P=0.6$ $q=0.4$.

Find

a) $P(X=7)$

b) $P(X \leq 2)$

$$\rightarrow P(X=7) = {}^8C_7 (0.6)^7 (0.4)^{8-7}$$

$$= {}^8C_7 \times 0.2799 \times 0.4$$

$$= 0.8957.$$

$$P(X \leq 3) = P(0) + P(1) + P(2) + P(3)$$

$$= {}^8C_0 (0.6)^0 (0.4)^8 + {}^8C_1 (0.6)^1 (0.4)^7$$

$$+ {}^8C_2 (0.6)^2 (0.4)^6 + {}^8C_3 (0.6)^3 (0.4)^5$$

$$= 1 \times 1 \times 0.00065536 \times 8 \times 0.6 \times 0.001638$$

$$+ 42 \times 0.36 \times 0.0004096 +$$

$$56 \times 0.216 \times 0.101024$$

$$= 0.1736704$$

$$P(X=2 \text{ or } 3) = P(2) + P(3)$$

$$= {}^8C_2 (0.6)^2 (0.4)^6 + {}^8C_3 (0.6)^3 (0.4)^5$$

$$= 2^8 \times 0.36 \times 0.004096 + 56 \times$$

$$0.216 \times 0.101024$$

$$= 0.04128768 + 0.12386804$$

$$= 0.16515012$$

Practical No. 5

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Normal Distribution \rightarrow

Normal distribution is an example of continuous probability distribution

$$x \sim N(\mu, \sigma^2)$$

a) $P(x = x)$ answer $\text{dnorm}(x, \mu, \sigma)$

b) $P(x < x)$ = $\text{pnorm}(x, \mu, \sigma)$

c) $P(x > x)$ = $1 - \text{pnorm}(x, \mu, \sigma)$

d) To find the value of x so that the command is given
 $\text{qnorm}(p, \mu, \sigma)$

$$k \quad P(x \geq k) = p$$

$\text{qnorm}(p, \mu, \sigma)$

e) To generate a random sample of size n ,
 ~~$\text{rnorm}(n, \mu, \sigma)$~~

A random variable $x \sim N(10, 2)$. Find

1.] $P(x \leq 7)$ 2.] $P(x \geq 12)$ 3.] $P(5 \leq x \leq 12)$

4.] $P(x < k) = 0.4$ with $\mu = 10, \sigma = 2$

$$x \sim N(100, 36)$$

$$\sigma = \sqrt{36}$$

1.] $P(x \leq 110)$

$$2.] P(x > 105)$$

$$3.] P(x \leq 92)$$

4.] $P(95 \leq x \leq 110)$

$$5.] P(x \geq k) = 0.9$$

Generate 10 random sample and find the sample mean, median and variance, standard deviation

$\sigma_{\text{tot}} = 10$

$\epsilon = 3/2$

$\epsilon_{\text{p1}} = \text{pnasim}(0.1, m, s)$

$\Rightarrow \text{cat}(\text{C}^1 p \text{ exz=1}) \text{ is } "1", \text{ p1}$

$P(\text{exz=1}) \text{ is } = 0.68688477$

$\epsilon_{\text{p2}} = \text{pnasim}(0.1, m, s)$

$\Rightarrow \text{cat}(\text{C}^1 p \text{ exz=1}) \text{ is } "1", \text{ p2}$

$P(\text{exz=1}) \text{ is } = 0.15886582$

$\epsilon_{\text{p3}} = \text{pnasim}(0.1, m, s) - \text{pnasim}(0.5, m, s)$

$\Rightarrow \text{cat}(\text{C}^1 p \text{ exz=1 to 12}) \text{ is } "1", \text{ p3}$

$P(\text{exz=1 to 12}) \text{ is } = 0.4831651$

$\epsilon_{\text{p4}} = \text{pnasim}(0.1, m, s)$

$\Rightarrow \text{cat}(\text{C}^1 p \text{ exz=1 to 12}) \text{ is } "1", \text{ p4}$

$P(\text{exz=1 to 12}) \text{ is } = 0.4493306$

$\int \sigma_m = 100$

$\Rightarrow S = \sqrt{100 \cdot 0.86}$

$\epsilon_{\text{p1}} = \text{pnasim}(0.1, m, s)$

$\Rightarrow \text{cat}(\text{C}^1 p \text{ exz=1 to 10}) \text{ is } "1", \text{ p1}$

$P(\text{exz=1 to 10}) \text{ is } = 0.9522096$

$\epsilon_{\text{p2}} = 1 - \text{pnasim}(0.1, m, s)$

$\Rightarrow \text{cat}(\text{C}^1 p \text{ exz>10}) \text{ is } "1", \text{ p2}$

$P(\text{exz>10}) \text{ is } = 0.2028284$

$\epsilon_{\text{p3}} = \text{pnasim}(0.1, m, s)$

$\Rightarrow \text{cat}(\text{C}^1 p \text{ exz=92}) \text{ is } "1", \text{ p3}$

$P(\text{exz=92}) \text{ is } = 0.09121122$

$\epsilon_{\text{p4}} = \text{pnasim}(0.1, m, s) - \text{pnasim}(0.95, m, s)$

$\Rightarrow \text{cat}(\text{C}^1 p \text{ exz=95 to 110}) \text{ is } "1", \text{ p4}$

$P(\text{exz=95 to 110}) \text{ is } = 0.7498813$

$\mu = \text{exp}(\bar{x} + 0.5 \cdot \text{sd}^2) = \text{exp}(16 + 0.5 \cdot 18)$
 $\sigma = \text{sqrt}(\text{exp}(\bar{x} + 2 \cdot \text{sd}^2) - \text{exp}(\bar{x} + 0.5 \cdot \text{sd}^2))$

$\mu = 10$
 $\sigma = 3$
 $n = 10$
 $x = \text{rnorm}(n=10, \mu, \sigma)$
 x

[1] 11.622405	9.686588	12.259686
9.051027	15.217608	12.706428
16.825089	16.117816	8.762215
6.842165		

$\rightarrow m = \text{mean}(x)$

$\rightarrow M$
[1] 11.8102

$\rightarrow m = \text{median}(x)$

$\rightarrow m$

[1] 10.77636

$\rightarrow v = (n-1) * (\text{var}(x) / n)$

$\rightarrow V$

[1] 8.977855

$\rightarrow sd = \text{sqrt}(v)$

$\rightarrow s.d. = \text{sqrt}(v)$

$\rightarrow sd$

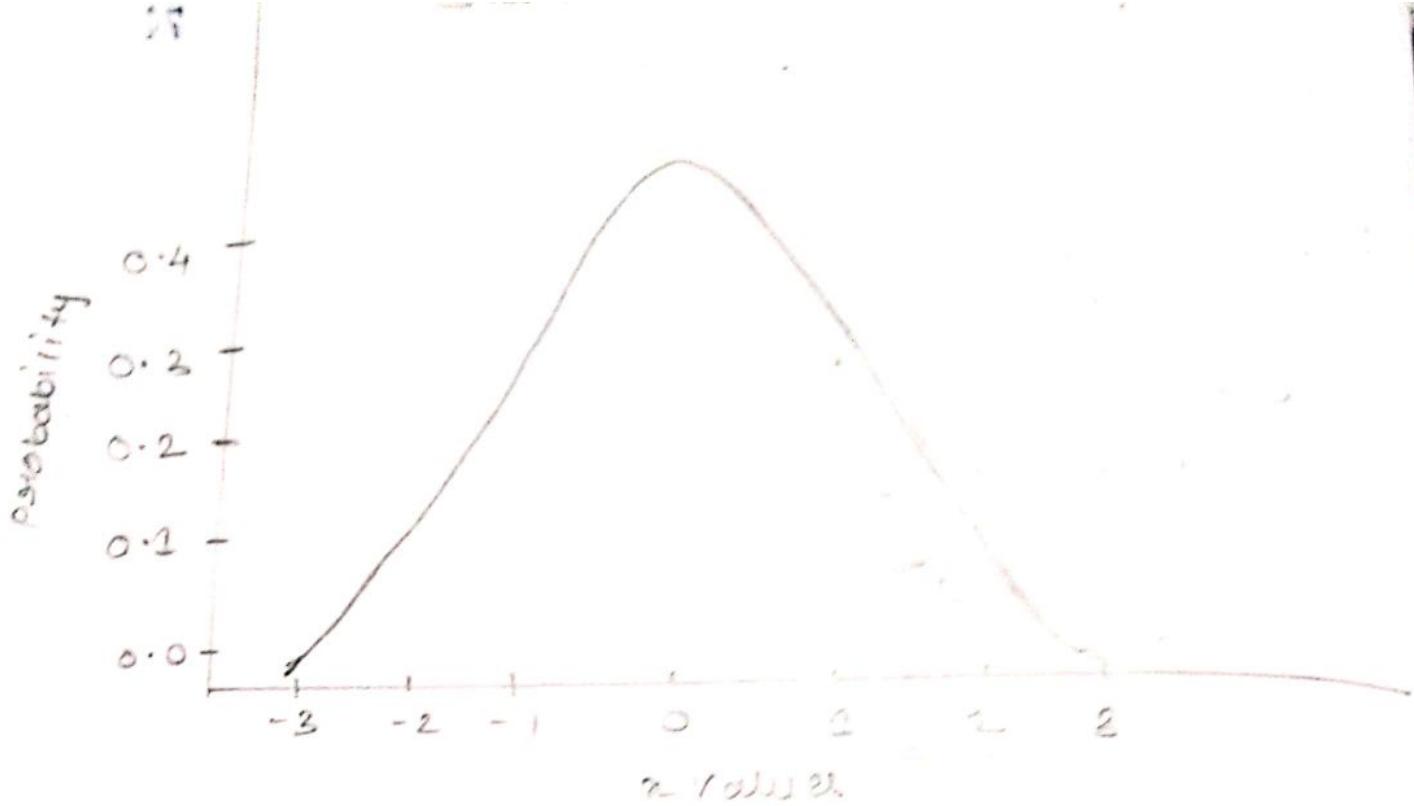
[1] 2.996307

\rightarrow plot the standard Normal curve

$x = \text{seq}(-3, 3, by = 0.1)$

$y = \text{dnorm}(x)$

? plot(x, y, xlab = "value", ylab = "probability")
? main = "Standard normal curve"



Q.5.] $\text{mean } (50, 100)$

Find 1.] $P(x \leq 60)$ 2.] $P(x > 65)$

3.] $P(45 \leq x \leq 60)$

$$\rightarrow \mu = 50$$

$$\sigma = \sqrt{100}$$

$$= 5$$

$$\sigma^2 = 10$$

$$\frac{P(x)}{\sqrt{10}}$$

$$\text{zp1} = \text{pnorm}(60, 0, 5)$$

$$\text{zp1}$$

$$[1] 0.8413447$$

$$\text{zp2} = 1 - \text{pnorm}(65, 0, 5)$$

$$\text{zp2}$$

$$[1] 0.668072$$

$$\text{zp3} = \text{pnorm}(60, 0, 5) - \text{pnorm}(45, 0, 5)$$

$$\text{zp3}$$

$$[1] 0.5328072$$

Practical No. 6

Topic :- Z and t

distribution Sums.

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- 1] Test the hypothesis $H_0: \mu = 20$ against $H_1: \mu \neq 20$ sample of size 400 with selective and sample mean 20.2 and a standard deviation 2.25 test that 5% level of significance.

$$m_0 = 20$$

$$m_t = 20.2$$

$$sd = 2.25$$

$$n = 400$$

$$z_{\text{cal}} = (m_t - m_0) / (sd / \sqrt{n})$$

$$z_{\text{cal}}$$

$$\approx 1.77778$$

at C 1% calculated is = "1, zcal)

z calculated is = 1.77778 ✓

pvalue

$$\approx 0.07544036$$

since pvalue is more than 0.05 we accept $H_0: \mu = 20$

- 2] We want to test the hypothesis $H_0: \mu = 250$ against $H_1: \mu \neq 250$ a sample of size 100 has a mean of 275 and sd as 30. Test the hypothesis at 5% level of significance.

$$m_0 = 250$$

$$m_t = 275$$

$$sd = 30$$

$$n = 100$$

$$z_{\text{cal}} = (\bar{x} - \mu_0) / (\sigma / \sqrt{n})$$

zcal

[1] 8.333333

> cat ("z calculated is = ", zcal)

z calculated is = 8.333333 >

> pvalue = 2 * (1 - pnorm (abs (zcal)))

pvalue

[1] 0

Since pvalue is less than 0.05 we reject H_0 .

Q8.] we want to test the hypothesis $H_0: P = 0.2$ against $H_1: P \neq 0.2$ ($P = \text{population proportion}$)
A sample of 400 is selected and the sample proportion is calculated 0.125. Test the hypothesis at 1% level of significance.

$$\rightarrow P = 0.2 \quad H_0:$$

$$\tau Q = 1 - P$$

$$\tau p = 0.125$$

$$\tau n = 400$$

$$z_{\text{cal}} = (p - P) / \sqrt{P(1-P)/n}$$

zcal

[1] -3.75

> pvalue = 2 * (1 - pnorm (abs (zcal)))

pvalue

[1] 0.0001768346

Since pvalue is less than 0.05 we reject H_0 .

In a big city 325 men out of 600 men were found to be self employed. Thus this information supports the conclusion that exactly $\frac{1}{2}$ of the men are self-employed.

$$z_p = 0.5$$

$$z_n = 600$$

$$z_p = 325/600$$

$$z_Q = 1 - p$$

$$z_{\text{cal}} = (p - P) / \sqrt{(P * Q/n)}$$

$$z_{\text{cal}}$$

$$[1] 2.041241$$

$$z_{\text{pvalue}} = 2 * (1 - \text{pnorm}(z_{\text{cal}}))$$

$$z_{\text{pvalue}}$$

$$[1] 0.04122683$$

Since pvalue is less than 0.05 we reject H_0 .

Q5.] Test the hypothesis of $H_0: \mu = 50$ against $H_1: \mu \neq 50$

A sample of 30 is collected -

50, 49, 52, 44, 45, 48, 46, 45, 49, 45, 40, 47, 55

54, 46, 48, 47, 44, 59, 60, 61, 41, 52, 44, 55, 56, 46,

45, 48, 49

H_1'

$$\rightarrow m_0 = 50$$

$$z_x = c(50, 49, 52, \dots, 48, 49)$$

$$z_n = \text{length}(x) > n [1] 30$$

$$\text{mean} = \text{mean}(x) > mx [1] 49.3333$$

$$\text{variance} = (n-1) * \text{var}(x)/n [1] 30.45556$$

$$\text{sd} = \sqrt(\text{variance}) > sd [1] 5.563778$$

$$z_{\text{cal}} = (mx - m_0) / sd / (\sqrt(n))$$

$$z_{\text{cal}}$$

$$[1] -0.6562964$$

$z\text{ value} = 2.4$ - positive

z value

0.5116284

Since $p\text{ value}$ is more than 0.05 we accept

$H_0: \mu = 50$

$$\frac{P}{27.5} \chi^2$$

Practical - 7.

Topic: \Rightarrow Large Sample test

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P.Q.] Two random samples are drawn from two populations with a standard deviation 2 & 3 respectively test the hypothesis that the two population means are equal at 5% level of significance sample means are 67 and 68 respectively.

$$\Rightarrow n_1 = 1000$$

$$n_2 = 2000$$

$$m_{n_1} = 67$$

$$m_{n_2} = 68$$

$$sd_1 = 2$$

$$sd_2 = 3$$

$$z_{cal} = (m_{n_1} - m_{n_2}) / \sqrt{sd_1^2/n_1 + sd_2^2/n_2}$$

\Rightarrow cal z^2 calculated is $= 10.84652$

z calculated is $= -10.84652$

$$p\text{value} = 2 * (1 - \text{pnorm}(|z_{cal}|))$$

$\Rightarrow p\text{value}$

[1] 0

Since $p\text{value}$ is less than 0.05 we reject H_0 : $\mu_1 = \mu_2$.

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1) A study of noise level in 2 hospitals is done following data is calculated.
 First Sample size = 84, First Sample mean = 52, First standard deviation = 7.9
 Second Sample size = 34, second sample mean = 54.4, second standard deviation = 7.8
 χ^2 test $H_0: \mu_1 = \mu_2$ at 1% of 105.

$$\Rightarrow n_1 = 84$$

$$\Rightarrow n_2 = 34$$

$$\Rightarrow \bar{m}_{n_1} = 61.2$$

$$\Rightarrow \bar{m}_{n_2} = 54.4$$

$$\Rightarrow S_{d1} = 7.9$$

$$\Rightarrow S_{d2} = 7.8$$

$$\Rightarrow z_{\text{calculated}} = (\bar{m}_{n_1} - \bar{m}_{n_2}) / \sqrt{S_{d1}^2/n_1 + S_{d2}^2/n_2}$$

$$\Rightarrow z_{\text{calculated}} \text{ is } 1.32 (z_{\text{cal}})$$

$$z_{\text{calculated}} \text{ is } 1.31 + 1.77$$

$$\Rightarrow p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$\Rightarrow p\text{value}$

$$[1] 0.25 & 0.06$$

Since pvalue is greater than 0.01, we accept H_0 i.e. $\mu_1 = \mu_2$.

3) From each of two population of oranges the following samples are collected to test whether the proportion of bad oranges are equal or not. First Sample size = 250
 Second Sample size = 200; no. of bad oranges

In the first sample = n_1 and second sample = n_2

$H_0: P_1 = P_2$ against $H_1: P_1 \neq P_2$

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$$n_1 = 250$$

$$n_2 = 200$$

$$P_1 = 44/250$$

$$P_2 = 30/200$$

$$P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$$

$$Q = 1 - P$$

$$\chi^2_{\text{cal}} = (P_1 - P)^2 / Q \sqrt{P * Q * (1/n_1 + 1/n_2)}$$

$$\chi^2_{\text{cal}} = 7.393582$$

$$\text{pvalue} = 2 * (\text{I}(\text{chi-square}))$$

$$\text{pvalue}$$

$$0.4596896$$

Since p Value is greater than 0.05, we

Q4] Random Sample of 400 males and 600 females when asked whether they want the ATM nearby 200 males and 390 females were in favor of the proposal. Test the hypothesis that the proportion of males and females proposal are equal at not at 5% level of significance.

$$n_1 = 400$$

$$n_2 = 600$$

$$P_1 = 200/400$$

$$P_2 = 390/600$$

$$P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$$

$$Q = 1 - P$$

$$\chi^2_{\text{cal}} = (P_1 - P)^2 / Q \sqrt{P * Q * (1/n_1 + 1/n_2)}$$

$\gamma_{2\text{cal}}$

$$[1] -4.724751$$

$\gamma_{p\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(\gamma_{2\text{cal}})))$

$\gamma_{p\text{value}}$

$$[1] 2.303972e-0.6$$

Since pvalue is less than 0.05 we reject H_0 . $p_{1,2}$

5.) Following are the two independent Sample from the two population test equality of two means at $\alpha = 1\% \text{ LOS}$

$$\gamma_{x1} = 74, 73, 79, 77, 76, 82, 72, 75, 78, 77, 78, 76, 76, 74$$

$$\gamma_{x2} = 72, 76, 74, 70, 70, 78, 70, 72, 75, 79, 79, 74, 75, 78, 72, 74, 80.$$

$$\rightarrow \gamma_{n1} = c(74, 77, 79, 77, \dots, 74)$$

$$\gamma_{n1} = \text{length}(\gamma_{x1}) \rightarrow [1] 14$$

$$\gamma_{m1} = \text{mean}(\gamma_{x1})$$

$$\gamma_{variance1} = (\gamma_{n1} - 1) * \text{Var}(\gamma_{x1}) / \gamma_{n1} [1] 0.4508$$

$$\gamma_{sd1} = \sqrt{\text{Variance1}} [1] 0.6711^2$$

$$\gamma_{x2} = (72, 76, \dots, 74, 80)$$

$$\gamma_{n2} = \text{length}(\gamma_{x2})$$

$$\gamma_{m2} = \text{mean}(\gamma_{x2})$$

$$\gamma_{variance2} = (\gamma_{n2} - 1) * \text{Var}(\gamma_{x2}) / \gamma_{n2} [1]$$

$$0.6163$$

$$\gamma_{sd2} = \sqrt{(\text{variance2})} [1] 0.7850$$

$$t\text{-test}([1], \gamma_{x1}, \gamma_{x2})$$

M

$$\gamma_{p\text{value}} = 0.1387$$

> 0.05 is accepted.

Topic: \rightarrow Small Sample test
 Q1.7 Random sample of 15 observations are given by 80, 100, 110, 105, 122, 70, 120, 110, 101, 88, 83, 95, 89, 107, 125. Do this data support that population mean is 100.

Soln $\rightarrow n = 15$ (80, 100, 110, 105, 122, 70, 120, 110, 101, 88, 83, 95, 89, 107, 125)

Σx

[1] 80 100 110, 105 122 70 120 110, 101,
 88 83, 95 89 107 125

T-test (n)

One sample t-test

Data: x

$t = 24.029$, $df = 14$, $p\text{-value} = 8.819 \times 10^{-13}$

alternative hypothesis: true mean is not equal to

91.37775 109.28892

Sample estimates

mean of x

100.3333

Since the p-value is greater than 0.005, the p-value is rejected.

$H_0: \mu \neq 100$

PB
Patients took 2 medicines one after another
in the weight reducing the average the decreasing
below
after medicine one given

medicine A
(kg)

10 12 13 14 15

medicine B

8 9 11 14 16 18 19

Is there a significant difference between the
means of medicine?

$$Sd_{n-2} = \sqrt{4.2} = 2.05$$

$$\bar{x}_{n-2} = \bar{x}(8, 9, 12, 14, 15, 16, 19) \\ \bar{x} = 13.8$$

$$\bar{x}_{n-1} = \bar{x}(10, 12, 13, 14, 15, 16) \\ \bar{x} = 13.2$$

$$\bar{x}_n = \bar{x}(10, 12, 13, 14, 15, 16, 19) \\ \bar{x} = 14.2$$

$$\bar{x}_{n-1}$$

$$[13.2, 14.2]$$

$$[13.2, 14.2]$$

welch true sample t-test

data $\bar{x} \times 1$ and s^2

$$t = 0.80384, df = 9.7094, p\text{-value} = 0.4406$$

alternative hypothesis: true difference
in means is not equal to 0.95%.

95% interval:

$$[-1.78117, 3.48271]$$

Sample estimates

mean of x mean y

12

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Q.4.] The weight reducing diet program
conducted and observation are noted for
10 participants test whether diet program
is effective or not.

Before = (120, 125, 115, 130, 123, 119, 122, 127,
123, 118)
After - (112, 114, 107, 120, 115, 112,
112, 125)

H₀ - there is no significant difference in
weight

against H₁ = the diet program reduce
weight

Sal h \rightarrow $x = c(120, 125, 155, 130, 123, 119, 120,$
 $117, 128, 118)$

γx

(2) 120 125 155 130 123 119 120, 127 128 118

$\Sigma g = c(147, 114, 107, 120, 115, 112, 112, 120, 119, 118)$

$t + t_{\alpha/2} (n, 4)$ paired = 7, alternative = "less"
paired + - test

data and y

$t = 3.0792$, $df = 9$, p-value = 0.0032

alternative hypothesis: true difference in
means is less than 0 95% confidence
interval

- INF 19.62252

Some estimate:
mean of diff

12.3

Q6) Sample A = 66, 67, 75, 76, 82, 84, 88, 90, 92
 Sample B = 64, 66, 70, 72, 85, 87, 92, 93, 95, 97
 Test the Population mean are equal or not.

Q6) following are

$$\bar{x}_1 = \frac{1}{10} (66 + 67 + 75 + 76 + 82 + 84 + 88 + 90 + 92)$$

$$\bar{x}_2 = \frac{1}{10} (64 + 66 + 74 + 82 + 85 + 87 + 92 + 93 + 95 + 97)$$

$$[1] 66\ 67\ 75\ 76\ 82\ 84\ 88\ 90\ 92$$

$$[2] 64\ 66\ 74\ 82\ 85\ 87\ 92\ 93\ 95\ 97$$

$$t + \text{test}(x, y)$$

t

$$t = 0.63968, \text{ df} = 7, \text{ pvalue} = 0.5304$$

95 percent confidence interval

$$-12.8359 \quad 6.85399$$

mean of x	mean of y
80	83

\therefore the pvalue is greater than 0.05 we

accept

$$H_0: \mu_1 = \mu_2$$

5% level of significance

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Q.6] Following are the marks and before and after of a training program test the Program is effective or not

Before : 71, 72, 74, 69, 70, 74, 74, 70, 73, 75

After : 74, 77, 74, 73, 79, 76, 82, 72, 75, 78

H_0 = No significant differences in marks

H_1 the test Program increases the mark

$\mu_n = \bar{x} (71, 72, 74, 69, 70, 74, 76, 70, 73, 75)$

$\mu_y = \bar{x} (73, 77, 74, 73, 79, 76, 82, 72, 75, 78)$

t-test (μ_1, μ_2 , paired = T, alternative = "greater")

$t = -4.4691$ df = 9, pvalue = 0.9992.

95 percent of confidence interval

-5.076639

mean of the differences

= 3.6.

The Pvalue is greater than 0.05, we accept H_0 = no increase in marks at 5% level of significance.

AM

Topic: → Large and small sample test.

- 1.] The arithmetic mean of a sample of 100 items from a large population is 52 if the SD is 7 Test the hypothesis that the population mean is 55 against the alternative it is more than 55 at 5%. LOS level of significance.
- 2.] In a big city 350 out of 700 males are found to be smokers. Test this info - support that exactly half of the males in the city are smokers? test at 1%. LOS.
- 3.] Thousand articles from a factory A are found to have 2% defectives. 1500 articles from a second factory B are found to have 1% defective. Test that 5% of LOS. That the 2 factories are similar or not.
- 4.] A sample of size 400 was drawn and the sample mean is 99 test of 5%. LOS that the sample comes from a population with mean 100 and Variance 69?
- 5.] The flower stems are selected and the heights are found to be (cm) 63, 63, 68, 69, 71, 71, 72, Test the hypothesis that the mean height is 66 at 1% of 1% LOS.
- 6.] Two random samples were drawn from two normal populations and the values are
 A:-> 66, 67, 75, 76, 83, 84, 88, 90, 92
 B:-> 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97

Q3

Test whether the population have the same Variance at 5% LOS.

Solution:->

$H_0: \sigma_1^2 = \sigma_2^2$ against $H_1: \sigma_1^2 \neq \sigma_2^2$

I.] $n = 200$

$$\bar{m}_1 = 52$$

$$\sigma_m = 55$$

$$\sigma_{sd} = 7$$

$$z_{\text{cal}} = (\bar{m}_1 - \mu_0) / (\sigma_{sd} / \sqrt{n})$$

$$z_{\text{cal}}$$

$$[1] -4.285719$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$\text{pvalue}$$

$$[1] 1.82153e-05$$

Pvalue is < 0.05 we reject

(2) $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$

$$\alpha_p = 0.5$$

$$\bar{P} = 350/700$$

$$\bar{D}$$

$$(1) 0.5$$

$$\bar{n} = 700$$

$$\bar{\sigma} = 2 - P$$

$$\bar{\sigma}$$

$$[1] 0.5$$

$$z_{\text{cal}} = (\bar{P} - P) / (\sigma / \sqrt{n})$$

$$s_{\text{cal}}$$

[30]

$$z_{p\text{value}} = 2 * (\text{1} - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

[31]

pvalue > 0.05 we accept

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[32] $n_1 = 1000$

[33] $n_2 = 1500$

[34] $p_1 = 20 / 1000$

[35] $p_2 = 20 / 1500$

$$p_p = (n_1 * p_1 + n_2 * p_2) / (n_1/n_2 + 1/n_2)$$

[36]

$$z_{\text{cal}} = (p_1 - p_2) / \sqrt{p_p * q * (1/n_1 + 1/n_2)}$$

[37]

[38] 2.082731

$$z_{p\text{value}} = 2 * (\text{1} - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

[39]

[40] 0.03727577

Since pvalue < 0.05

∴ we reject pvalue.

1) $8n = 400$

$\bar{x}_{\text{max}} = 99$

$\bar{x}_{\text{min}} = 100$

$\Rightarrow \text{Variance} = 64$

$\Rightarrow \text{SD} = \sqrt{\text{Variance}}$

$\Rightarrow \text{SD}$

[1] 8

$\Rightarrow z_{\text{test}} = (\text{mean} - \mu_0) / (\text{SD} / \sqrt{n})$

$\Rightarrow z_{\text{test}}$

[1] -2.5

$\Rightarrow p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{test}})))$

$\Rightarrow p\text{value}$

[1] 0.01241933

Since $p\text{value} < 0.05$

\therefore we reject $H_0: \mu_1 = \mu_2$

5) $\gg x = c(62, 63, 68, 69, 71, 71, 72)$

$t\text{-test}(x)$

One Sample t-test

data: x

$\bar{x} = 67.54$, $df = 6$, $p\text{value} = 5.522e-09$

alternative hypothesis: true mean is not equal to
0

95% CI: Confidence Interval:

64.66479 73.62092

Sample estimate
mean of x

65.14286

p-value is < 0.05 we reject

$H_0: \mu_2 = \mu_1$ against $H_1: \mu_2 \neq \mu_1$

$$\bar{x}_1 = C(66, 67, \dots, 90, 92)$$

$$\bar{x}_2 = C(64, 66, \dots, 95, 97)$$

$\rightarrow F = \text{var}(x_1) / \text{var}(x_2)$

ZF

F test to compare two Variances

data: x1 and x2

F = 0.70686, num df = 8, denom df = 10, p-value = 0.8359

alternative hypothesis: true ratio of variances is not equal

$$\lambda = 1$$

95 percent confidence interval:

0.1833662

3.0360393

Sample estimated

~~AM~~
~~17.2%~~

Ratio of variance

~~0.7068567~~

$H_0: \mu_2 = \mu_1$ against $H_1: \mu_2 \neq \mu_1$

$\therefore \text{p-value} > 0.05$ we accept

$H_0: \mu_1 = \mu_2$

Practical 10.

Anova and chi squares

Use the following data to test whether the cleanliness of home and cleanliness of child are independent or not.

Cleanliness of child

Clean	Clean	Dirty
Fairly Clean	70	50
Fairly Dirty	80	20
Dirty	35	45

H_0 : CC & CH

$\tau x = c(20, 80, 35, 50, 20, 45)$

τn

[1] 20 80 35 50 20 45

$\tau m = 3$

$\tau n = 2$

$\tau y = \text{matrix}(x, \text{ncol} = m, \text{nrow} = n)$

τy

[1,1] [1,2]

[1,1] 20 50

[2,1] 80 20

[3,1] 35 45

$\tau pr = \text{chisq.test}(y)$

τpr

pearson's chi-squared test

data: y

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$$\chi^2 = 48.82, \text{ df} = 2, \text{ p-value}$$

Q. 2.] Use the following data to find if Vaccination and Particular disease are independent or not

Soln ->

		AFF	Not AFF
VGC	Given	20	30
	Not Given	25	35

Soln -> H_0 : Vaccination and disease are independent

$$x = c(20, 25, 30, 35)$$

> x

$$[1] 20 25 30 35$$

> m = 2

> n = 2

> y = matrix(x, nrow = m, ncol = n)

> y

	[1,1]	[1,2]
[1,1]	20	30
[1,2]	25	35

> pr = chisq.test(y)

> pr

Pearson Chi-squared test with
Yates's continuity correction.

data = y

χ^2 -squared = 0, df = 3, p-value = 1

Q.3.] Perform Anova for following data

Varieties	Observations
A	50, 52
B	53, 55, 53
C	50, 58, 57, 56
D	52, 54, 54, 55

Soln \rightarrow H_0 : Mean of the Varieties are equal

> $x_1 = c(50, 52)$

> $x_2 = c(53, 55, 53)$

> $x_3 = c(60, 58, 57, 56)$

> $x_4 = c(52, 54, 54, 55)$

> d = stack (list (b1 = x1, b2 = x2, b3 = x3, b4 = x4))

> d

	Values	ind
1	50	b1
2	52	b4
3	53	b2
4	55	b2
5	53	b2
6	60	b3
7	58	b3
8	57	b3
9	56	b3

10	52	b4
11	54	b4
12	54	b4
13	55	b4

names (d)

[1] "values" "ind"

? oneway.test (values ~ ind, data=d, var.equal=T)
 One-way analysis of means
 data: values and ind

F = 11.735, num df=3, denom df=9, p-value =
 0.001

? anova = aov (values ~ ind, data=d)

? anova

call:

aov (formula = values ~ ind, data=d)

Terms:

	ind	residuals
--	-----	-----------

Sum of squares	71.06410	18.1664
Deg of freedom	3	9

Residual Standard error: 1.420746
 estimated effects may be unbalanced

∴ p-value is less than 0.005
 we reject H₀

Q.4] The following data gives life of tree

Type	Observations
A	20, 23, 18, 17, 18, 22, 24
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 16

Test the hypothesis average life of four branches are same

Soln → H_0 : the average life of all branches are same

$$\sum x_1 = C(20, 23, 18, 17, 18, 22, 24)$$

$$\sum x_2 = C(19, 15, 17, 20, 16, 17)$$

$$\sum x_3 = C(21, 19, 22, 17, 20)$$

$$\sum x_4 = C(15, 14, 16, 18, 16)$$

$$d = \text{stack}(\text{list}(b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 = x_4))$$

d

	Values	Ind
1	20	b1
2	23	b1
3	18	b1
4	17	b2
5	18	b1
6	22	b1
7	24	b1
8	21	b2
9	19	b2
10	22	b2

11	17	b2
12	20	b2
13	15	b2
14	14	b3
15	22	b3
16	17	b3
17	20	b3
18	15	b4
19	14	b4
20	16	b4
21	18	b4
22	14	b4
23	16	b4
24		

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, names(cd)

[1] "values" "ind"

>oneway •t est (values ~ ind, data=d, var.equal=T)
one-way analysis of means

data: values and ind

F = 6.8445, num df=3 denom df=20, p-value =
0.00234

?anova = aov (values ~ ind, data=d)

?anova

Call:

aov (formula = values ~ ind, data=d)

Terms	Residuals
Sum of Squares	91.4381 84.0619
Deg of freedom	3 20

Sum of Squares

Deg of freedom

Residual Standard Error: 2.110236

estimated effects may be unbalanced
if the P-value is less than 0.005 we
reject the null hypothesis.

Q5.] 2000 students of a college are graded
accordingly to their IQ and economic condition
of home check that is there any association
between their economic of house and they are
IQ?

IQ

EC	High	Low
High	460	140
Md		
Medium	330	200
Low	240	160

Soln \rightarrow H_0 : EC & IQ are independent

$x = c(460, 330, 240, 140, 200, 160)$

$m = 3$

$n = 2$

$y = \text{matrix}(x, nrow = m, ncol = n)$

y

	[1,1]	[1,2]
[1,1]	460	140
[1,2]		
[1,3]	330	200
[1,4]	240	160

$\chi^2_{PV} = \text{chisq.test}(y)$

χ^2_{PV}

pearson's chi-squared test

data : y

χ^2 squared = 39.926 , df = 2, p-value = $2.364e^{-09}$
Since p-value is less than 0.005 we reject
 H_0 : CC & CP are independent.

Practical 11:Non-Parametric Test

Q1] Following are the amounts of Sulphur oxide emitted by industries in 20 days apply sign test to test the hypothesis that Population median is 21.5?

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26.

H_0 : population median is 21.5

> $x = c(17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26)$

> $sp = \text{length}(x[x > \text{median}])$

> sp

> $c(17, 9)$

> $sp = \text{length}(x[x < \text{median}])$

> sn

> $c(1) 11$

> $n = sp + sn$

> n

> $c(1) 20$

> $pr = \text{pbinom}(sp, n, 0.5)$

[1] 0.4219015

∴ P value is greater than 0.059
we accept the Value at 5% level of Significance.

Q2] Apply sign test hypothesis that population median 6:5 against alternative is greater than 6:5 at 1% los? 90

612, 619, 632, 628, 643, 640, 655, 649, 670, 670,

663.

Soln \rightarrow H₀ the Alternative is greater than

$y_n = CC(612, 619, 632, 628, 643, 640, 655, 649, 670, 670,$

663)

median = 24

$s_p = \text{length}(x[x > \text{median}])$

~~s_p~~

[1] 10

~~$s_n = \text{length}(x[x < \text{median}])$~~

~~s_n~~

[1] 10

~~$s_h = s_p + s_n$~~

~~s_h~~

[1] 20

$p_{pv} = p\text{binom}(s_n, n, 0.1)$

~~p~~

[1] 0.9999993

Q.3.] 10 Observations are 36, 32, 21, 30, 24, 25, 20, 22, 20, 18.
 Using sign test hypothesis that population median is 25 against alternative is less than 25 at 5% level of significance?

Soln $\rightarrow x = c(36, 32, 21, 30, 24, 25, 20, 22, 20, 18)$
 $\hat{\gamma}_{\text{median}} = 25$
 $\hat{\gamma}_{\text{sp}} = \text{length}(\mathbf{x}[\mathbf{x} > \text{median}])$
 $\hat{\gamma}_{\text{sn}} = \text{length}(\mathbf{x}[\mathbf{x} < \text{median}])$
 $\hat{\gamma}_n = \hat{\gamma}_{\text{sp}} + \hat{\gamma}_{\text{sn}}$
 $\hat{\gamma}_n$
 $[1] 8$
 $\hat{\gamma}_{\text{PV}} = \text{pbinom}[\hat{\gamma}_{\text{sp}}, n, 0.5]$
 $\hat{\gamma}_{\text{PV}}$
 $[2] 0.3632813$

Q.4.] The following are some measurements 63, 65, 60, 89, 61, 71, 58, 52, 69, 62, 63, 39, 72, 65 using wilcoxon signed rank test. Test the hypothesis that population median is 60 against alternative it is greater than 60, at 5% loss?

Soln $\rightarrow H_0$: population median is 60
 $\hat{\gamma}_x = c(63, 65, 60, 89, 61, 71, 58, 52, 69, 62, 63, 39, 72, 65)$
 $\rightarrow \text{wilcox.test}(x, alt = \text{"greater"}, mu = 60)$
 wilcoxon sign rank test with continuity correction
 data: x

$$V = 48.5, p\text{-value} = 0.9232$$

alternative hypothesis: true location is less than 60.

15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26.
use wilcoxon test to test hypothesis that population median is 20 against alternative is lesser than 20.

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$x = c(15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26.)$
wilcox.test(x)

wilcoxon signed rank test with continuity correction
data: x

V = 48.5, p-value = 0.9232

alternative hypothesis: true location is less than 20.

16) 20, 25, 27, 30, 18 test the hypothesis that population median is 25 against alternative is not less than 25?

$x = c(20, 25, 27, 30, 18)$

wilcox.test(x, alt = "two.sided", mu = 25)
wilcoxon signed rank test with continuity correction.

data: x

PA 3.20

V = 3.5, p-value = 0.7127937
alternative hypothesis: true location is not equal to 25.