

Subset sum problem is as follows:-

→ Given some natural numbers w_1, w_2, \dots, w_n and a target number W , is there a subset of $\{w_1, w_2, \dots, w_n\}$ that adds up to W ?

example:-

Let the set be $\{3, 34, 4, 12, 5, 23\}$

$W = 9$

$\Rightarrow \{4, 5\}$ is a subset which adds up to 9

We can use dynamic programming to solve this problem.

We will create a 2D array ^{Mat} of size $(n+1) \times (W+1)$ of bool type. The state $Mat[i][j]$ will be true if there exists a subset of elements from $\{w_1, \dots, w_i\}$ with sum value = 'j'.

The pseudocode for recursion is as follows:-

if $(w[i] > j)$
 $Mat[i][j] = Mat[i-1][j]$

else
 $Mat[i][j] = Mat[i-1][j] \text{ or } Mat[i-1][j-w[i]]$

This means that if current element has value greater than 'current sum value' we will copy answer from previous case

And if The current sum value is greater than the 'ith' element we will see if any of previous states have already experienced the sum = 'j' on any previous states experienced a value 'j - ~~w~~ (i)' which will solve our purpose.

Now is a simulation:-

W Set = {3, 4, 5, 2, 5} W = 6

Mat \Rightarrow

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|---|---|---|---|---|---|---|---|
| 0 | T | F | F | F | F | F | F |
| 3 | T | F | F | T | F | F | F |
| 4 | T | F | F | T | T | F | F |
| 5 | T | F | F | T | T | T | F |
| 2 | T | F | T | T | T | T | T |