2.9.18

AI25BTECH11002 - Ayush Sunil Labhade

Question:

Find the volume of a cuboid whose edges are given by $-3\hat{\imath} + 7\hat{\jmath} + 5\hat{k}$, $-5\hat{\imath} + 7\hat{\jmath} - 3\hat{k}$ and $7\hat{\imath} - 5\hat{\jmath} - 3\hat{k}$.

Solution: Given:

Point	Vector
a	$\begin{pmatrix} 3 \\ 7 \\ 5 \end{pmatrix}$
b	$\begin{pmatrix} -5 \\ 7 \\ -3 \end{pmatrix}$
c	$\begin{pmatrix} 7 \\ -5 \\ -3 \end{pmatrix}$

TABLE I: Given data

To find volume we need to compute $[a\ b\ c]$ We will compute by finding the determinant of $[a\ b\ c]$:

$$\mathbf{D} = \begin{pmatrix} a & b & c \end{pmatrix} \tag{1}$$

$$\mathbf{D} = \begin{pmatrix} 3 & -5 & -7 \\ 7 & 7 & -5 \\ 5 & -3 & -3 \end{pmatrix} \tag{2}$$

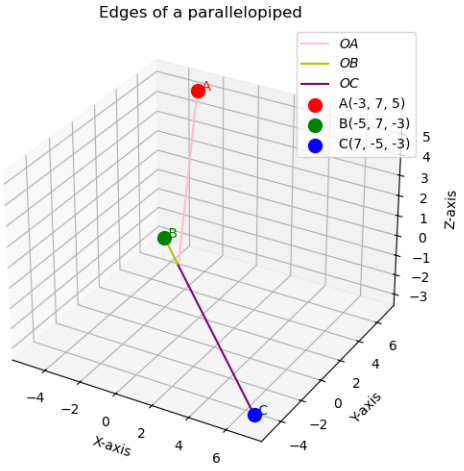
On computing,

$$det(\mathbf{D}) = 264 \tag{3}$$

$$\therefore [a\ b\ c] = 264 \tag{4}$$

Thus, the volume is 264.

Graph:


Edges of a parallelopiped
OA
OB
OC
A(-3, 7, 5)
B(-5, 7, -3)
C(7, -5, -3)
A
B
C
X-axis
Y-axis
Z-axis