

Off-line cursive handwritten word recognition using hidden Markov models

Davide Modolo and Thijs Kooi

dmodolo@student.uva.nl, Thijs.Kooi@student.uva.nl

Abstract—Over the past decades, much research has been performed in the field of optical character recognition and where the research in recognizing typewritten words and handwritten isolated characters has given rise to a variety of robust methods, the recognition of cursive handwritten words remains a challenge. This paper describes a complete system for the off-line recognition of handwritten words, a task that does not furnish temporal information, and apply a hidden Markov model to estimate word probabilities. Preprocessing techniques are described, including segmentation and normalization of word images to give invariance to scale, slant, slope, and stroke thickness. Representation of the image is discussed and the skeleton and morphological features used are described. The system has been first tested on some simple word recognition tasks and subsequently on a larger dataset. Results confirm the correctness of the system, but they highlight few difficulties. These difficulties are fully described in the paper, and several ideas about how to solve them are presented.

I. INTRODUCTION

Even though contemporary communication seems to emphasize on electronic information exchange rather than pen and paper, we still encounter cursive reading and writing on a daily basis. In the pursuit of making our lives easier, computers may serve a purpose by mitigating laborious document transcription. For applications one can think of tasks such as automatically processing bank checks, various application forms and address lines on an envelope.

The field of optical character recognition (OCR) is a sub field of pattern recognition and computer vision and is concerned with this automatic casting of analogue character sequences to a digital mould. The area can be dichotomized into typewritten and handwritten character transcription, with the latter further split into on-line and off-line recognition. In the case of on-line recognition, the path of the pen is followed, thereby providing efficacious data about the nature of the character and the technique can be applied in devices that make use of a touch screen of some kind. On the other hand, off-line handwritten word recognition does not incorporate the temporal dimension, rendering it harder but consequently more widely applicable. Despite ongoing academic attention, and the availability of successful commercial systems for typewritten and isolated characters, cursive character recognition remains a formidable challenge.

Over the past decades, researchers have performed in-depth studies of different fields of the recognition pipeline, however, no consensus has been reached as to what is the most effective method at each stage. The overall routine however, seems to follow the same pattern. In the first stage,

the image of the word or document is pre-processed and typically normalized. The second stage generally involves feature extraction, followed by the use of some pattern recognition technique. Although many methods make use of a hidden Markov model (HMM) [?], [?] to parametrize the character or word distributions, alternatives have been researched. Artificial neural networks (ANN) are commonly combined with the HMM [?] to model, for example, the probability of a character, given a certain observation. Schomaker [?], applies an ANN in the form of a Kohonen self-organizing map to model cursive script. An extended mean shift clustering method has proved to be successful in clustering Japanese characters in a high-dimensional space [?]. Rather than statistical modelling, a form of edit distance was used by Park and Govindaraju [?] to characterize words.

Instead of character and word classification, an OCR system can also focus on writer identification [?], [?], which has applications in forensic science and to identify users of a system. The normalization of observations we would perform in the recognition task is omitted and the key idea is now to focus on salient writer-specific traits.

In this paper we will take a bird eye view of the whole OCR pipeline, without overly scrutinizing specific stages. We will apply different pre-processing methods to segment sentences and words and normalize the characters. Rudimentary features will subsequently be extracted from the acquired images and we will use a sliding window to obtain observation sequences. To classify the words, we will make use of the HMM and will experiment with different parameters and observation distributions in the attempt to optimize recognition performance. The methods will first be tested on simple recognition tasks and subsequently in a more realistic setting with a larger dictionary.

This paper is outlined as follows. In sec. ??, we will describe an overview of the typical OCR pipeline, followed by details about the pre-processing in sec. ?. Sec. ? will subsequently cover the feature extraction, followed by a brief description of the HMM in sec. ?. Sec. ? will cover the experimental setup and results acquired and we will finish with a conclusion and discussion in section ?.

II. OVERVIEW

As mentioned before, the typical OCR pipeline has different stages: pre-processing, feature extraction and classification, each touching different fields of research and providing its own challenges. The pre-processing stage mainly entails image processing, whereas in the feature extraction and

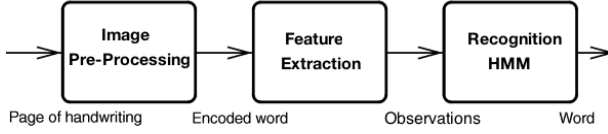


Fig. 1. A schematic of the recognition system.

classification stage, machine learning methods are more dominant. The pipeline is depicted in figure 1. In the following sections we will elaborate on the different aspect of this system and point out the challenges encountered along with the attempts to solve these.

III. PRE-PROCESSING

Several general pre-processing steps are done on the composite raw image before word recognition starts. These steps attempt to normalize the image as much as possible. It is assumed that the image has been binarized from grey scale. A pipeline of the preprocessing is shown in Fig. ??, and in the next subsections we will briefly describe all the steps involved. It is worth to note that in the presented pipeline skew and slant correction steps are applied both to lines and individual words. The repetition is useful to first obtain a good word segmentation, and to then obtain a good estimation of the baselines on single words.

A. Line Segmentation

Line segmentation is used to divide text of document into individual lines for further preprocessing. Line segmentation works on the assumption that the lines of the text are relatively horizontal. First, a histogram of black pixels of the image in the y direction is generated and smoothed with a median filter, where median filtering is used to remove insignificant minima and maxima; and then, cuts are made at significant local minima (often 0).

B. Skew Correction

The skew correction procedure rotates the text line such that the line on which the words are written becomes horizontal. For this purpose two steps are applied. First, the skew angle is estimated. Second, the input image is rotated by the estimated skew angle. To estimate the skew the lowest black pixel in every column are determined, and the set P defined as:

$$P = \{p_i = (x_i, y_i) | \text{lowest black pixel in column } x_i\} \quad (1)$$

Once P is populated, a least-squares linear regression is computed to find a line on the form $y = ax + b$ to fit as baseline of the input line. Then, the rotation angle is computed as $\theta = \arctan(a)$, as the image is rotated by $-\theta$ to remove the skew.

C. Slant Correction

The goal of slant correction is to bring the handwriting into an upright position. Depending on the writing style, the handwriting (especially its long vertical strokes) is more or

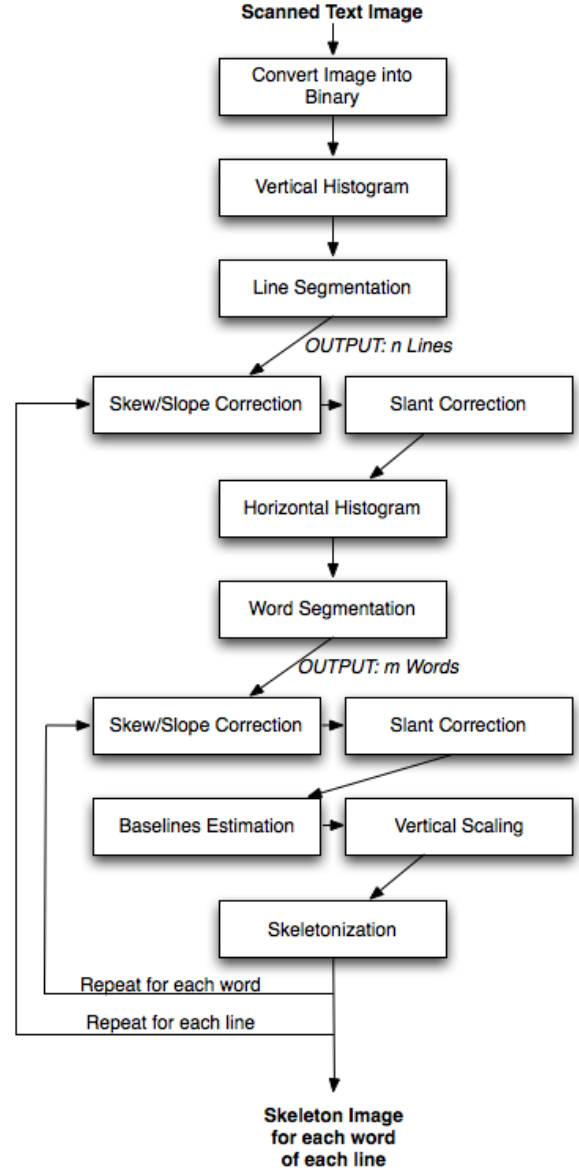


Fig. 2. Our pipeline of the preprocessing part of the system.

less slanted to the right or to the left. Similar to the skew correction, two steps are applied to remove the slant. First, the slant angle is estimated from the image. Second, an affine transformation with the estimated slant angle brings the handwriting into an upright position. The slant is estimated by finding the average angle of near-vertical strokes. First, the contour of the thresholded image is found, and a chain of connected pixels representing the edges of stroke is obtained. Second, the mode orientation of those edges close to the vertical is used as overall slant estimate.

D. Word Segmentation

Word segmentation is used to split lines into individual words, again, for further preprocessing. Word segmentation is not always straight-forward. Gaps between words are generally expected to be larger than gaps between characters

in a word. This however, is not necessarily true. Variations are ordinary and ligatures and flourish often cause larger geometric gaps to appear small, resulting in improper word segmentation [?]. A neural network could be used to intelligently segment words, but in our implementation we used a slightly less robust, but significantly faster approach. First, all the white spaces in y direction in the line are estimated, where a white space is defined as one or more (consecutive) columns of zero black pixels. Then, k-means clustering is performed on the white spaces with $k = 2$ to separate significant divisions (white spaces between words) from insignificant divisions (white spaces between characters).

E. Baselines Estimation

Four horizontal lines (ascender, upper, lower and descender - ordered from the top to the bottom) must be fit to the line of text for proper scaling and, later, recognition. Determining the upper and lower baselines is rather trivial, and can be done using linear regression as explained in skew subsection. Upper black pixels of each column are used to determine the upper baseline, and lower black pixels are used to determine the lower baselines. Ascender and descender baselines can be estimated respectively as the first y non-zero value and the last y non-zero value on the vertical histogram of the line. Once the baselines are estimated the input line can be horizontally divided into three parts, the descender part, the middle part, where the body of the text is located, and the ascender part. The rest of the image (above the ascender baseline and below the descender baseline) is discarded.

F. Vertical Scaling

In this step, the three regions defined in the previous subsection, are scaled to a predefined height. This normalization makes the feature extraction more robust because the location of the handwriting is correlated to the corresponding characters. Some characters, e.g. *a* or *e*, are entirely written in the middle part, whereas upper-case letters and characters like *l* and *t* also involve the ascender part.

G. Skeletonization

Before passing the image to the recognition system, the image has to become a skeleton. The image is first smoothed by convolution with a 2-dimensional Gaussian filter to remove noise and to correct some handwritten mistakes (e.g. the bottom loop of the letter *g* is not complete and it misses few pixels). Next, an iterative, erosive, thinning algorithm is applied to reduce the stroke in the writing to the width of a pixel. The obtained image is called the skeleton of the word.

IV. FEATURE EXTRACTION

After pre-processing, a feature extraction method is applied to capture the most relevant characteristic of the word to recognize. As in most machine learning and pattern recognition tasks, feature extraction is of vital importance; a highly complex recognition model will yield poor results if features are not selected properly.

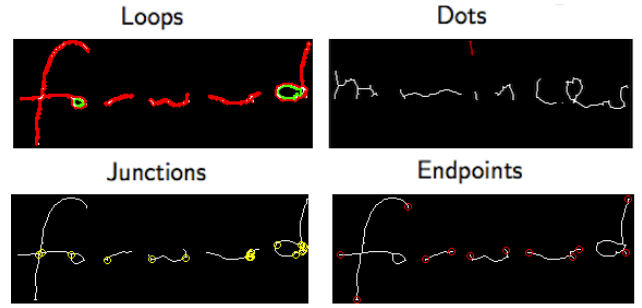


Fig. 3. Example of morphological features.

All the features are extracted from the skeleton of the image obtained after the pre-processing step of the pipeline. In our implementation we mainly focused on two types of features: statistical and morphological. The former only represent low-level information about the word, and they are based on the percentage of black pixels in the three regions of the word: ascender, middle and descender, respectively. The latter represent salient information about the word. They are often more discriminative, and have been found to reduce the error rate significantly [?]. Those features are:

- **Dots:** Dots above the letters 'i' and 'j' can be identified as short, isolated strokes occurring in the ascender part of the word.
- **Junctions:** Junctions occur where two strokes meet or cross and are easily found in the skeleton as points with more than two neighbors.
- **Endpoints:** Endpoints are points in the skeleton with only one neighbor and they mark the ends of strokes.
- **Loops:** Loops are found from connected-component analysis on the skeleton, to find areas of background color not connected to the region surrounding the word.

Each of the features above could be encoded as a single number, the total number of occurrences, but as it is also useful to know whether, for instance, a loop or a dot is present in a particular frame, the positions of the dots, junctions, endpoints and loops are also stored.

To extract the above mentioned features from the image, a sliding window is applied, thereby creating a sequence of related feature vectors, one for each position of the sliding window. This has the advantage that it relieves the pain of explicitly segmenting the letters in the word, but on the other hand gives rise to two more parameters, the width and interval of the window. In order to exploit the sequential nature of the observations, we need a model that does not treat the data as i.i.d. This is provided by the *hidden Markov model* (HMM) [?], [?], a generative classifier, widely applied in areas such as speech and gesture recognition and computational linguistics.

V. HIDDEN MARKOV MODELS

The HMM can be understood from different perspectives. It bears strong resemblance to the finite state automaton and

can essentially be seen as a specific type of graphical model. Moreover, researcher acquainted with the POMDP formalism will see familiar aspects. An HMM can be formally described by:

- A set of N states $S = (s_1, s_2, \dots, s_N)$, where the state of the system at time t is denoted q_t
- A set of priors $\pi = (\pi_1, \pi_2, \dots, \pi_N)$, providing the probability $P(q_1 = s_i)$.
- A transition function \mathbf{A} , where $a_{ij} = P(q_{t+1} = s_j | q_t = s_i)$.
- An observation function \mathbf{B} , mapping each observation at every state to a probability $b_i(\mathbf{o}_t) = P(\mathbf{o}_t | q_t = s_i, \lambda)$, where λ denotes the model parameters.

The model is trained to estimate the posterior probability $P(\mathbf{O}|\lambda)$ of an observation sequence $\mathbf{O} = (\mathbf{o}_1, \mathbf{o}_2, \dots, \mathbf{o}_T)$, with D -dimensional observation vectors $\mathbf{o}_t = (o_1, o_2, \dots, o_D)$. We assume time to be discrete and the transition and observation probabilities to be static. The hyper parameters we have to concern ourselves with are the network topology, i.e., the number of states and the transition probability and choice of the observation or emission probability function. In general, the exact state sequence remains hidden, hence the name *hidden* Markov model. The Markov property describes the dependency relation between subsequent data points. For speech and handwriting recognition a left-to-right model is generally applied, as show in figure 1, though variations exist.

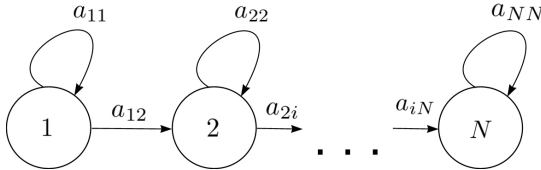


Fig. 4. Illustration of a simple left-to-right model

The three main problems to be solved for this model architecture are:

- 1) The probability of an observation sequence, given the model, $P(\mathbf{O}|\lambda)$.
- 2) The most likely state sequence, underlying a given observation sequence and the model, $Q^* = \max P(Q|\mathbf{O}, \lambda)$.
- 3) The most likely parameters of the model $\lambda^* = \max P(\lambda|\mathbf{O})$, given a training set of M observation sequences $X = (\mathbf{O}_1, \mathbf{O}_2, \dots, \mathbf{O}_M)$.

The third problem is solved by the Viterbi algorithm, but will not be needed for our particular task. A naive way to address the first problem of estimating the posterior probability of an observation sequence, would be to simply marginalize over all possible state sequences \mathbf{Q} and evaluate their probability. Unfortunately, the cardinality of \mathbf{Q} increases exponentially with the number of observations, rendering the method $\mathcal{O}(N^T)$ and thereby infeasible for all but the smallest models.

Luckily, an alternative exists in the form of the *forward-backward* algorithm, a special instance of the *sum-product* algorithm.

A. Forward-backward algorithm

The forward-backward algorithm is an efficient way of computing the probability of an observation sequence, given the model. The forward probability, is defined as the probability of a partial observation sequence $\mathbf{o}_1, \mathbf{o}_2, \dots, \mathbf{o}_t$ ending in state i at time t , $P(\mathbf{o}_1, \mathbf{o}_2, \dots, \mathbf{o}_t | q_t = s_i, \lambda)$ and can recursively be computed as:

$$\alpha_t(i) = \left[\sum_{j=1}^N \alpha_{t-1}(j) a_{ij} \right] b_j(\mathbf{o}_t) \quad (2)$$

A schematic illustration of the computation is provided in figure 2.

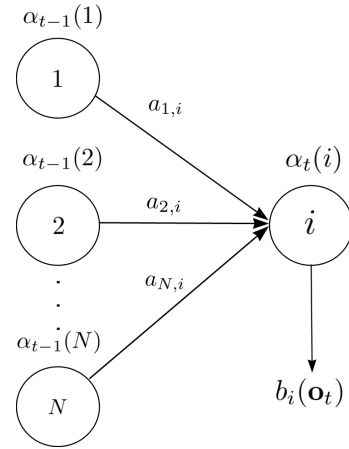


Fig. 5. Forward probability

The posterior probability of the observation sequence is subsequently calculated by summing over all possible end-states:

$$P(\mathbf{O}|\lambda) = \sum_{i=1}^N \alpha_T(i) \quad (3)$$

This holds a complexity of only $\mathcal{O}(N^2T)$, which is considerably less than the exponential time. Similarly, a backward probability is defined, which conveys the probability of observing the remaining data in state i at time t , $P(\mathbf{o}_{t+1}, \mathbf{o}_{t+2}, \dots, \mathbf{o}_T | q_t = s_j, \lambda)$ and can be efficiently computed according to:

$$\beta_t(i) = \sum_{j=1}^N a_{ij} b_j(\mathbf{o}_{t+1}) \beta_j(\mathbf{o}_{t+1}) \quad (4)$$

Although we do not need β for the computation of $P(\mathbf{O}|\lambda)$, it provides a comprehensible variable for the training of the model parameters, which is done by *Baum-Welch re-estimation*, a special instance of the EM-algorithm.

B. Baum-Welch re-estimation

To train the model, we need to maximize the likelihood of the parameters $\mathcal{L}(\lambda|\mathbf{O})$, by taking partial derivatives of every variable and setting it to zero. If we knew the probability of being in a state at a time step, we could analytically optimize the model parameters and if we knew the model parameters we could estimate the probability of being in a state at a time step. Therefore, we are presented with a chicken-or-egg problem and are left to the mercy of the EM algorithm, which iteratively computes and optimizes these values. For the left-to-right model, the probability of entering state 1, is initialized to 1 and therefore parameter π_i will remain fixed during the whole re-estimation procedure. To make the rest of the update steps more comprehensible, a set of intermediate variables is defined. First, the probability of begin in a state i at time step t , $P(q_t = s_i|\mathbf{O}, \lambda)$, which by Bayes' theorem and the before defined forward and backward probabilities can be written as:

$$\gamma_t(i) \equiv (P(\mathbf{O}|\lambda))^{-1} \alpha_t(i) \beta_t(i) \quad (5)$$

Where normalization constant $P(\mathbf{O}|\lambda) = \sum_{j=1}^N \alpha_t(i) \beta_t(i) = \sum_{j=1}^N \alpha_T(j)$. To estimate the transition probability between states, we also need the probability of being in a state at t and subsequently transitioning to another state, which is provided by:

$$\xi_t(i, j) \equiv (P(\mathbf{O}|\lambda))^{-1} \alpha_t(i) a_{ij} b_j(\mathbf{o}_t) \beta_t(j) \quad (6)$$

Where $\sum_{j=1}^N \xi_t(i, j) = \gamma_t(i)$. With these variables defined, we can easily and intuitively update the transition function, by marginalizing over all possible time steps:

$$\hat{a}_{ij} = \frac{\sum_{t=1}^{T-1} \xi_t(i, j)}{\sum_{t=1}^{T-1} \gamma_t(i)} \quad (7)$$

The update rules for the observation function depend on the distribution used.

C. Observation modeling

A common choice for an observation function is the Gaussian distribution. However, if we assume one state for every letter, a disadvantage in using a single Gaussian, is that for different writing styles of the same class, the Gaussian model might be trained to give the highest probability for a letter in between two instances. The intuition is illustrated in figure 3, where two different writing styles of an f are plotted in a two dimensional feature space. The Gaussian mixture model (GMM) conveys the following observation function:

$$b_j(\mathbf{o}_t) = \sum_{k=1}^K w_k \mathcal{N}(\mathbf{o}_t; \mu_{jk}, \Sigma_{jk}) \quad (8)$$

Where w_k denotes the prior probability of mixture component k , or weight of the mixture. In the case of a GMM, an additional latent variable, the weight of each mixture component, is introduced to the system and we need to adjust the E-step slightly:

$$\gamma_t(i, k) \equiv \gamma_t(i) \frac{b_{i,k}(\mathbf{o}_t)}{b_i(\mathbf{o}_t)} \quad (9)$$

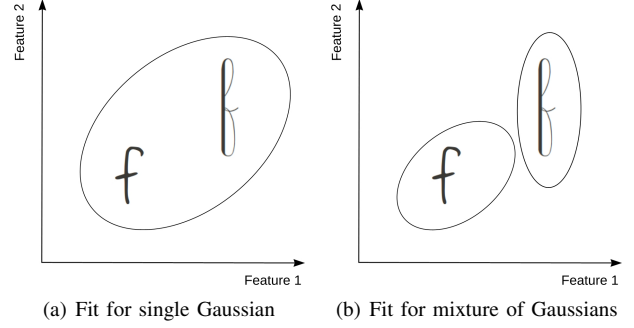


Fig. 6. Intuition behind the Gaussian mixture model

The new mixture weights at each iteration are now computed according to:

$$\hat{w}_{i,k} = \frac{\sum_{t=1}^T \gamma_t(i, k)}{\sum_{t=1}^T \gamma_t(i)} \quad (10)$$

The new mean is computed by:

$$\hat{\mu}_{i,k} = \frac{\sum_{t=1}^T \gamma_t(i, k) \mathbf{o}_t}{\sum_{t=1}^T \gamma_t(i, k)} \quad (11)$$

And the covariance is updated as:

$$\hat{\Sigma}_{i,k} = \frac{\sum_{t=1}^T \gamma_t(i, k) (\mathbf{o}_t - \mu_{i,k})(\mathbf{o}_t - \mu_{i,k})^T}{\sum_{t=1}^T \gamma_t(i, k)} \quad (12)$$

Please note that the update rules for a single Gaussian can easily be derived by setting K to 1.

The GMM introduces a number of additional hyper parameters, such as the number of mixture components and the shape of the covariance matrix, resulting in extra difficulties optimizing the system. Another issue of concern is the possibility of singular covariances, or extremely dense masses of probability, centered around a specific feature. This can in part be circumvented by implementation tricks, such as random reinitialization if the matrix is near singular, but feature dimensions that plainly convey no variance should be filled with some random noise in order to make the HMM do its job properly. Since we are working with features such as dots and loops, this is a highly likely scenario, considering not all words contain these characteristics and for the same reason, we do want to keep these features, as they are typically distinctive. The next section will cover experiments with these trade-offs and different parameters settings. We will return on the some of these issues in the discussion.

VI. EXPERIMENTS

The pipeline described has been entirely implemented in MATLAB due to the flexibility of its Image Processing Toolbox, and its power in matrix operations. In the next subsections we will present some experiments with it. The first experiment (Subsec. ??) aims at showing the performance of the skew and slant steps of the preprocessing pipelines. They are two fundamental steps, and their correctness is vital for the rest of the recognition system. The second

experiment (Subsec. ??) was done to test the correctness of the pipeline and to analyze the variation of the log likelihood between words. To keep the recognition system as easy as possible, in the experiment we used two words at a time and we performed *one vs one* recognition. Finally, the third experiment (Subsec. ??) will show some results obtained using the pipeline on a bigger dataset.

For the first experiment we personally collected a small data set of words with different level of variation in skew and slant. In the other two experiments, a small portion of the *IAM Handwriting Database*¹ was used. The IAM Handwriting Database contains forms of handwritten English text which can be used to train and test handwritten text recognizers and to perform writer identification and verification experiments. The database was first published in [?] at the ICDAR 1999, and a new version - the one used in these experiments - was released in 2004 [?]. The database contains forms of unconstrained handwritten text, which were scanned at a resolution of 300dpi and saved as PNG images with 256 grey levels.

A. Skew and Slant experiments

In Fig. ?? and Fig. ?? we show some example of skew and slant correction, respectively. To prove the flexibility of our approaches we tested them on words that differ in level of skew/slant, as well as in stroke, size and source (author). Despite all these variations, the approaches show to perform properly and to be general to different input.

B. One vs one word recognition

As previously described, to test whether the system was working or not, we performed one vs one word recognition.

We initially tried two simple typewritten words, *letter* and *number* described by only intensity features. The width of the sliding window was set to 3 and the interval to 1, so that consecutive windows overlap. The images were first pre-processed according to the methods described and an HMM with N states and K component GMM is trained for every word. Random noise of 20% is added to possibly empty feature dimensions. A sample from a test set of the word *letter* is subsequently fed to each model, to get the log-likelihood. Results are shown in the first line of Table ?. As we can see, the system gives an higher log-likelihood of 121.68 to the correct word. However, the second word also get a pretty high log-likelihood value of 106.36, and it happens because intensity features are not discriminative enough. The other rows of the table shows results of experiments on the same data using different parameters and all the features described in Sec. ?. As we can see, the log-likelihood is now really high for the correct word, and relatively small for the wrong one, confirming the discriminative power of the morphological features. For all the experiments we both trained and tested the model 40 different times and averaged the log-likelihood values.

¹<http://www.iam.unibe.ch/fki/databases/iam-handwriting-database/iam-handwriting-database>

ORIGINAL IMAGE	AFTER SKEW CORRECTION

Fig. 7. Experiments on the skew correction approach used in the preprocessing pipeline.

ORIGINAL IMAGE	AFTER SLANT CORRECTION

Fig. 8. Experiments on the slant correction approach used in the preprocessing pipeline.

TABLE I
Log-likelihood - Typewritten words

Features	N	K	Letter	Number	Diff.
Intensity	6	1	121.68	106.36	15.32
All	6	1	795.45	14.08	781.37
All	1	1	602.22	-90.02	692.22
All	6	3	226.96	-820.30	$1.04e^3$
All	6	1, diag. cov.	871.16	531.27	487.75
All	6	1, isotr. cov.	-179.00	-272.23	197.35

Next, to see how the system performs on actual hand-written data, we again took two words of the same length, namely *before* and *people*, from the IAM database. The models were trained on 25 instances and tested on 5. Again this process is repeated 40 times and log-likelihoods are averaged over these runs. Results for different parameter settings are provided in Table ???. Against our expectations, the system fails in recognizing the correct word, even though log-likelihood values are pretty high for both models. This is probably happening because the words *before* and *people* shares several letter, and they have loops more or less at the same positions. We expect to avoid this misclassification increasing the number of features.

TABLE II
Log-likelihood - Handwritten words

N	K	<i>before</i>	<i>people</i>	Diff.
6	1	$1.17e^3$	$1.19e^3$	480.16
1	1	699.56	$1.01e^3$	422.78
12	1	$1.44e^3$	$1.60e^3$	661.02
6	1, diag. cov.	$1.21e^3$	$1.41e^3$	521.20

During testing we experienced difficulty recognizing words of different length: long words are typically classified correctly, but short words are often wrongly classified as longer words. In the attempt to find optimal parameters and circumvent this problem, we performed the one-vs-one recognition on the short word *At* and the long word *Government*. Similar to previous experiments we feed observations from the first word to both HMMs and test different parameters. Since we are dealing with words of different length, the number of states per letter is denoted, rather than the actual number. Results are shown in Table ??. As expected, the long word *Government* obtained, in general, much higher log-likelihood values than the short word *At*. However, it is worth to note that using an HMM with 1 state and a GMM with 1 component the short word *At* achieved a slightly higher log-likelihood than the long word *Government*. The difference is so small that could be considered almost insignificant, however, it confirms our assumption that optimizing the parameters could solve the difficulty in recognizing words with short length.

TABLE III
Log-likelihood - Short versus long words

N	K	<i>At</i>	<i>Government</i>	Diff.
1	1	$2.79e^3$	$2.42e^3$	368.77
2	1	421.61	$3.31e^3$	$2.89e^3$
1	1, diag. cov.	373.88	$3.04e^3$	$2.67e^3$

For both of the previous previous two experiments other parameter settings where attempted, but resulted in singularity problems.

C. All vs all words recognition

To finally observe the performance of the system on a real dataset, we extracted the most frequent 200 words from the IAM Handwriting Database. Given the long time taken by training and testing the HMMs, the reduction of the dataset was needful. Different experiments with different values for number of states N and number of gaussian components K have been performed. Results are shown in Table ??. The last 3 columns of the table show the accuracy achieved on retrieving the correct words in the first one, three and five positions in rank, respectively. As we can see, the accuracy of the system when considering correct the words retrieved as first in the rank list is pretty low, but it increases pretty fast as soon as we consider a word correct if it appears in the top 5 of the ranked list. Again, we expect to considerably increase the accuracy extracting more features that will help in better discriminate between words. A cumulative match curve (CMC) is show in Fig. ??

TABLE IV
Log-likelihood - Small dataset of 200 words

N	K	Acc. 1	Acc. 2	Acc. 5
lengthWord	1	0.2400	0.3400	0.51
1	1	0.2000	0.3600	0.52
1	5	0.0800	0.1800	0.34
lengthWord	5	0.1200	0.3000	0.45

VII. DISCUSSION

From the experiments we can conclude that every aspect of the pipeline works. The experiments with slant, slope and skew correction clearly show improvement, albeit lack of quantification. The experiments performed on the typewritten words show that the feature extraction is performing well, clearly outperforming basic intensity features, but experiments performed on handwritten words clearly show that the features are too few to properly discriminate similar words. Moreover, we have proven the HMM to work correctly, since all instances of the typewritten words yield a higher log-likelihood for the correct word than the wrong one. There is room for improvement however.

One of the biggest problems we encountered in working with the HMMs where singularity related. As can be seen from the tables in the previous section, the log-likelihood is extremely high, which is presumably caused by probability

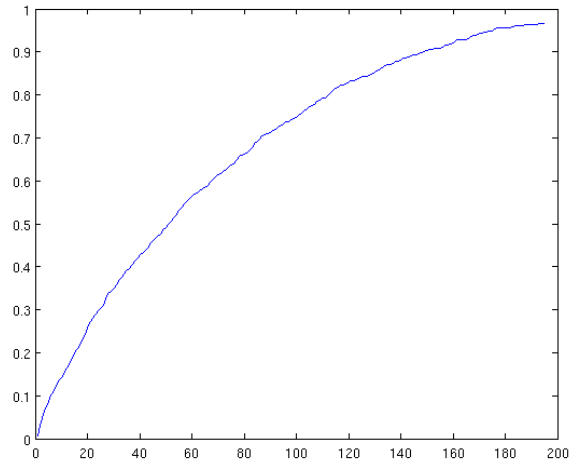


Fig. 9. Cumulative match curve (CMC) for the dataset. On the x axis we have the 200 words and on the y axis the percentage of retrieved data.

mass centered around a specific location in the feature space. A careful inspection of the trained HMMs confirms this hypothesis. Our attempted solutions where adding noise to the dataset and adjusting the shape of the covariance matrix, to decrease the ability to fit the data. This, however, was to no avail and in some cases even worsened results.

Another hurdle we faced was the apparent inability of the system to correctly classify short words. We suspect this to have different causes: (1) short words are more likely to be subject to writing variations, as described in Sec. ?? and (2) when computing the posterior probability of an observation sequence, the most likely path might end halfway in the state sequence, since longer words generally contain shorter words within them. We tried to prevent the first problem by using the Gaussian mixture model, described earlier. This, however, did not improve results and caused a lot of singularity problems. A different solution may lay in the explicit modeling of duration in the HMMs [?][?]. In this approach, the forward-backward algorithm is enhanced by a probability distribution over the duration of a given state, i.e., the number of times the model returns to the current state. This way, we can place a lower and upper bound on the number of permitted re-entries by setting the rest to zero, thereby ensuring an observation sequence is spread out over the complete state space. This method, however, does convey extra parameter fitting during the learning phase and additional hyper parameters to tweak, but it is definitely worth to try.

The assumption that a character is stationary over a number of observations may be false. Even though some features like loops output 1, whenever a loop is present in the window, other features do output continuous values and violate this assumption. In the experiments, we have tried to model more states per character, but this does not seem to improve results. Literature appears inconclusive about the number of states to use per letter; some researcher prefer

to use a single letter for every state and some model 3 or more for each character. This will most likely depend on the feature set used, but some clear research into this topic might reveal regularities.

The system contains many parameters and the properly optimizing of a considerable part of these has been omitted, due to time limitations. The results show a large difference between parameter settings, however, and therefore we suspect that the system can drastically be improved, given the right amount of time to optimize all of them. We suspect the feature extraction stage to be another bottleneck, mainly the lack in quantity. More and different features might prevent some of the overfitting and singularity problems we had.

VIII. CONCLUSION

A full working pipeline for an off-line word recognition system as been implemented and described in this paper. Few problems encountered during the implementation of the system were addressed, and some ideas about how to solve them are described. Different experiments were presented and the results confirmed the correctness of the pipeline. Despite this positive results, the system has shown to have a large margin of increment. Future work should focus on the optimization of the high number of parameters of the HMM, as well as on the extraction of more features. Moreover, it would be interesting to use of a language model as an extra post-processing step.

REFERENCES

- [1] Haikal El Abed and Volker Margner. Comparison of different preprocessing and feature extraction methods for offline recognition of handwritten arabicwords. *Document Analysis and Recognition, International Conference on*, 2:974–978, 2007.
- [2] H. Bunke, M. Roth, and E.G. Schukat-Talamazzini. Off-line cursive handwriting recognition using hidden markov models, 1995.
- [3] Horst Bunke, M. Roth, and Ernst Günter Schukat-Talamazzini. Off-line cursive handwriting recognition using hidden markov models. *Pattern Recognition*, 28(9):1399–1413, 1995.
- [4] A. P. Dempster, N. M. Laird, and D. B. Rubin. Maximum likelihood from incomplete data via the EM algorithm. *Proceedings of the Royal Statistical Society*, B-39:1–38, 1977.
- [5] Salvador Espana-Boquera, Maria Jose Castro-Bleda, Jorge Gorbe-Moya, and Francisco Zamora-Martinez. Improving offline handwritten text recognition with hybrid hmm/ann models. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 99(RapidPosts), 2010.
- [6] John T. Favata. Offline general handwritten word recognition using an approximate beam matching algorithm. *IEEE Transactions on Pattern Analysis and Machine Intelligence (PAMI)*, 23:200–1, 2001.
- [7] Alex Graves, Marcus Liwicki, S. Fernandez, Roman Bertolami, Horst Bunke, and Jürgen Schmidhuber. A novel connectionist system for unconstrained handwriting recognition. *IEEE Trans. Pattern Anal. Mach. Intell.*, 31(5):855–868, 2009.
- [8] Gyeonghwan Kim, Venu Govindaraju, and Sargur N. Srihari. An architecture for handwritten text recognition systems. *International Journal on Document Analysis and Recognition*, 2:37–44, 1999. 10.1007/s100320050035.
- [9] U.-V. Marti and H. Bunke. A full english sentence database for off-line handwriting recognition. In *Proceedings of the Fifth International Conference on Document Analysis and Recognition, ICDAR '99*, pages 705–, Washington, DC, USA, 1999. IEEE Computer Society.

- [10] U. V. Marti and H. Bunke. The IAM-database: an English sentence database for offline handwriting recognition. *Int. Journal on Document Analysis and Recognition*, 5:39–46, 2002.
- [11] Urs-Viktor Marti and Horst Bunke. Using a statistical language model to improve the performance of an HMM-based cursive handwriting recognition system. *IJPRAI*, 15(1):65–90, 2001.
- [12] J. Park and V. Govindaraju. Using lexical similarity in handwritten word recognition. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition (CVPR-00)*, pages 290–295, Los Alamitos, June 13–15 2000. IEEE.
- [13] L. R. Rabiner and B. H. Juang. An introduction to hidden markov models. *ASSP Magazine*, pages 4–16, January 1986.
- [14] Lawrence R. Rabiner. A tutorial on hidden Markov models and selected applications in speech recognition. *Proceedings of the IEEE*, 77(2):257–286, 1989.
- [15] Andreas Schlapbach and Horst Bunke. A writer identification and verification system using HMM based recognizers. 2007.
- [16] L. Schomaker. Using stroke or character-based self-organizing maps in the recognition of on-line, connected cursive script. *Pattern Recognition*, 26(3):443–450, March 1993.
- [17] L. Schomaker. Advances in writer identification and verification. In *ICDAR*, pages 1268–1273, 2007.
- [18] R. Seiler, M. Schenkel, and F. Eggimann. Off-line cursive handwriting recognition compared with on-line recognition. In *In Proc. Int. Conference on Pattern Recognition (ICPR)*, pages 505–509, 1996.
- [19] Andrew W. Senior and Anthony J. Robinson. An off-line cursive handwriting recognition system. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 20:309–321, 1998.
- [20] László Tóth and András Kocsor. Explicit duration modelling in HMM/ANN hybrids. In Václav Matousek, Pavel Mautner, and Tomás Pavelka, editors, *TSD*, volume 3658 of *Lecture Notes in Computer Science*, pages 310–317. Springer, 2005.
- [21] T. Wakahara and K. Ogura. Extended mean shift in handwriting clustering. In *ICPR*, pages Vol I: 384–388, 1998.
- [22] Shun-Zheng Yu and Hisashi Kobayashi. Practical implementation of an efficient forward-backward algorithm for an explicit-duration hidden markov model. *IEEE Transactions on Signal Processing*, 54(5):1947–1951, 2006.