

## Assignment 7

### Q1. Polyglot Optimization

You are given a list of  $N$  projects. Each project requires proficiency in a certain set of languages. You are a polyglot programmer, skilled in a variety of languages, and can work on any project as long as you know all the required languages for that project.

Each project has a value associated with it, representing the reward or benefit of completing that project. You want to maximize your total reward by selecting a subset of projects such that for each project in the subset, you know all the required languages.

#### Input:

- An integer  $N$  representing the number of projects.
- An array values of size  $N$ , where values[i] is the value of the  $i$ -th project.
- A list of lists required\_languages of size  $N$ , where required\_languages[i] is a list of languages required for the  $i$ -th project.
- A set known\_languages containing the languages you know.

#### Output:

- The maximum total value of the projects you can complete.

#### Example:

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
int maxProjectValue(int N, vector<int>& values, vector<vector<string>>& required_languages, set<string>& known_languages) {  
    // Your dynamic programming solution goes here  
    return max_value;  
}
```

```
int main() {  
    int N = ;  
    vector<int> values = {50, 30, 70, 20, 90, 10, 60, 40, 80, 100};  
    vector<vector<string>> required_languages = {{ "Python", "C++", {"Java", "Python"}, {"C++", "Java", "Python"}, {"Python"}, {"Java", "Go"}, {"C++", {"Python", "Go"}, {"C++", "Python"}, {"Java", "Python", "Go"}, {"C++", "Java", "Go"}}, {"Python", "C++", "Java"};  
    int result = maxProjectValue(N, values, required_languages, known_languages);  
    cout << "Maximum Project Value: " << result << endl;  
    return 0;  
}
```

## Q2. Knapsack Problem

You are given a list of  $N$  items, each with a weight and a value. You have a knapsack that can hold a maximum weight  $W$ . Additionally, you have some constraints and additional features:

1. Each item may have a dependency on another item. If you include item  $i$ , you must also include its dependent item  $j$ .
2. Some items can be grouped into categories, and you can select at most one item from each category.
3. Each item can be taken multiple times, but only up to a maximum limit  $L[i]$  for item  $i$ .

Your task is to determine the maximum value you can achieve while respecting the knapsack's weight limit, the dependency constraints, the category constraints, and the item repetition limits.

### Input:

- An integer  $N$  representing the number of items.
- An integer  $W$  representing the maximum weight the knapsack can hold.
- An array `weights` of size  $N$ , where `weights[i]` is the weight of the  $i$ -th item.
- An array `values` of size  $N$ , where `values[i]` is the value of the  $i$ -th item.
- An array `dependencies` of size  $N$ , where `dependencies[i]` is the index of the item that  $i$ -th item depends on, or  $-1$  if there is no dependency.
- An array `categories` of size  $N$ , where `categories[i]` is the category of the  $i$ -th item.
- An array `limits` of size  $N$ , where `limits[i]` is the maximum number of times the  $i$ -th item can be taken.

### Output:

- The maximum value that can be achieved within the given constraints.

### Example:

```
#include <bits/stdc++.h>
using namespace std;

int knapsack(int N, int W, vector<int>& weights, vector<int>& values, vector<int>& dependencies, vector<int>& categories, vector<int>& limits) {
    // Your dynamic programming solution goes here
}

int main() {
    int N = 10;
    int W = 100;
    vector<int> weights = {10, 20, 30, 40, 15, 25, 35, 45, 55, 50};
    vector<int> values = {60, 100, 120, 240, 150, 90, 200, 170, 250, 300};
    vector<int> dependencies = {-1, 0, -1, 2, -1, -1, 1, 4, -1, 7} // Items 1 depends on 0, 3 depends on 2, 6 depends on 1, 7 depends on 4, 9 depends on 7
    vector<int> categories = {1, 0, 0, 1, 2, 2, 3, 3, 4, 4} // Categories constrain the selection to at most one item per category
    vector<int> limits = {1, 2, 1, 1, 1, 1, 1, 1, 1, 1} // Maximum times each item can be taken
    int result = knapsack(N, W, weights, values, dependencies, categories, limits);
    cout << "Maximum Knapsack Value: " << result << endl;
    return 0;
}
```