

**VISVESVARAYA TECHNOLOGICAL
UNIVERSITY**
“JnanaSangama”, Belgaum -590014, Karnataka.



LAB REPORT

on

Artificial Intelligence (23CS5PCAIN)

Submitted by

Ayush Ranjan (1BM23CS058)

in partial fulfillment for the award of the degree of
BACHELOR OF ENGINEERING

in
COMPUTER SCIENCE AND ENGINEERING



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B.M.S. College of Engineering,
Bull Temple Road, Bangalore 560019
(Affiliated To Visvesvaraya Technological University, Belgaum)
Department of Computer Science and Engineering



CERTIFICATE

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **Ayush Ranjan (1BM23CS058)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

Sandhya A Kulkarni Assistant Professor Department of CSE, BMSCE	Dr. Kavitha Sooda Professor & HOD Department of CSE, BMSCE
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Github Link:

<https://github.com/AyushRanjan-58/AI>

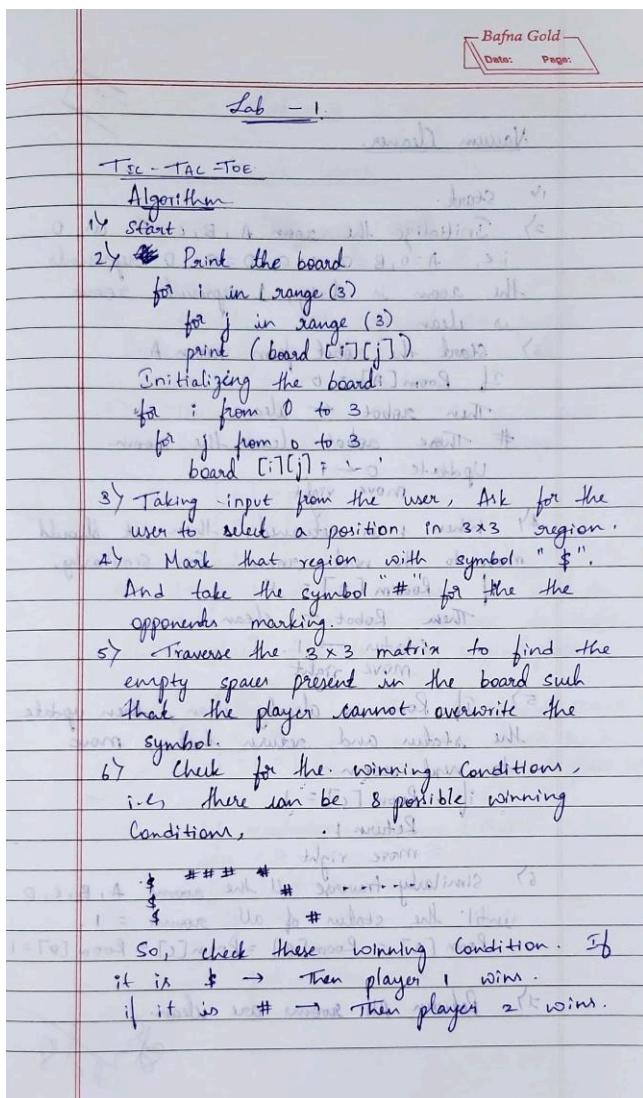
Program 1

Implement Tic – Tac – Toe Game

Implement vacuum cleaner

agent

Algorithm for Tic-Tac-Toe:



Code for Tic-Tac-Toe:

```
board={1:' ',2:' ',3:' ',
       4:' ',5:' ',6:' ',
       7:' ',8:' ',9:' '
     }

def printBoard(board):
    print(board[1] + '|' + board[2] + '|' + board[3]
          ) print('---')
    print(board[4] + ' |' + board[5] + ' |' +
          board[6]) print('---')
    print(board[7] + ' |' + board[8] + ' |' +
          board[9]) print('\n')

def spaceFree(pos):
    if(board[pos]==' '):
        return True
```

```
else:  
    return False  
  
  
def checkWin():  
    if(board[1]==board[2] and board[1]==board[3] and board[1]!=' '):  
        return True  
  
    elif(board[4]==board[5] and board[4]==board[6] and board[4]!=' '):  
        return True  
  
    elif(board[7]==board[8] and board[7]==board[9] and board[7]!=' '):  
        return True  
  
    elif (board[1] == board[5] and board[1] == board[9] and board[1] != ' '):  
        return True  
  
    elif (board[3] == board[5] and board[3] == board[7] and board[3] != ' '):  
        return True  
  
    elif (board[1] == board[4] and board[1] == board[7] and board[1] != ' '):  
        return True  
  
    elif (board[2] == board[5] and board[2] == board[8] and board[2] != ' '):  
        return True  
  
    elif (board[3] == board[6] and board[3] == board[9] and board[3] != ' '):  
        return True  
  
    else:  
        return False
```

```
def checkMoveForWin(move):
```

```
if (board[1]==board[2] and board[1]==board[3] and board[1] ==move):
    return True

elif (board[4]==board[5] and board[4]==board[6] and board[4] ==move):
    return True

elif (board[7]==board[8] and board[7]==board[9] and board[7] ==move):
    return True

elif (board[1]==board[5] and board[1]==board[9] and board[1] ==move):
    return True

elif (board[3]==board[5] and board[3]==board[7] and board[3] ==move):
    return True

elif (board[1]==board[4] and board[1]==board[7] and board[1] ==move):
    return True

elif (board[2]==board[5] and board[2]==board[8] and board[2] ==move):
    return True

elif (board[3]==board[6] and board[3]==board[9] and board[3] ==move):
    return True

else:
    return False
```

```
def checkDraw():
    for key in
        board.keys(): if
            (board[key]==''):
                return False
```

```
return True
```

```
def insertLetter(letter, position):

    if (spaceFree(position)):

        board[position] = letter

        printBoard(board)

        if (checkDraw()):

            print('Draw!')

        elif (checkWin()):

            if (letter == 'X'):

                print('Bot wins!')

            else:

                print('You win!')

        return

    else:

        print('Position taken, please pick a different position.')

        position = int(input('Enter new position: '))

        insertLetter(letter, position)

    return

player = 'O'

bot ='X'
```

```
def playerMove():
    position=int(input('Enter position for
O:')) insertLetter(player, position)
    return
```

```
def compMove():
    bestScore=-100
    0 bestMove=0
    for key in
        board.keys(): if
            (board[key]==' '):
                board[key]=bot
                score = minimax(board, False)
                board[key] = ''
                if (score > bestScore):
                    bestScore = score
                    bestMove = key
    insertLetter(bot, bestMove)
    return

def minimax(board,
    isMaximizing): if
        (checkMoveForWin(bot)):
```

```
    return 1  
  
elif (checkMoveForWin(player)):
```

```
    return -1

elif (checkDraw()):
    return 0

if isMaximizing:
    bestScore = -1000

for key in board.keys():
    if board[key] == '':
        board[key] = bot
        score = minimax(board, False)
        board[key] = ''
        if (score > bestScore):
            bestScore = score
    return bestScore

else:
    bestScore = 1000

for key in board.keys():
    if board[key] == '':
        board[key] = player
        score = minimax(board, True)
        board[key] = ''
        if (score < bestScore):
            bestScore = score
```

```
bestScore = score  
return bestScore
```

while not checkWin():

compMove()

playerMove()

Algorithm for Vacuum Cleaner Agent:

Vacuum Cleaner.

1) Start.
2) Initialize the room A, B, C, D as 0
i.e., A=0, B=0, C=0, D=0. 0 represents the room is dirty, 1 represents room is clean.
3) Stand the robot from room A.
If Room[A] = 0
Then Robot \leftarrow clean.
Then robot clean the room.
Update 0 \leftarrow 1
move right.
4) When 1 is returned, then it should move to the next room. So, similarly,
if Room[B] = 0
Then Robot \leftarrow clean,
status \rightarrow 1
move right.
5) If Room is already clean, then update the status and return that; move to next room.
if Room[C] = 1
Return 1.
move right.
6) Similarly traverse all the rooms A, B, C, D until the status of all room = 1.
Room[A] = Room[B] = Room[C] = Room[D] = 1
7) Return All rooms are clean.

8/20/08

```
def vacuum_world():

    goal_state = {'A': '0', 'B':
        '0'}

    cost = 0

    location_input = input("Enter Location of Vacuum: ")

    status_input = input("Enter status of " + location_input + ": ")

    status_input_complement = input("Enter status of other room: ")

    print("Initial Location Condition: " + str(goal_state))

    if location_input == 'A':

        print("Vacuum is placed in Location A")

        if status_input == '1':

            print("Location A is Dirty.")

            goal_state['A'] = '0'

            cost += 1

            print("Cost for CLEANING A: " + str(cost))

            print("Location A has been Cleaned.")

    if status_input_complement == '1':

        print("Location B is Dirty.")
```

```
print("Moving right to Location B.")
```

```
cost += 1

print("COST for moving RIGHT: " + str(cost))

goal_state['B'] = '0'

cost += 1

print("COST for SUCK: " + str(cost))

print("Location B has been

Cleaned.")

else:

    print("Location B is already clean. No action.")

else:

    print("Location A is already

clean.") if status_input_complement

    == '1':


        print("Location B is Dirty.")

        print("Moving right to Location B.")

        cost += 1

        print("COST for moving RIGHT: " + str(cost))

goal_state['B'] = '0'

cost += 1

print("Cost for SUCK: " + str(cost))

print("Location B has been Cleaned.")

else:
```

```
print("Location B is already clean. No action.")
```

```
else:  
    print("Vacuum is placed in Location B")  
  
  
if status_input == '1':  
    print("Location B is Dirty.")  
  
  
    goal_state['B'] = '0'  
    cost += 1  
  
    print("COST for CLEANING B: " + str(cost))  
    print("Location B has been Cleaned.")  
  
  
if status_input_complement == '1':  
  
  
    print("Location A is Dirty.")  
    print("Moving left to Location A.")  
    cost += 1  
  
    print("COST for moving LEFT: " + str(cost))  
  
  
    goal_state['A'] = '0'  
    cost += 1  
  
    print("COST for SUCK: " + str(cost))  
    print("Location A has been Cleaned.")  
  
else:  
    print("Location A is already clean. No action.")
```

```
else:  
    print("Location B is already clean.")  
  
    if status_input_complement == '1':  
        print("Location A is Dirty.")  
  
        print("Moving left to Location A.")  
        cost += 1  
  
        print("COST for moving LEFT: " + str(cost))  
  
  
    goal_state['A'] = '0'  
  
    cost += 1  
  
    print("Cost for SUCK: " + str(cost))  
  
    print("Location A has been Cleaned.")  
  
else:  
    print("Location A is already clean. No action.")  
  
  
print("GOAL STATE: ")  
print(goal_state)  
print("Performance Measurement: " + str(cost))  
  
  
vacuum_world()
```

Program 2 :

Implement 8 puzzle problems using Depth First Search (DFS)

Implement Iterative deepening search algorithm

8 – puzzle usig DFS :

Algorithm :

3/1/25
Bafna Gold
Date: _____ Page: _____

Lab - 2

8 - Puzzle Game

Algorithm:

- 1) Start.
- 2) Initially, we represent the puzzle state using $[0, 1, 2, 3, 4, 5, 6, 7, 8]$, where $0 \leftarrow$ blank tile.
- 3) There will be a 3×3 grid and we need to arrange it in ordered way.
- 4) Using Manhattan distance, we need to calculate the minimum distance to shift the displaced tile to its original place.

0	1	2
3	4	5
6	7	8

i.e., (6, 1, 2)
(4, 0, 5)
(3, 7, 8)

So, (6, 1, 2) should move 2 places down & 3 should move 1 place up.

```
def manhattan_distance(state):  
    dist = 0  
    for i in range(9):  
        if state[i] == 0:  
            continue  
        goal_index = i - 1
```

N = 3

class PuzzleState:

def __init__(self, board, x, y, depth):

 self.board = board

 self.x = x

 self.y = y

 self.depth =

 depth

row = [0, 0, -1, 1]

col = [-1, 1, 0, 0]

def is_goal_state(board):

 goal = [[1, 2, 3], [4, 5, 6], [7, 8, 0]]

 return board == goal

def is_valid(x, y):

 return 0 <= x < N and 0 <= y <

N def print_board(board):

 for row in board:

 print(''.join(map(str, row)))

 print("")

def solve_puzzle_dfs(start, x,

 y): stack = []

 visited = set()

 stack.append(PuzzleState(start, x, y,

 0)) visited.add(tuple(map(tuple, start)))

```

while stack:

    curr = stack.pop()

    print(f'Depth: {curr.depth}')

    print_board(curr.board)

    if is_goal_state(curr.board):

        print(f'Goal state reached at depth {curr.depth}')

        return

    for i in range(4):

        new_x = curr.x + row[i]

        new_y = curr.y + col[i]

        if is_valid(new_x, new_y):

            new_board = [row[:] for row in curr.board]

            new_board[curr.x][curr.y], new_board[new_x][new_y] = new_board[new_x][new_y], new_board[curr.x][curr.y]

            board_tuple = tuple(map(tuple, new_board))

            if board_tuple not in visited:

                visited.add(board_tuple)

                stack.append(PuzzleState(new_board, new_x, new_y, curr.depth + 1))

    print('No solution found (DFS Brute Force reached depth limit)')

if __name__ == '__main__':

    start = [[1, 2, 3], [4, 0, 5], [6, 7, 8]]

    x, y = 1, 1

    print('Initial State:')

    print_board(start)

```

solve_puzzle_dfs(start, x,

y) 8-puzzle for IDS :

Pseudocode

- 1) Start
- 2) Initialize A* function,
function A-star (start, goal):
 open-set = priority queue().
 open-set.push (start, priority = heuristic (start)).
- 3) While open-set is non-empty,
 current = open-set.pop()
 if current = goal:
 return solution-path
- 4) for neighbour in neighbour (current):
 (g)
 tentative_g = g-score [current] + 1
 f = tentative_g + heuristic (neighbour).
 if neighbour not in g-score,
 g-score [neighbour] = tentative_g.
 f = tentative_g + heuristic (neighbour).
 open-set.push (neighbour, priority = f).
- 5) return no solution
- 6) Now arrange all the popped elements
 in the order way to get solution

```
N = 3

class PuzzleState:

    def __init__(self, board, x, y, depth):
        self.board = board
        self.x = x
        self.y = y
        self.depth = depth

    row_moves = [0, 0, -1, 1]
    col_moves = [-1, 1, 0, 0]

    def is_goal_state(board):
        goal = [[1,2,3],[4,5,6],[7,0,8]]
        return board == goal

    def is_valid(x, y):
        return 0 <= x < N and 0 <= y < N

    def print_board(self):
        for r in board:
            print(''.join(map(str, r)))
        print("")

def dfs_with_depth_limit(start, x, y, depth_limit):
    stack = []
```

```

visited = set()

stack.append(PuzzleState(start, x, y,
0)) visited.add(tuple(map(tuple, start)))

while stack:

    curr = stack.pop()

    print(f'Depth: {curr.depth}')

    print_board(curr.board)

    if is_goal_state(curr.board):

        print(f'Goal state reached at depth {curr.depth}')

        return True

    if curr.depth ==

        depth_limit: continue

    for i in range(4):

        new_x = curr.x + row_moves[i]

        new_y = curr.y + col_moves[i]

        if is_valid(new_x, new_y):

            new_board = [row[:] for row in curr.board]

            new_board[curr.x][curr.y], new_board[new_x][new_y] = new_board[new_x][new_y],
            new_board[curr.x][curr.y]

```

```
board_tuple = tuple(map(tuple, new_board))

if board_tuple not in visited:

    visited.add(board_tuple)

    stack.append(PuzzleState(new_board, new_x, new_y, curr.depth + 1))

return False

def iterative_deepening_search(start, x, y, max_depth=50):

    for depth in range(max_depth):

        print(f"Trying depth limit: {depth}")
        found = dfs_with_depth_limit(start, x, y, depth)
        if found:
            print(f"Solved at depth {depth}!")

return

print("No solution found within max depth

limit.") if __name__ == '__main__':

    start = [[1, 2, 3], [4, 0, 5], [6, 7, 8]]

    x, y = 1, 1

    print('Initial State:')

    print_board(start)

    iterative_deepening_search(start, x, y)
```

Pseudo code:

```

1) function DDFS (root, goal):
    depth = 0
    found = DLS (root, goal, depth)
    return true

loop → while true:
    2) function DLS (node, goal, limit):
        if node is null,
            return false
        if node == goal:
            return true
        if limit == 0:
            return false
        for each child in children (node):
            if DLS (child, goal, limit - 1) == true:
                return true
        return false
    
```

Solved ✓

Path → A → C → F → K.

```

4) max-depth (src):
    if (src == null):
        return 0
    L = max-depth (src.left),
    R = max-depth (src.right),
    
```

Problem 3:

Implement A* search algorithm

Algorithm:

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Algorithm

Consider,

- 1) `b bool DLS (src, target, limit):`
 - if (`src == target`) `return true;`
 - (`else return false;`)
- 2) If not, then in,
 - `src ← i` (any)
 - `if (DLS(i, target, limit)) return true.`
 - `return false.`
- 3) `bool IDDFS (src, target, max-depth)`
 - for limit 0 to max-depth.
 - `if DLS (src, target, max-depth).`
 - `return false.`

Tracking:

Code :

```
from copy import deepcopy
```

```
import heapq
```

```
GOAL_STATE = [
```

```
    [1, 2, 3],
```

```
    [4, 5, 6],
```

```
    [7, 8, 0]
```

```
]
```

```
DIRECTIONS =
```

```
    { 'up': (-1, 0),
```

```
     'down': (1, 0),
```

```
     'left': (0, -1),
```

```
     'right': (0, 1)
```

```
}
```

```
def print_state(state):
```

```
    for row in state:
```

```
        print(row)
```

```
        print('-' * 10)
```

```
def state_to_tuple(state):
```

```
    return tuple(tuple(row) for row in state)
```

```
def find_zero(state):
```

```
    for i in range(3):
```

```
        for j in
```

```
            range(3):
```

```
                if state[i][j] == 0:
```

```
                    return i, j
```

```
def move(state, direction):
```

```

x, y = find_zero(state)

dx, dy = DIRECTIONS[direction]

nx, ny = x + dx, y + dy

if 0 <= nx < 3 and 0 <= ny <

    3: new_state =

        deepcopy(state)

        new_state[x][y], new_state[nx][ny] = new_state[nx][ny], new_state[x][y]

        return new_state

    return None

def manhattan_distance(state):

    distance = 0

    for i in range(3):

        for j in

            range(3):

                value = state[i][j]

                if value != 0:

                    goal_x = (value - 1) // 3

                    goal_y = (value - 1) % 3

                    distance += abs(i - goal_x) + abs(j - goal_y)

    return distance

def a_star(start_state, goal_state):

    open_list = []

    g_score = {state_to_tuple(start_state): 0}

    f_score = {state_to_tuple(start_state): manhattan_distance(start_state)}

```

```
heappq.heappush(open_list, (f_score[state_to_tuple(start_state)], start_state, []))
```

```
visited = set()
```

```

iteration = 0

print("\nStarting A* Search...\n")

while open_list:

    iteration += 1

    _, current_state, path = heapq.heappop(open_list)

    print(f"Iteration {iteration}:")
    print_state(current_state)

    print(f"g(n): {len(path)}, h(n): {manhattan_distance(current_state)}, f(n): {len(path)} +"
          f" manhattan_distance(current_state)}")

    state_key = state_to_tuple(current_state)

    if state_key in visited:
        continue

    visited.add(state_key)

    if current_state == goal_state:
        print("Goal state reached!\n")
        return path + [current_state]

    for direction in DIRECTIONS.keys():

        new_state = move(current_state, direction)

        if new_state:
            new_key =
                state_to_tuple(new_state) if
                new_key not in visited:

                new_g = len(path) + 1
                new_f = new_g + manhattan_distance(new_state)
                heapq.heappush(open_list, (new_f, new_state, path + [current_state]))

```

```
print("No solution found.")

return None

if __name__ == "__main__":
    print("Enter the initial 3x3 puzzle state (use 0 for the blank):")

    initial_state = []

    for i in range(3):
        row = input(f"Row {i+1} (space-separated): ").strip().split()
        initial_state.append([int(num) for num in row])

    solution_path = a_star(initial_state, GOAL_STATE)

if solution_path:
    print("Solution Path (step-by-step):")

    for idx, state in enumerate(solution_path):
        print(f"Step {idx}:")
        print_state(state)

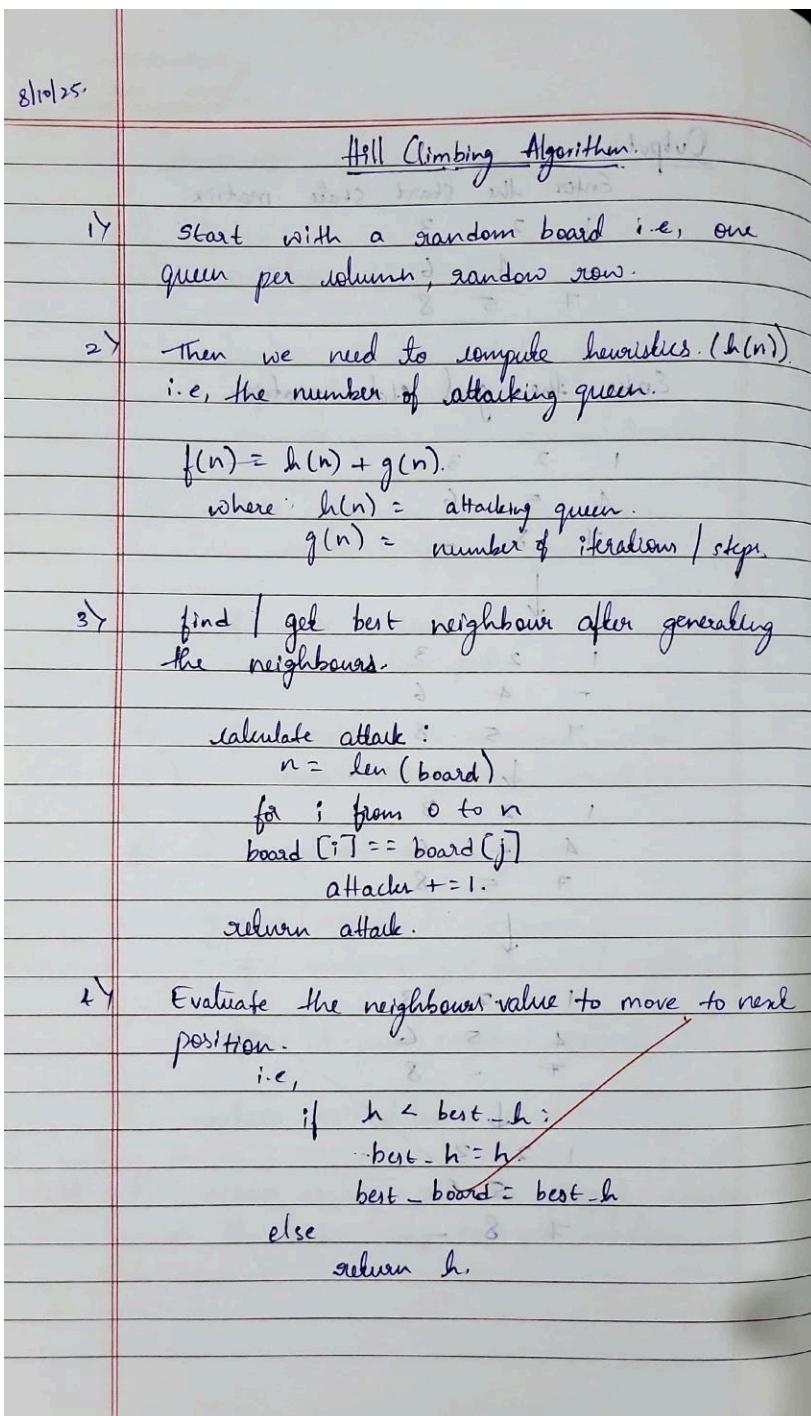
    print(f"Puzzle Solved in {len(solution_path) - 1} moves!")

else:
    print("Could not find a solution.")
```

Problem 4:

Implement Hill Climbing search algorithm to solve N-Queens problem

Algorithm:



Code :

```
import random

def calculate_conflicts(state):
    conflicts = 0
```

```
N = len(state)

for i in
    range(N):

    for j in range(i + 1, N):

        if state[i] ==

            state[j]:

                conflicts += 1

        if abs(state[i] - state[j]) == abs(i - j):

            conflicts += 1

    return conflicts

def get_neighbors(state):

    neighbors = []

    N = len(state)

    for col in range(N):

        for row in
            range(N):

                if state[col] != row:

                    new_state = state.copy()

                    new_state[col] = row

                    neighbors.append(new_state)

    return neighbors

def print_board(state):

    N = len(state)

    board = [".." for _ in range(N)] for _ in range(N)]
```

for col in range(N):

 board[state[col]][col] = "Q"

for row in board:

```
print(" ".join(row))

print()

def hill_climbing_nqueens(N=4):

    current_state = [random.randint(0, N - 1) for _ in range(N)]

    current_cost = calculate_conflicts(current_state)

    print_board(current_state)

    while True:

        if current_cost == 0:

            return current_state

        neighbors = get_neighbors(current_state)

        best_neighbor = min(neighbors, key=calculate_conflicts)

        best_cost = calculate_conflicts(best_neighbor)

        if best_cost >= current_cost:

            return current_state

        else:

            current_state, current_cost = best_neighbor, best_cost

            print_board(current_state)

solution = hill_climbing_nqueens(4)

print("Final Solution:", solution)

print("Conflicts:", calculate_conflicts(solution))
```

Problem 5:

Simulated Annealing to Solve 8-Queens problem

Algorithm:

8/10/2025.

Simulated Annealing.

1) Start

2) Initialize current-state & initial state.
Check for the temperature T .

Simulated annealing().
current \leftarrow initial-state.
 $T \leftarrow$ a large positive ~~large~~ value.

3) while $T > 0$
do,
next \leftarrow a random neighbour of
current.
 $\Delta E \leftarrow$ current-cost - next-cost.

4) if $\Delta E > 0$
 current \leftarrow next.
else
 current \leftarrow next with
 probability $= p \cdot e^{\frac{-\Delta E}{T}}$
 decrease T .

5) return current.

5) End / terminate.

OK
8/10/25

Code :

```
import random  
  
import math  
  
def random_state(n=8):  
  
    """Generate a random board: list of row positions for each column."""  
  
    return [random.randint(0, n - 1) for _ in range(n)]
```

```
def conflicts(state):
    """
    Number of attacking pairs of
    queens. Lower is better. A solution
    has 0.

    h = 0

    n = len(state)

    for i in
        range(n):

        for j in range(i + 1, n):

            if state[i] ==
                state[j]:

                h += 1

            if abs(state[i] - state[j]) == abs(i -
                j): h += 1

    return h

def
random_neighbor(state):
    """
    Create a neighbor by moving a queen in one random
    column to a random row.

    """

    n = len(state)

    new_state = state.copy()

    col = random.randint(0, n - 1)
```

```
row = random.randint(0, n - 1)
```

```
new_state[col] = row
```

```
return new_state

def simulated_annealing(max_steps=100000, n=8):

    current = random_state(n)

    current_cost = conflicts(current)

    T = 1.0

    cooling = 0.0001

    for step in

        range(max_steps): if

            current_cost == 0:

                return current, step

        T = max(T * math.exp(-cooling * step),

0.0001) next_state =

random_neighbor(current) next_cost =

conflicts(next_state)

delta = current_cost - next_cost

if delta > 0 or random.random() < math.exp(delta /

T): current = next_state

current_cost =

next_cost return None,

max_steps

solution, steps =

simulated_annealing() if solution:

    print(f"Solution found in {steps}

steps:") print("State:", solution)

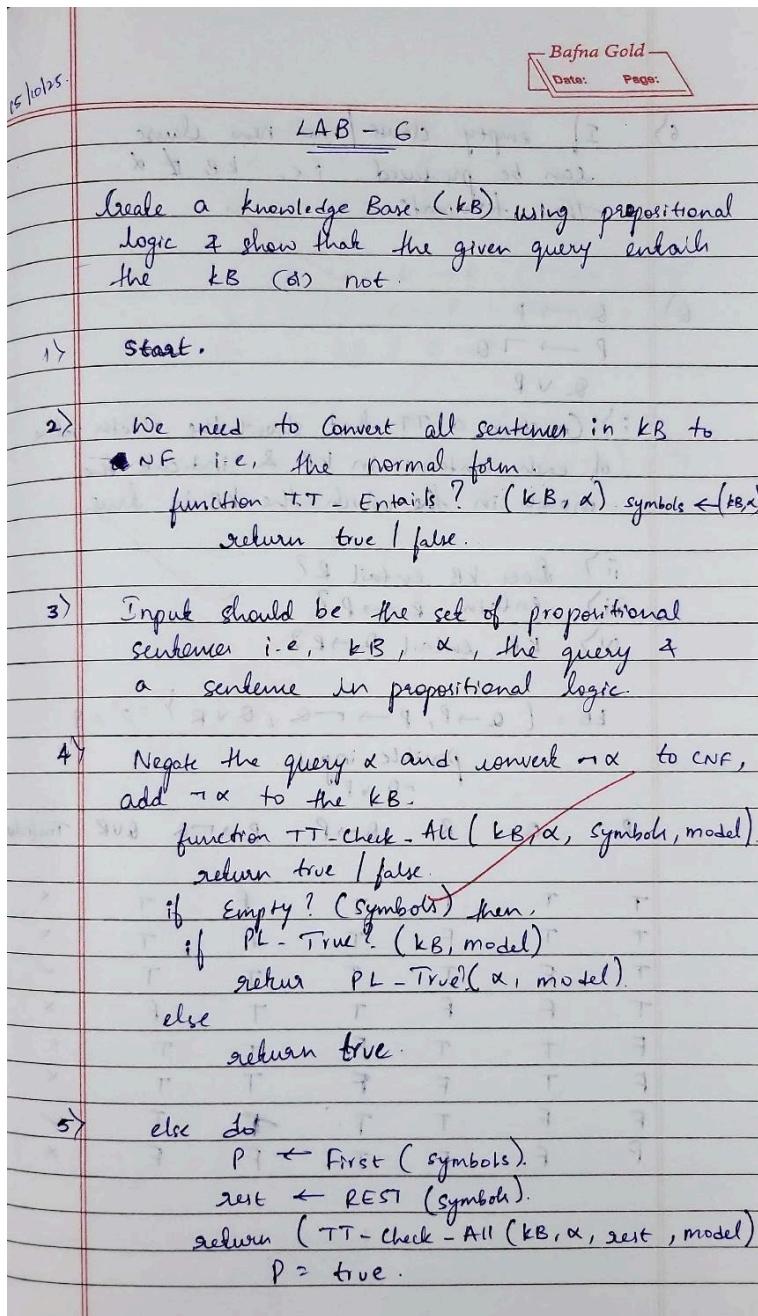
    print("Conflicts:", conflicts(solution))
```

```
else:  
    print("No solution found.")
```

Problem 6:

Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

Algorithm :



Code :

```
import itertools

class Formula:

    def __init__(self, symbols, expr):
        self.symbols = set(symbols)
```

```

self.expr = expr

def evaluate(self, model):
    return
    self.expr(model)

def get_all_symbols(kb, query):
    symbols = set()
    for f in kb + [query]:
        symbols |=
        f.symbols
    return sorted(symbols)

def entails(kb, query):
    symbols = get_all_symbols(kb, query)
    for values in itertools.product([False, True], repeat=len(symbols)):
        model = dict(zip(symbols, values))
        if all(f.evaluate(model) for f in kb):
            if not query.evaluate(model):
                print("Counterexample found:", model)
                return False
    return True

R_implies_W = Formula({"R", "W"}, lambda m: (not m["R"]) or m["W"])
S_implies_W = Formula({"S", "W"}, lambda m: (not m["S"]) or m["W"])
W_implies_L = Formula({"W", "L"}, lambda m: (not m["W"]) or m["L"])
C_implies_R = Formula({"C", "R"}, lambda m: (not m["C"]) or m["R"])
S_or_C = Formula({"S", "C"}, lambda m: m["S"] or m["C"])

```

```
S_equiv_D = Formula({"S", "D"}, lambda m: m["S"] == m["D"])
```

```
Query_L = Formula({"L"}, lambda m: m["L"])
```

```
KB = [
```

```
    R_implies_W,
```

```
    S_implies_W,
```

```
    W_implies_L,
```

```
    C_implies_R,
```

```
    S_or_C,
```

```
    S_equiv_D
```

```
]
```

```
result = entails(KB, Query_L)
```

```
print("\nDoes KB entail L (grass is slippery)? →", result)
```

Program 7:

Implement unification in first order logic

Algorithm:

Unification problem.

① $P(f(x), g(y), y)$
 $P(f(g(z)), g(f(a)), f(a))$

find Θ (MGU)

② $\Theta(x, f(x))$
 $\Theta(f(y), y)$

③ $\Theta(x, g(x))$
 $\Theta(g(y), g(g(z)))$

④ $f(x) = f(g(z)) \quad \left\{ \begin{array}{l} x \rightarrow g(z) \\ y \rightarrow f(a) \end{array} \right.$
 $x = g(z)$
 $g(y) = g(f(a))$
 $y = f(a)$

$y = f(a)$ ✓

The last 2 expression holds so,
unifiable.

2) $\Theta(x, f(x))$ no of arguments are same.
 $\Theta(f(y), y)$.
 $x = f(y)$.
 $f(x) = y$.

So, $f(x) = y$. but $f(x) = f(f(y))$

So, they are conflicts. does not hold
cannot be unified

Code :

```
def occurs_check(var,  
expr): if var == expr:
```

```
    return True  
  
elif isinstance(expr, list):
```

```
    return any(occurs_check(var, subexpr) for subexpr in expr)
return False
```

```
def unify(x, y,
          subst=None):
    if subst is None:
        subst = {}

    if isinstance(x, str) and
        x.islower():
        if x in subst:
            return unify(subst[x], y,
                         subst)
        elif occurs_check(x, y):
            return None
    else:
        subst[x] = y
        return subst

    elif isinstance(y, str) and
        y.islower():
        return unify(x, subst[y], subst)
    elif occurs_check(y, x):
        return None
    else:
```

subst[y] = x

```
return subst

elif x == y:
    return subst

elif isinstance(x, list) and isinstance(y,
list): if len(x) != len(y):
    return None

for xi, yi in zip(x, y):
    subst = unify(xi, yi,
    subst) if subst is None:
        return None

    return subst

else:
    return None

expr1 = ["Knows", "John", "x"]
expr2 = ["Knows", "y", "Mary"]

print("Expression 1:", expr1)
print("Expression 2:", expr2)
```

```
result = unify(expr1,  
expr2) if result:  
  
    for k, v in result.items():  
  
        print(f'{k} / {v}')  
  
else:  
  
    print("Unification failed.")
```

Program 8:

Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning:

Code :

```
from copy import deepcopy

def occurs_check(var, expr):
    if var == expr:
        return True
```

```
elif isinstance(expr, list):
    return any(occurs_check(var, subexpr) for subexpr in expr)
    return False

def substitute(expr, subst):
    if isinstance(expr, str):
        return subst.get(expr, expr)
    elif isinstance(expr, list):
        return [substitute(e, subst) for e in expr]
    return expr

def unify(x, y, subst=None):
    if subst is None:
        subst = {}
    if subst is
        None: return
    None
    if x == y:
        return
    subst
    elif isinstance(x, str) and
        x.islower(): if x in subst:
            return unify(subst[x], y,
    subst) elif occurs_check(x, y):
            return None
    else:
        subst[x] = y
```

```
    return subst  
  
elif isinstance(y, str) and y.islower():
```

```
    return unify(y, x, subst)

elif isinstance(x, list) and isinstance(y, list) and len(x) == len(y):

    for a, b in zip(x, y):

        subst = unify(a, b, subst)

    if subst is None:

        return None

    return subst

else:

    return None
```

```
def parse_sentence(sentence):

    """Parse sentence like 'Parent(John, x)' → ['Parent', 'John', 'x']"""

    sentence = sentence.strip()

    if '(' in sentence and ')' in sentence:

        pred = sentence[:sentence.index('(')]

        args = sentence[sentence.index('(') + 1:sentence.index(')').split(',')]

        args = [a.strip() for a in args]

        return [pred] + args

    else:

        return [sentence]
```

```
def to_string(expr):

    if len(expr) ==

        1:

            return expr[0]

    else:
```

```
return f'{expr[0]}({', '.join(expr[1:]))}'
```

```
def fol_fc_ask(KB, query):
    print("FORWARD CHAINING START ")
    print("Initial Knowledge Base:")
    for fact in KB:
        print(" ", fact)
    print("Query:", query)

iteration = 0
new = set()

while True:
    iteration += 1
    print(f"\n--- Iteration {iteration} ---")
    n_new = set()

    for rule in KB.copy():
        if "=>" in rule:
            premise, conclusion = rule.split("=>")
            premise = premise.strip()
            conclusion = conclusion.strip()
            premises = [p.strip() for p in premise.split("^")]
            print(f"\nChecking rule: {rule}")

            substitutions = []
```

```
for fact in KB:
```

```
    if "=>" not in fact:
```

```
        for p in premises:
```

```
            s = unify(parse_sentence(p), parse_sentence(fact))
```

```
            if s is not None:
```

```
                print(f" Premise '{p}' unified with fact '{fact}' using {s}")
```

```
                substitutions.append(s)
```

```
for s in substitutions:
```

```
    new_fact = to_string(substitute(parse_sentence(conclusion),
```

```
        s)) if new_fact not in KB and new_fact not in n_new:
```

```
        print(f"=> New fact inferred: {new_fact}")
```

```
        n_new.add(new_fact)
```

```
        phi = unify(parse_sentence(new_fact), parse_sentence(query))
```

```
        if phi is not None:
```

```
            print("\n Query proved!")
```

```
            print(f"Substitution set: {phi}")
```

```
            return phi
```

```
if not n_new:
```

```
    print("\nNo new inferences. Forward chaining ends.")
```

```
    print("Query cannot be proved.")
```

```
return False
```

```
print("\nNewly inferred facts this  
iteration:") for fact in n_new:  
    print(" ", fact)
```

```
KB |= n_new  
print("\nUpdated Knowledge Base:")  
for fact in KB:  
    print(" ", fact)
```

```
KB = {  
    "Parent(John, Mary)",  
    "Parent(Mary, Alice)",  
    "Parent(x, y) ^ Parent(y, z) => Grandparent(x, z)"  
}
```

```
query = "Grandparent(John, Alice)"
```

```
result = fol_fc_ask(deepcopy(KB), query)
```

Program 9:

Create a knowledge base consisting of first order logic statements and prove the given query using Resolution

Algorithm :

12/11/25 First Order Logic

Reduction is a theorem proving technique that proceeds by building refutation proof i.e., by contradiction.

1. Eliminate biconditional and implication:
i.e., replacing $(\alpha \rightarrow \beta) \wedge (\beta \rightarrow \alpha)$. $\leftrightarrow = \alpha \leftrightarrow \beta$
eliminate \rightarrow , replacing $\alpha \rightarrow \beta$ with $\neg \alpha \vee \beta$.
2. Move \neg inwards:
 $\neg (\forall x p) \equiv \exists x \neg p$,
 $\neg (\exists x p) \equiv \forall x \neg p$,
 $\neg (\alpha \vee \beta) \equiv \neg \alpha \wedge \neg \beta$,
 $\neg (\alpha \wedge \beta) \equiv \neg \alpha \vee \neg \beta$,
 $\neg \neg \alpha \equiv \alpha$.
3. Standardize variables apart by renaming them i.e., each quantifier should use a different variable.
4. Skolemize each existential variable is replaced by a skolem constant or skolem constant function of the enclosing universally quantified variables.
5. Drop Universal quantifiers.
6. Distribute \wedge over \vee :
 $(\alpha \wedge \beta) \vee \gamma \equiv (\alpha \vee \gamma) \wedge (\beta \vee \gamma)$.

Code :

```
import copy

def is_variable(x):
    return isinstance(x, str) and x[0].islower()
```

```
def unify(x, y, theta=None):
    if theta is None:
        theta = {}
    if theta == "FAIL":
        return "FAIL"
    elif x == y:
        return theta
    elif is_variable(x):
        return unify_var(x, y, theta)
    elif is_variable(y):
        return unify_var(y, x, theta)
    elif isinstance(x, list) and isinstance(y, list) and len(x) == len(y):
        return unify(x[1:], y[1:], unify(x[0], y[0], theta))
    else:
        return "FAIL"
```

```
def unify_var(var, x, theta):
    if var in theta:
        return unify(theta[var], x,
                    theta)
    elif x in theta:
        return unify(var, theta[x],
                    theta)
    else:
        if occurs_check(var, x, theta):
            return "FAIL"
        theta_copy = theta.copy()
```

```
theta_copy[var] = x
return theta_copy

def occurs_check(var, x, theta):
    if var == x:
        return True
    elif isinstance(x, list):
        return any(occurs_check(var, arg, theta) for arg in x)
    elif isinstance(x, str) and x in theta:
        return occurs_check(var, theta[x], theta)
    return False
```

```
def substitute(theta, clause):
    new_clause = []
    for pred in clause:
        name = pred[0]
        args = pred[1]
        new_args = [(theta[arg] if arg in theta else arg) for arg in args]
        new_clause.append([name, new_args])
    return new_clause
```

```
def resolve(ci, cj):
    resolvents = []
```

```
for pi in ci:
```

```
    for pj in
```

```
        cj:
```

```
            if pi[0] == "~" + pj[0] or pj[0] == "~" + pi[0]:
```

```
                theta = unify(pi[1], pj[1],
```

```
                {}) if theta != "FAIL":
```

```
                    ci_new = substitute(theta, [x for x in ci if x !=
```

```
                    pi]) cj_new = substitute(theta, [x for x in cj if x
```

```
                    != pj])
```

```
            resolvent = []
```

```
            for term in ci_new +
```

```
                cj_new: if term not in
```

```
                resolvent:
```

```
                    resolvent.append(term)
```

```
            resolvents.append(resolvent)
```

```
        return resolvents
```

```
def clause_to_hashable(clause):
```

```
    """
```

```
    clause = [["Pred", ["a", "b"]], ["~Q", ["x"]]]
```

$\rightarrow ((\text{Pred}, (\text{"a"}, \text{"b"})), (\text{"\sim Q"}, (\text{"x"},)))$

""""

return tuple((pred[0], tuple(pred[1]))) for pred in clause)

```
def hashable_to_clause(tup):
    """ reverse conversion """
    return [[pred, list(args)] for pred, args in tup]
```

```
def resolution_algorithm(KB, query):
```

```
    KB = copy.deepcopy(KB)
```

```
    neg_query = []
```

```
    for q in query:
```

```
        if q[0].startswith("~"):
```

```
            neg_query.append([q[0][1:], q[1]])
```

```
        else:
```

```
            neg_query.append(["~" + q[0], q[1]])
```

```
    KB.append(neg_query)
```

```
    print("\nInitial KB + neg(query):")
```

```
    for c in KB:
```

```
        print(c)
```

```
    new = set()
```

```
while True:
```

```
    pairs = [(KB[i], KB[j]) for i in range(len(KB)) for j in range(i+1, len(KB))]
```

```
    for (ci, cj) in pairs:
```

```
        resolvents = resolve(ci,  
                           cj)
```

```
        for r in resolvents:
```

```
            if r == []:
```

```
                print("\n ! Contradiction found → QUERY PROVED.\n")
```

```
                return True
```

```
r_hash = clause_to_hashable(r)
```

```
if r_hash not in new:
```

```
    new.add(r_hash)
```

```
if all(hashable_to_clause(r) in KB for r in new):
```

```
    print("\nNo new clauses → QUERY NOT  
PROVED.\n") return False
```

```
for r in new:  
    clause =  
        hashable_to_clause(r) if  
        clause not in KB:  
            KB.append(clause)  
  
KB = [  
    [["Parent", ["x", "y"]], ["~Mother", ["x",  
        "y"]]], [["Mother", ["Mary", "John"]]]  
]  
  
query = [["Parent", ["Mary", "John"]]]  
print("Trying to prove:", query)  
resolution_algorithm(KB, query)
```

Program 10:

Implement Alpha-Beta Pruning.

Algorithm :

Adversarial Search

function Alpha-beta-(state).
 returns an action.

$u \leftarrow \text{max-value}(\text{state}, -\infty, +\infty)$
 return the action in actions(state) with
 value v .

function max-value (state; α, β) return x
utility value.

if terminal-test (state) then return utility (state).

$v \leftarrow -\infty$.

 for each a in Actions (state) do
 $v \leftarrow \max(v, \text{min-val}(\text{result}(s, a), \alpha, \beta))$
 if $v \geq \beta$ then return v .
 $x \leftarrow \max(x, v)$.
 return v .

function Min-Value (state, α, β) returns a utility val
if Terminal-test (state).
 return Utility (state).
 $v \leftarrow -\infty$.

 for each a in Action (state) do
 $v \leftarrow \text{MAX}(v, \text{Min-Value}(\text{Result}(s, a), \alpha, \beta))$
 if $v \leq \alpha$ then return v .
 $\beta \leftarrow \min(\beta, v)$.
 return v .

Code :

```
import math
```

```
def alphabeta(node, depth, alpha, beta, maximizingPlayer):
```

```
if depth == 0 or isinstance(node, int):
    return node

if maximizingPlayer:
    value = -math.inf
    for child in node:
        value = max(value, alphabeta(child, depth - 1, alpha, beta, False))
        alpha = max(alpha, value)
        if beta <= alpha:
            print(f"Pruned in MAX node: alpha={alpha}, beta={beta}")
            break
    return value

else:
    value = math.inf
    for child in node:
        value = min(value, alphabeta(child, depth - 1, alpha, beta, True))
        beta = min(beta, value)
        if beta <= alpha:
            print(f"Pruned in MIN node: alpha={alpha}, beta={beta}")
            break
    return value
```

```
game_tree = [
    [3, 5, 6],
    [1, 2, 4],
    [7, 9, 8]
]

result = alphabeta(game_tree, 2, -math.inf, math.inf, True)
print("\nFinal Result (Best value for Max):", result)
```