

CSM CS61B
Runtime Practice

Problem 1. Orders of Growth.

(a) Simplify using Big-O Notation: $N^2 + N \log N + 1000N + 6$

(b) Calculate the following limit: $\lim_{n \rightarrow \infty} \frac{n^2}{2^n}$

(c) What does the result of the above limit imply about the exponential and polynomial runtimes.
Hint: Is one always greater (grows faster) than the other?

(d) True or False: If function f has $\mathcal{O}(n)$ and $\Omega(1)$, its tight bound is always found by taking the average of n and 1 giving: $\Theta(n)$

Problem 2. Iteration

What is the runtime of the following functions?

```
public static void loopingMore(int[] array) {  
    int n = array.length;  
    for (int i = 0; i < 3*n*n*n; i++) {  
        System.out.println('I love you');  
    }  
}
```

```
public static void doubleLoopingHalf(int n) {  
    for (int i = 0; i < n; i++) {  
        for (int j = n; j > 0; j = j / 2) {  
            System.out.println('I love you');  
        }  
    }  
}
```

```
public static void weirdLooping(int n) {  
    for (int i = 0; i < n; i++) {  
        int num = Math.pow(2, i + 1) - 1;  
        for (int j = 0; j < num; j++) {  
            System.out.println('I love you');  
        }  
    }  
}
```

Problem 3. Recursion

Practice using the Work Per Layer Summation Formula

```
public static void mergeSort(int[] arr, int l, int r) {
    if (l < r) {
        // Compute Middle Index
        int m = (l + r) / 2

        mergeSort(arr, l, m);
        mergeSort(arr, m+1, r);

        merge(arr, l, m, r); // Runs in linear time
    }
}
```

```
public static void thinTree(int n) {
    if (N <= 1) {return;}
    else {
        thinTree(2);
        thinTree(n / 2);
    }
}
```

```
public static void splitter(int n) {
    if (N == 1) {return;}
    else {
        int i = 0;
        while (i < n) {
            i++
            System.out.println(i);
        }
        return splitter(n / 3) + splitter(2n / 3);
    }
}
```

Problem 4. Mutual Recursion

The following problem has been adapted from Prof. Hug's Sp15 Midterm 2

State the runtime of each function start with f1.

```
public static void f1(int n) {  
    for (int i = 0; i < 2*n; i++) {  
        System.out.println('Welcome');  
    }  
}
```

```
public static void f2(int n) {  
    if (n == 0) { return; }  
    f2(n / 3);  
    f1(n);  
    f2(n / 3);  
    f1(n);  
    f2(n / 3);  
}
```

```
public static void f3(int n) {  
    if (n == 0) { return; }  
    f3(n - 1);  
    f1(16);  
    f3(n - 1);  
}
```

```
public static void f4(int n) {  
    if (n == 0) { return; }  
    f4(n - 1);  
    f1(16);  
    f1(n);  
    f4(n - 1);  
}
```

```
public static void f5(int n, int m) {  
    if (m <= 0) {  
        return;  
    } else {  
        for (int i = 0; i < n; i++) {  
            f5(n, m-1);  
        }  
    }  
}
```
