

Engineering Mathematics

Single Variable Calculus

DPP-01

1. On the interval $[0, 1]$ the function $x^{25}(1-x)^{75}$ takes its maximum value at
 - (a) 0
 - (b) $1/2$
 - (c) 1
 - (d) $1/4$
2. The product of minimum value of x^x and maximum value of $\left(\frac{1}{x}\right)^x$ is
 - (a) e
 - (b) e^{-1}
 - (c) 1
 - (d) e^2
3. The minimum value of the function defined by $f(x) = \max(x, x+1, 2-x)$ is
 - (a) 0
 - (b) $1/2$
 - (c) 1
 - (d) $3/2$
4. The greatest and the least values of the function, $f(x) = 2 - \sqrt{1+2x+x^2}$, $x \in [-2, 1]$ are
 - (a) 2, 1
 - (b) 2, -1
 - (c) 2, 0
 - (d) None of these
5. The difference between the greatest and least values of the function $f(x) = \sin 2x - x$ on $[-\pi/2, \pi/2]$ is
 - (a) $\frac{\sqrt{3}+\sqrt{2}}{2}$
 - (b) $\frac{\sqrt{3}+\sqrt{2}}{2} + \frac{\pi}{6}$
 - (c) $\frac{\pi}{2}$
 - (d) π
6. If p and q are positive real numbers such that $p^2 + q^2 = 1$, then the maximum value of $(p+q)$ is
 - (a) 2
 - (b) $\frac{1}{2}$
 - (c) $\frac{1}{\sqrt{2}}$
 - (d) $\sqrt{2}$
7. If x is real, the maximum value of $\frac{3x^2+9x+17}{3x^2+9x+7}$ is
 - (a) 41
 - (b) 1
 - (c) $17/7$
 - (d) $1/4$
8. The maximum value $x^3 - 3x$ in the interval $[0, 2]$ is
 - (a) 1
 - (b) 2
 - (c) 0
 - (d) -2
9. Minimum value of $\frac{1}{3\sin\theta - 4\cos\theta + 7}$ is
 - (a) $\frac{7}{12}$
 - (b) $\frac{5}{12}$
 - (c) $\frac{1}{12}$
 - (d) $\frac{1}{6}$
10. The number of values of x where $f(x) = \cos x + \cos\sqrt{2}x$ attains its maximum value is
 - (a) 1
 - (b) 0
 - (c) 2
 - (d) infinite
11. The greatest value of $f(x) = (x+1)^{1/3} - (x-1)^{1/3}$ in $[0, 1]$ is
 - (a) 1
 - (b) 2
 - (c) 3
 - (d) $2^{1/3}$
12. if $\int_1^x \frac{dt}{t|\sqrt{t^2-1}|} = \frac{\pi}{6}$, then x can be equal to
 - (a) $\frac{2}{\sqrt{3}}$
 - (b) $\sqrt{3}$
 - (c) 2
 - (d) None of these
13. if $f(x) = \begin{cases} x; & x < 1 \\ x-1; & x \geq 1 \end{cases}$, then $\int_0^2 x^2 f(x) dx$ is equal to
 - (a) 1
 - (b) $4/3$
 - (c) $5/3$
 - (d) $5/2$

14. $\int_0^{\pi} |1 + 2\cos x| dx$ equal to :

- (a) $2\pi/3$ (b) π
(c) 2 (d) $\frac{\pi}{3} + 2\sqrt{3}$

15. The value of $\int_{-1}^3 (|x-2| + [x]) dx$ is equal to (where $[*]$ denotes greatest integer function)

- (a) 7 (b) 5
(c) 4 (d) 3

16. If $\int_{-1}^{3/2} |x \sin \pi x| dx = \frac{k}{\pi^2}$, then the value of k is

- (a) $3\pi + 1$ (b) $2\pi + 1$
(c) 1 (d) 4

17. $\int_{\log \pi - \log 2}^{\log \pi} \frac{e^x}{1 - \cos\left(\frac{2}{3}e^x\right)} dx$ is equal to

- (a) $\sqrt{3}$ (b) $-\sqrt{3}$
(c) $\frac{1}{\sqrt{3}}$ (d) $-\frac{1}{\sqrt{3}}$

18. If $I_1 = \int_e^{e^2} \frac{dx}{\ln x}$ and $I_2 = \int_1^2 \frac{e^x}{x} dx$, then

- (a) $I_1 = I_2$ (b) $2 I_1 = I_2$
(c) $I_1 = 2 I_2$ (d) None of these

19. $\int_{2-\log 3}^{3+\log 3} \frac{\log(4+x)}{\log(4+x) + \log(9-x)} dx$

- (a) Cannot be evaluated
(b) Is equal to $5/2$
(c) is equal to $1 + 2 \log 3$
(d) Is equal to $\frac{1}{2} + \log 3$

20. $\int_0^{\infty} [2e^{-x}] dx$ is equal to

- (where $[*]$ denotes the greatest integer function)
(a) 0 (b) $\ln 2$
(c) e^2 (d) $2e^{-1}$

21. If $\int_0^{\infty} e^{-x^2} dx = \frac{\sqrt{x}}{2}$, then $\int_0^{\infty} e^{-ax^2} dx$ where $a > 0$ is

- (a) $\frac{\sqrt{\pi}}{2}$ (b) $\frac{\sqrt{\pi}}{2a}$
(c) $2\frac{\sqrt{\pi}}{a}$ (d) $\frac{1}{2}\sqrt{\frac{\pi}{a}}$

22. The expression $\frac{\int_0^n [x] dx}{\int_0^n \{x\} dx}$ is equal to

(where $[*]$ and $\{*\}$ denotes greatest integer function and fractional part function and $n \in \mathbb{N}$).

- (a) $1/n - 1$ (b) $1/n$
(c) n (d) $n - 1$

23. Let $A = \int_0^1 \frac{e^t dt}{1+t}$ then $\int_{a-1}^a \frac{e^{-t}}{t-a-1} dt$ has the value

- (a) Ae^{-a} (b) $-Ae^{-a}$
(c) $-ae^{-a}$ (d) Ae^a

24. $\int_0^{\pi} xf(\sin x) dx$ is equal to

- (a) $\pi \int_0^{\pi} f(\sin x) dx$
(b) $\frac{\pi}{2} \int_0^{\pi/2} f(\sin x) dx$
(c) $\pi \int_0^{\pi/2} f(\cos x) dx$
(d) $\pi \int_0^{\pi} f(\cos x) dx$

25. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be a differentiable function having

$f(2) = 6$, $f'(2) = \left(\frac{1}{48}\right)$. Then $\lim_{x \rightarrow 2} \int_6^{f(x)} \frac{4t^3}{x-2} dt$ equals

- (a) 18 (b) 12
(c) 36 (d) 24

26. The value of $\int_0^{\pi/2} \frac{(\sin x + \cos x)^2}{\sqrt{1 + \sin 2x}} dx$ is

- (a) 0 (b) 1
(c) 2 (d) 3

27. If $f(a+b-x) = f(x)$, then $\int_a^b xf(x)dx$ is equal to

- (a) $\frac{a+b}{2} \int_a^b f(b-x)dx$
 (b) $\frac{a+b}{2} \int_a^b f(x)dx$
 (c) $\frac{b-a}{2} \int_a^b f(x)dx$
 (d) $\frac{a+b}{2} \int_a^b f(a+b+x)dx$

28. The value of $\lim_{x \rightarrow 0} \frac{\int_0^{x^2} \sec^2 t dt}{x \sin x}$ is

- (a) 3 (b) 2
 (c) 1 (d) -1

29. $\int_{\sin x}^1 t^2 f(t) dt = 1 - \sin x \forall x \in (0, \pi/2)$, then $f\left(\frac{1}{\sqrt{3}}\right)$ is

- (a) 3 (b) $\sqrt{3}$
 (c) $1/3$ (d) None of these

30. $\lim_{x \rightarrow 0} \frac{\int_0^{x^2} \cos t^2 dt}{x \sin x}$ is equal to

- (a) -1 (b) 1
 (c) 2 (d) -2

31. If $\int_{\ln 2}^x \frac{dx}{\sqrt{e^x - 1}} = \frac{\pi}{6}$, then $x =$

- (a) 4
 (b) $\ln 8$
 (c) $\ln 4$
 (d) None of these

32. $\lim_{x \rightarrow \infty} \left(\frac{x^2 - 2x + 1}{x^2 - 4x + 2} \right)^x =$

- (a) 1 (b) 2
 (c) e^2 (d) e

33. If α and β be the roots of $ax^2 + bx + c = 0$, then

$\lim_{x \rightarrow \alpha} (1 + ax^2 + bx + c)^{\frac{1}{x-\alpha}}$ is

- (a) $a(\alpha - \beta)$ (b) $\ln |a(\alpha - \beta)|$
 (c) $e^{a(\alpha - \beta)}$ (d) $e^{a|\alpha - \beta|}$

34. $\lim_{x \rightarrow \pi/2} \frac{2^{-\cos x} - 1}{x(x - \pi/2)} =$

- (a) $\frac{2 \ln 2}{\pi}$ (b) $\ln 2$
 (c) $2/\pi$ (d) Does not exist

35. $\lim_{x \rightarrow \pi/2} \frac{\left(1 - \tan \frac{x}{2}\right)(1 - \sin x)}{\left(1 + \tan \frac{x}{2}\right)(\pi - 2x)^3}$ is

- (a) $1/16$ (b) $-1/16$
 (c) $1/32$ (d) $-1/32$

36. $\lim_{x \rightarrow 0} (\cos mx)^{n/x^2}$

- (a) $e^{-m^2 n/4}$ (b) $e^{-m^2 n/2}$
 (c) $e^{-mn^2/2}$ (d) $e^{-mn^2/4}$

37. $\lim_{x \rightarrow 0} \frac{(4^x - 1)^3}{\sin\left(\frac{x}{p}\right) \ln\left(1 + \frac{x^2}{3}\right)} =$

- (a) $9p(\log 4)$ (b) $3p(\log 4)^3$
 (c) $12p(\log 4)^3$ (d) $27p(\log 4)^2$

38. Evaluate

$\lim_{n \rightarrow \infty} \left(\frac{1}{\sqrt{n^2}} + \frac{1}{\sqrt{n^2 + 1}} + \frac{1}{\sqrt{n^2 + 2}} + \dots + \frac{1}{\sqrt{n^2 + 2n}} \right)$

- (a) 1 (b) $1/2$
 (c) 0 (d) 2

39. $\lim_{x \rightarrow \infty} \left(\frac{x^2 + 5x + 3}{x^2 + x + 3} \right)^x$ is equal to

- (a) e^4 (b) e^2
(c) e^3 (d) e

40. Let α and β be the distinct roots of $ax^2 + bx + c = 0$,

Then $\lim_{x \rightarrow \alpha} \frac{1 - \cos(ax^2 + bx + c)}{(x - \alpha)^2}$ is equal to

- (a) $\frac{1}{2}(\alpha - \beta)^2$ (b) $-\frac{a^2}{2}(\alpha - \beta)^2$
(c) 0 (d) $\frac{a^2}{2}(\alpha - \beta)^2$

41. $\lim_{x \rightarrow 0} \left(\cot \left(\frac{\pi}{4} + x \right) \right)^{\operatorname{cosec} x} =$

- (a) e^{-1} (b) e^2

- (c) e^{-2} (d) e^1

42. $\lim_{x \rightarrow \infty} \left(\sin \frac{1}{x} + \cos \frac{1}{x} \right)^x$ is

- (a) e (b) e^2
(c) $1/e$ (d) does not exist

43. $\lim_{x \rightarrow \infty} \frac{\sin(6x^2)}{\ln \cos(2x^2 - x)} =$

- (a) 12 (b) -12
(c) 6 (d) -6

44. $\lim_{x \rightarrow 0} \frac{e^{-x^2/2} - \cos x}{x^3 \sin x} =$

- (a) $1/4$ (b) $1/6$
(c) $1/12$ (d) $1/8$

Answer Key

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| <p>1. (d)
2. (c)
3. (d)
4. (c)
5. (d)
6. (d)
7. (a)
8. (b)
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