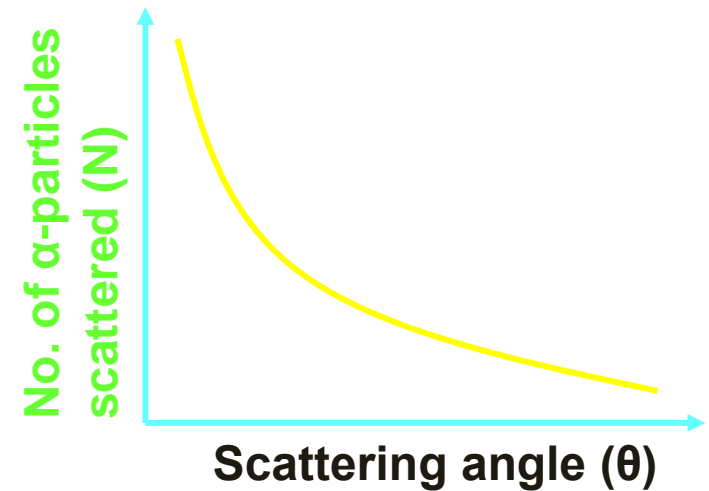
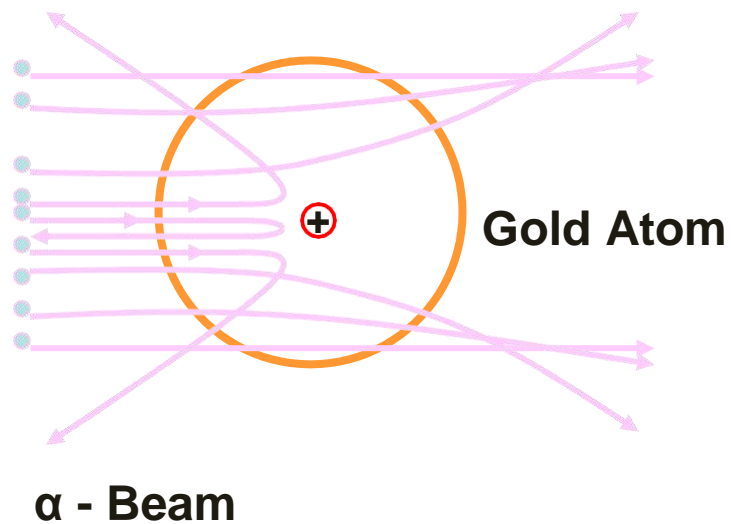
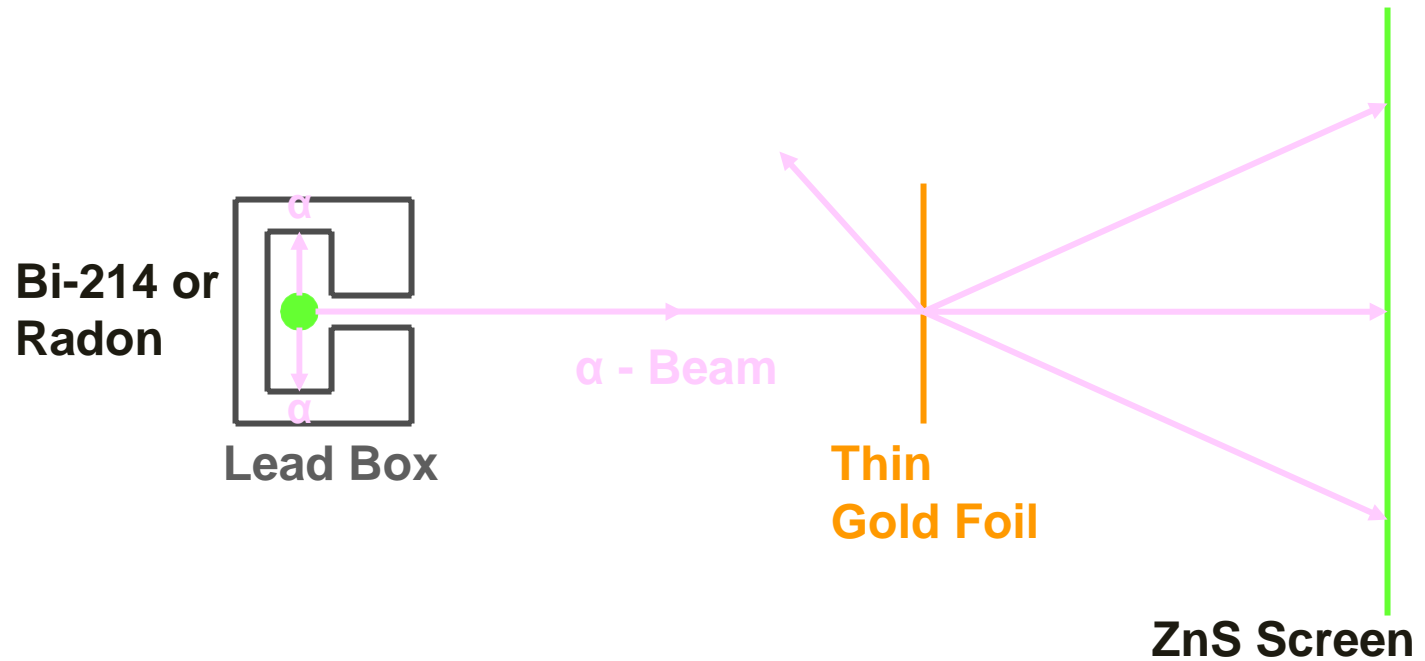


ATOMS & NUCLEI

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Rutherford's Alpha Scattering Experiment



Note It

Alpha – particle is a nucleus of helium atom carrying a charge of ‘+2e’ and mass equal to 4 times that of hydrogen atom. It travels with a speed nearly 10^4 m/s and is highly penetrating.

	Rutherford Experiment	Geiger & Marsden Experiment
Source of α -particle	Radon ${}_{86}\text{Rn}^{222}$	Bismuth ${}_{83}\text{Bi}^{214}$
Speed of α -particle	10^4 m/s	1.6×10^7 m/s
Thickness of Gold foil	10^{-6} m	2.1×10^{-7} m

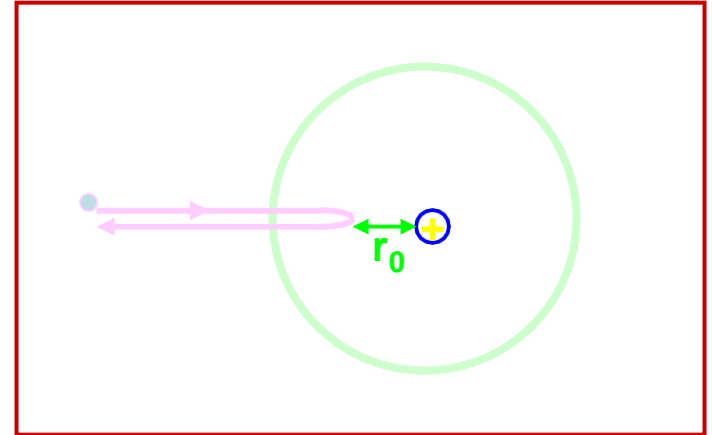
S. No.	Observation	Conclusion
1	Most of the α -particles passed straight through the gold foil.	It indicates that most of the space in an atom is empty.
2	Some of the α -particles were scattered by only small angles, of the order of a few degrees.	α -particles being +vely charged and heavy compared to electron could only be deflected by heavy and positive region in an atom. It indicates that the positive charges and the most of the mass of the atom are concentrated at the centre called 'nucleus'.
3	A few α -particles (1 in 9000) were deflected through large angles (even greater than 90°). Some of them even retraced their path. i.e. angle of deflection was 180° .	α -particles which travel towards the nucleus directly get retarded due to Coulomb's force of repulsion and ultimately comes to rest and then fly off in the opposite direction.

$$N(\theta) \propto \frac{1}{\sin^4(\theta/2)}$$

Distance of Closest Approach (Nuclear size):

When the distance between α -particle and the nucleus is equal to the distance of the closest approach (r_0), the α -particle comes to rest.

At this point or distance, the kinetic energy of α -particle is completely converted into electric potential energy of the system.



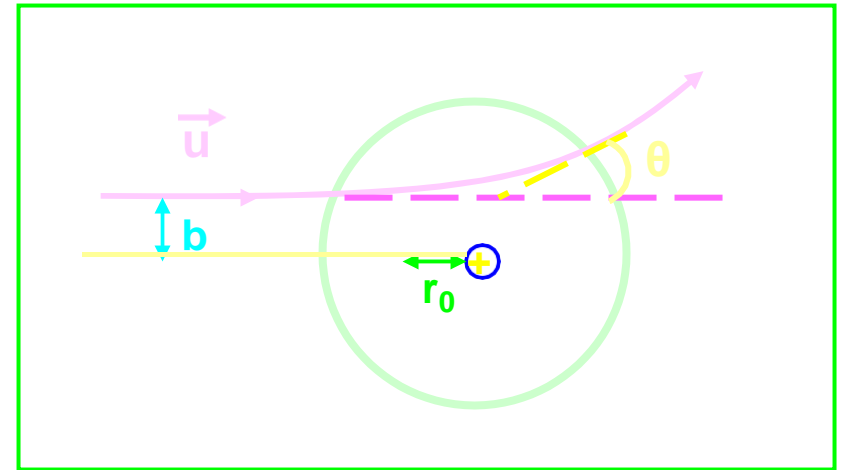
$$\frac{1}{2} mu^2 = \frac{1}{4\pi\epsilon_0} \frac{2 Ze^2}{r_0}$$

$$r_0 = \frac{1}{4\pi\epsilon_0} \frac{2 Ze^2}{\frac{1}{2} mu^2}$$

Impact Parameter (b):

The perpendicular distance of the velocity vector of the α -particle from the centre of the nucleus when it is far away from the nucleus is known as impact parameter.

$$b = \frac{Ze^2 \cot (\theta/2)}{4\pi\epsilon_0 (\frac{1}{2} mu^2)}$$



- i) For large value of b , $\cot \theta/2$ is large and θ , the scattering angle is small.
i.e. α -particles travelling far away from the nucleus suffer small deflections.
- ii) For small value of b , $\cot \theta/2$ is also small and θ , the scattering angle is large.
i.e. α -particles travelling close to the nucleus suffer large deflections.
- iii) For $b = 0$ i.e. α -particles directed towards the centre of the nucleus,

$$\cot \theta/2 = 0 \quad \text{or} \quad \theta/2 = 90^\circ \quad \text{or} \quad \theta = 180^\circ$$

The α -particles retrace their path.

Composition of Nucleus:

Every atomic nucleus except that of Hydrogen has two types of particles – protons and neutrons. (Nucleus of Hydrogen contains only one proton)

Proton is a fundamental particle with positive charge $1.6 \times 10^{-19} \text{ C}$ and mass $1.67 \times 10^{-27} \text{ kg}$ (1836 times heavier than an electron).

Neutron is also a fundamental particle with no charge and mass $1.675 \times 10^{-27} \text{ kg}$ (1840 times heavier than an electron).

Atomic Number (Z):

The number of protons in a nucleus of an atom is called atomic number.

Atomic Mass Number (A):

The sum of number of protons and number of neutrons in a nucleus of an atom is called atomic mass number.

$$A = Z + N$$

Atomic Mass Unit (amu):

Atomic Mass Unit (amu) is $(1 / 12)$ th of mass of 1 atom of carbon.

$$1 \text{ amu} = \frac{1}{12} \times \frac{12}{6.023 \times 10^{23}} \text{ g} = 1.66 \times 10^{-27} \text{ kg}$$

Size of Nucleus:

Nucleus does not have a sharp or well-defined boundary.

However, the radius of nucleus can be given by

$$R = R_0 A^{1/3} \quad \text{where } R_0 = 1.2 \times 10^{-5} \text{ m is a constant which is the same for all nuclei and } A \text{ is the mass number of the nucleus.}$$

Radius of nucleus ranges from 1 fm to 10 fm.

$$\text{Nuclear Volume, } V = (4/3) \pi R^3 = (4/3) \pi R_0^3 A$$

$$V \propto A$$

Nucleus Density:

$$\text{Mass of nucleus, } M = A \text{ amu} = A \times 1.66 \times 10^{-27} \text{ kg}$$

$$\begin{aligned} \text{Nuclear Volume, } V &= (4/3) \pi R^3 = (4/3) \pi R_0^3 A \\ &= \frac{4}{3} \times \frac{22}{7} \times (1.2 \times 10^{-15})^3 A \text{ m}^3 \\ &= 7.24 \times 10^{-45} A \text{ m}^3 \end{aligned}$$

$$\text{Nucleus Density, } \rho = M / V = 2.29 \times 10^{17} \text{ kg / m}^3$$

Discussion:

- 1. The nuclear density does not depend upon mass number. So, all the nuclei possess nearly the same density.**
- 2. The nuclear density has extremely large value. Such high densities are found in white dwarf stars which contain mainly nuclear matter.**
- 3. The nuclear density is not uniform throughout the nucleus. It has maximum value at the centre and decreases gradually as we move away from the centre of the nucleus.**
- 4. The nuclear radius is the distance from the centre of the nucleus at which the density of nuclear matter decreases to one-half of its maximum value at the centre.**

Mass – Energy Relation:

According to Newton's second law of motion, force acting on a body is defined as the rate of change of momentum.

$$F = \frac{d}{dt} (mv) = m \frac{dv}{dt} + v \frac{dm}{dt}$$

If this force F displaces the body by a distance dx , its energy increases by

$$dK = F \cdot dx = m \frac{dv}{dt} dx + v \frac{dm}{dt} dx$$

$$dK = m \frac{dx}{dt} dv + v \frac{dx}{dt} dm$$

$$dK = m v dv + v^2 dm \dots\dots\dots (1)$$

According to Einstein's relation of relativistic mass,

$$m = \frac{m_0}{[1 - (v^2 / c^2)]^{1/2}}$$

Note It

Squaring and manipulating, $m^2 c^2 - m^2 v^2 = m_0^2 c^2$

Differentiating (with m_0 and c as constants)

$$c^2 2m \, dm - m^2 2v \, dv - v^2 2m \, dm = 0$$

$$\text{or } c^2 \, dm - mv \, dv - v^2 \, dm = 0$$

$$c^2 \, dm = mv \, dv + v^2 \, dm \dots\dots\dots (2)$$

From (1) and (2), $dK = dm \, c^2$

If particle is accelerated from rest to a velocity v , let its mass m_0 increases to m .
Integrating,

$$\text{Total increase in K.E.} = \int_0^K dK = c^2 \int_{m_0}^m dm$$

$$\therefore K = (m - m_0) c^2 \quad \text{or} \quad K + m_0 c^2 = m c^2$$

Here $m_0 c^2$ is the energy associated with the rest mass of the body and K is the kinetic energy.

Thus, the total energy of the body is given by

$$E = m c^2$$

This is Einstein's mass - energy equivalence relation.

Mass Defect:

It is the difference between the rest mass of the nucleus and the sum of the masses of the nucleons composing a nucleus is known as mass defect.

$$\Delta m = [Zm_p + (A - Z) m_n] - M$$

Mass defect per nucleon is called packing fraction.

Binding Energy:

It is the energy required to break up a nucleus into its constituent parts and place them at an infinite distance from one another.

$$B.E = \Delta m c^2$$

Nuclear Forces:

They are the forces between p – p, p – n or n – n in the nucleus. They can be explained by Meson Theory.

There are three kinds of mesons – positive (π^+), negative (π^-) and neutral (π^0).

π^+ and π^- are 273 times heavier than an electron.

π^0 is 264 times heavier than an electron.

Nucleons (protons and neutrons) are surrounded by mesons.

Main points of Meson Theory:

1. There is a continuous exchange of a meson between one nucleon and other. This gives rise to an exchange force between them and keep them bound.
2. Within the nucleus, a neutron is never permanently a neutron and a proton is never permanently a proton. They keep on changing into each other due to exchange of π -mesons.
3. The $n - n$ forces arise due to exchange of π^0 – mesons between the neutrons.



4. The $p - p$ forces arise due to exchange of π^0 – mesons between the protons.



Note It

5. The n – p forces arise due to exchange of π^+ and π^- mesons between the nucleons.



6. The time involved in such an exchange is so small that the free meson particles cannot be detected as such.

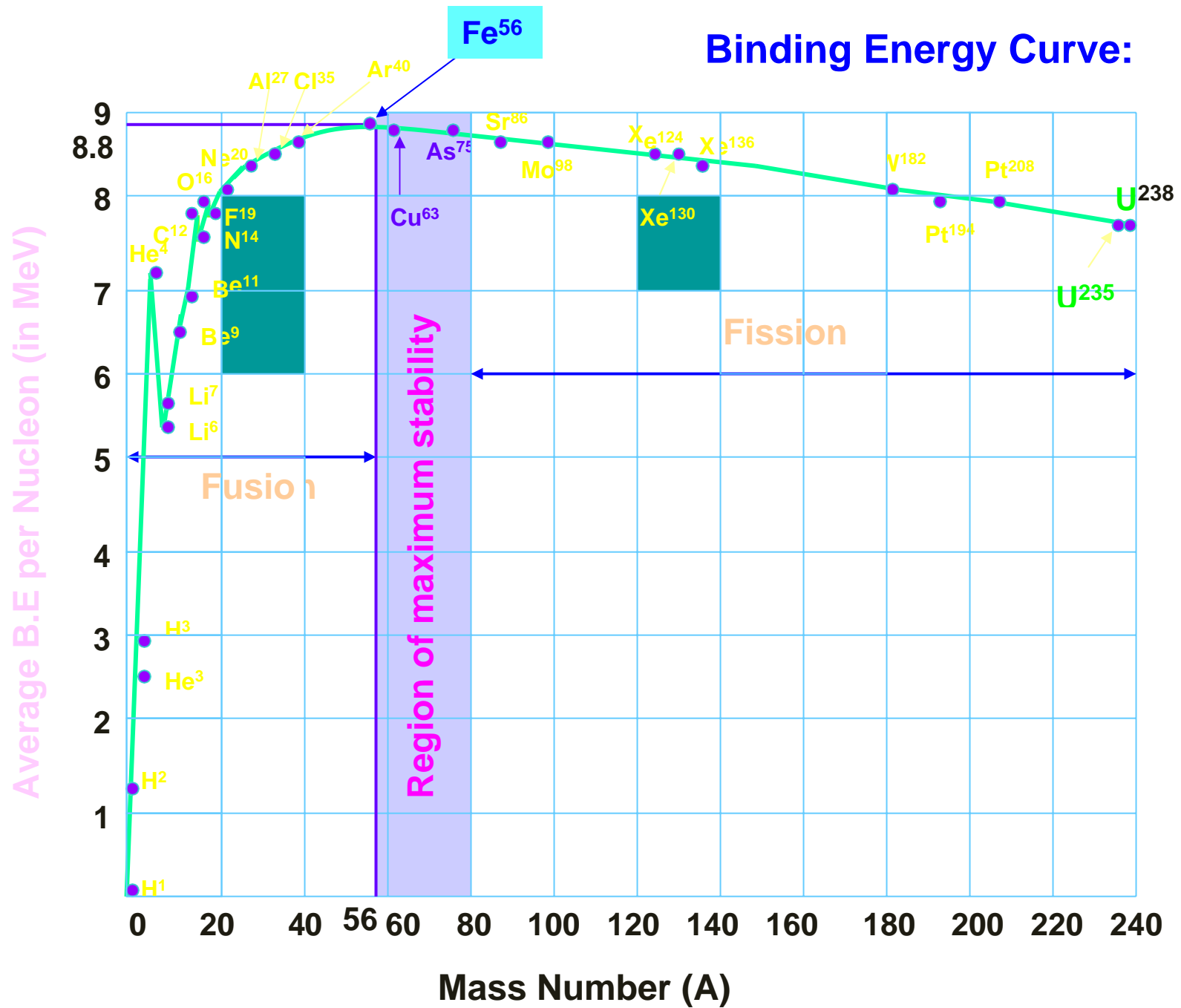
Binding Energy per Nucleon:

It is the binding energy divided by total number of nucleons.

It is denoted by B

$$B = \text{B.E} / \text{Nucleon} = \Delta m c^2 / A$$

Note It



Special Features of Binding Energy Curve

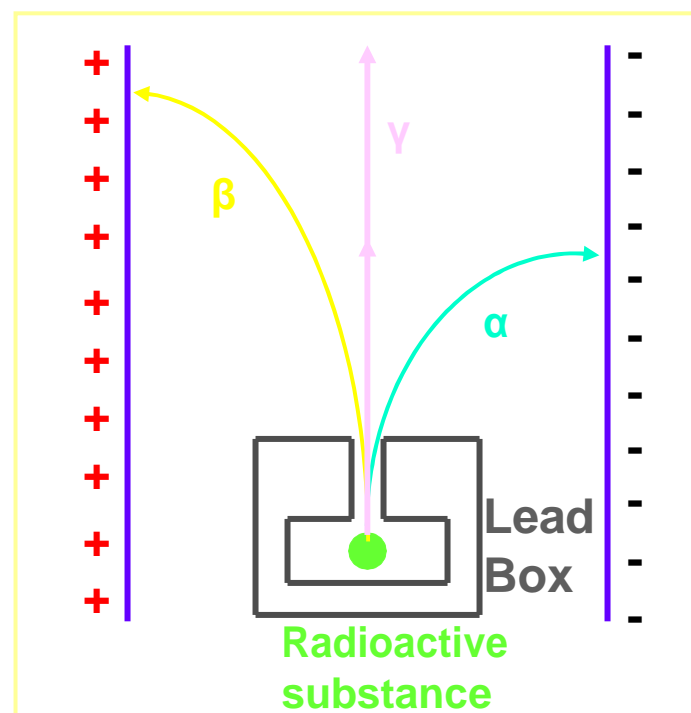
1. Binding energy per nucleon of very light nuclides such as ${}_1\text{H}^2$ is very small.
2. Initially, there is a rapid rise in the value of binding energy per nucleon.
3. Between mass numbers 4 and 20, the curve shows cyclic recurrence of peaks corresponding to ${}_2\text{He}^4$, ${}_4\text{Be}^8$, ${}_6\text{C}^{12}$, ${}_8\text{O}^{16}$ and ${}_{10}\text{Ne}^{20}$. This shows that the B.E. per nucleon of these nuclides is greater than those of their immediate neighbours. Each of these nuclei can be formed by adding an alpha particle to the preceding nucleus.
4. After $A = 20$, there is a gradual increase in B.E. per nucleon. The maximum value of 8.8 MeV is reached at $A = 56$. Therefore, Iron nucleus is the most stable.
5. Binding energy per nucleon of nuclides having mass numbers ranging from 40 to 120 are close to the maximum value. So, these elements are highly stable and non-radioactive.
6. Beyond $A = 120$, the value decreases and falls to 7.6 MeV for Uranium.
7. Beyond $A = 128$, the value shows a rapid decrease. This makes elements beyond Uranium (trans – uranium elements) quite unstable and radioactive.
8. The drooping of the curve at high mass number indicates that the nucleons are more tightly bound and they can undergo fission to become stable.
9. The drooping of the curve at low mass numbers indicates that the nucleons can undergo fusion to become stable.

Radioactivity:

Radioactivity is the phenomenon of emitting alpha, beta and gamma radiations spontaneously.

Soddy's Displacement Law:

1. ${}_Z Y^A \xrightarrow{\alpha} {}_{Z-2} Y^{A-4}$
2. ${}_Z Y^A \xrightarrow{\beta} {}_{Z+1} Y^A$
3. ${}_Z Y^A \xrightarrow{\gamma} {}_Z Y^A \text{ (Lower energy)}$



Rutherford and Soddy's Laws of Radioactive Decay:

1. The disintegration of radioactive material is purely a random process and it is merely a matter of chance. Which nucleus will suffer disintegration, or decay first can not be told.
2. The rate of decay is completely independent of the physical composition and chemical condition of the material.
3. The rate of decay is directly proportional to the quantity of material actually present at that instant. As the decay goes on, the original material goes on decreasing and the rate of decay consequently goes on decreasing.

Note It

If N is the number of radioactive atoms present at any instant, then the rate of decay is,

$$-\frac{dN}{dt} \propto N \quad \text{or} \quad -\frac{dN}{dt} = \lambda N$$

where λ is the decay constant or the disintegration constant.

Rearranging,

$$\frac{dN}{N} = -\lambda dt$$

Integrating, $\log_e N = -\lambda t + C$ where C is the integration constant.

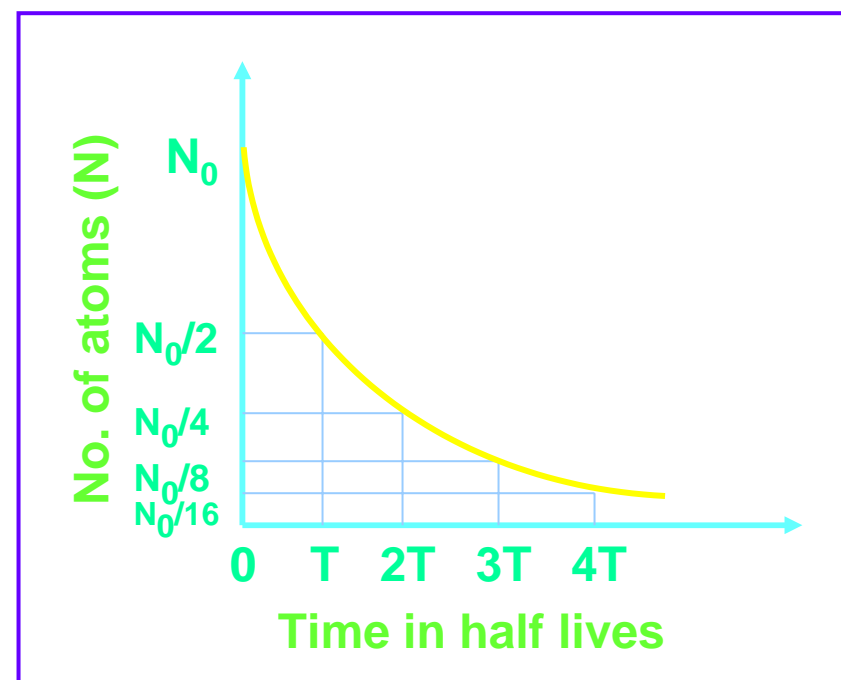
If at $t = 0$, we had N_0 atoms, then

$$\log_e N_0 = 0 + C$$

$$\therefore \log_e N - \log_e N_0 = -\lambda t$$

$$\text{or} \quad \log_e (N / N_0) = -\lambda t$$

$$\text{or} \quad \frac{N}{N_0} = e^{-\lambda t} \quad \text{or} \quad N = N_0 e^{-\lambda t}$$



Note It

Radioactive Disintegration Constant (λ):

According to the laws of radioactive decay,

$$\frac{dN}{N} = -\lambda dt$$

If $dt = 1$ second, then

$$\frac{dN}{N} = -\lambda$$

Thus, λ may be defined as the relative number of atoms decaying per second.

Again, since $N = N_0 e^{-\lambda t}$

And if, $t = 1 / \lambda$, then $N = N_0 / e$

$$\text{or } \frac{N}{N_0} = \frac{1}{e}$$

Thus, λ may also be defined as the reciprocal of the time when N / N_0 falls to $1 / e$.

Note It

Half – Life Period:

Half life period is the time required for the disintegration of half of the amount of the radioactive substance originally present.

If T is the half – life period, then

$$\frac{N}{N_0} = \frac{1}{2} = e^{-\lambda T} \quad (\text{since } N = N_0/2)$$

$$e^{\lambda T} = 2$$

$$\lambda T = \log_e 2 = 0.6931$$

$$T = \frac{0.6931}{\lambda} \quad \text{or} \quad \lambda = \frac{0.6931}{T}$$

Time t in which material changes from N_0 to N :

$$t = 3.323 T \log_{10} (N_0/N)$$

Number of Atoms left behind after n Half – Lives:

$$N = N_0 (1/2)^n \quad \text{or} \quad N = N_0 (1/2)^{t/T}$$

Units of Radioactivity:

1. **The curie (Ci):** The activity of a radioactive substance is said to be one curie if it undergoes 3.7×10^{10} disintegrations per second.

$$1 \text{ curie} = 3.7 \times 10^{10} \text{ disintegrations / second}$$

2. **The rutherford (Rd):** The activity of a radioactive substance is said to be one rutherford if it undergoes 10^6 disintegrations per second.

$$1 \text{ rutherford} = 10^6 \text{ disintegrations / second}$$

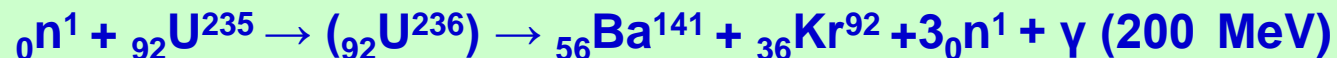
3. **The becquerel (Bq):** The activity of a radioactive substance is said to be one becquerel if it undergoes 1 disintegration per second.

$$1 \text{ becquerel} = 1 \text{ disintegration / second}$$

$$1 \text{ curie} = 3.7 \times 10^4 \text{ rutherford} = 3.7 \times 10^{10} \text{ becquerel}$$

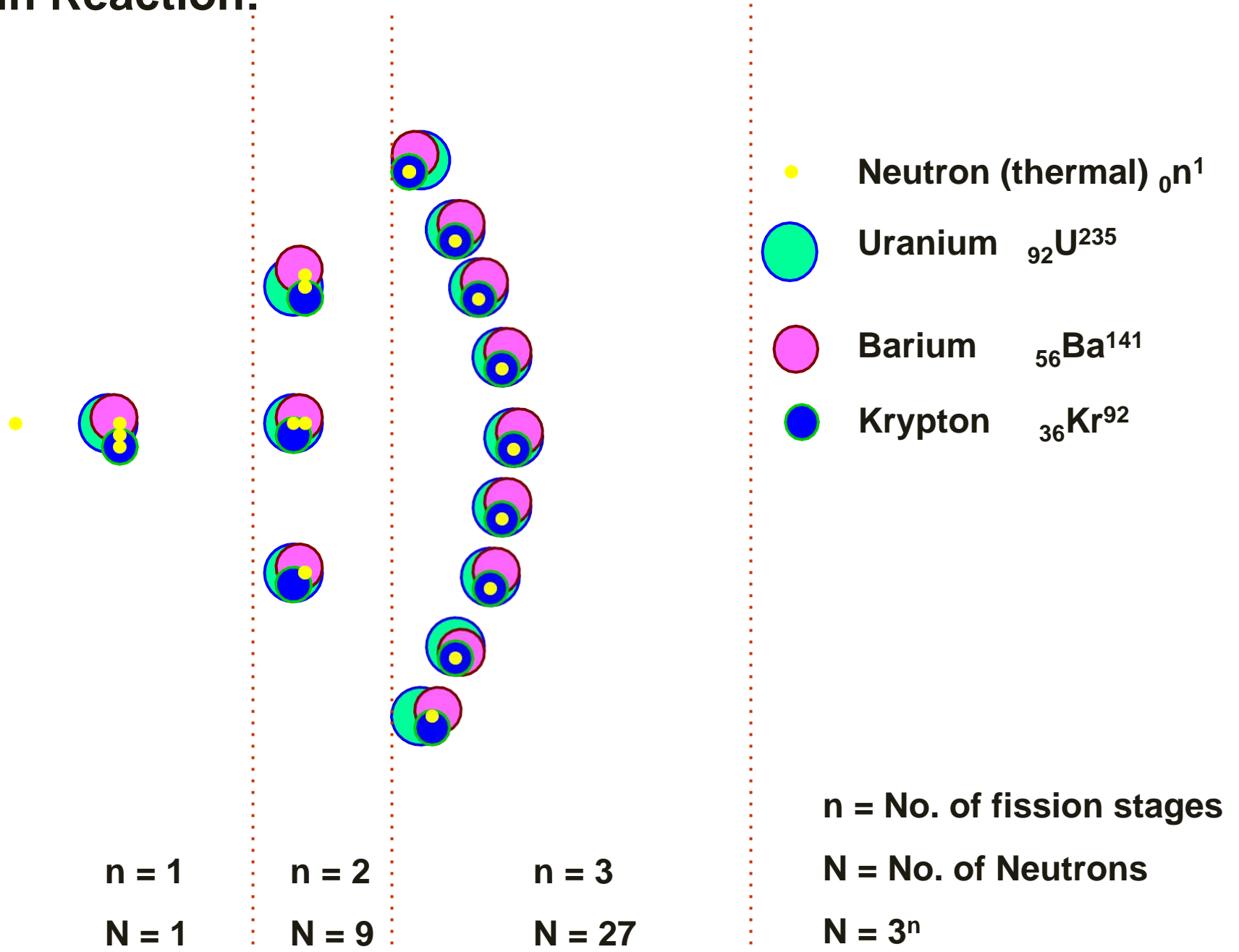
Nuclear Fission:

Nuclear fission is defined as a type of nuclear disintegration in which a heavy nucleus splits up into two nuclei of comparable size accompanied by a release of a large amount of energy.

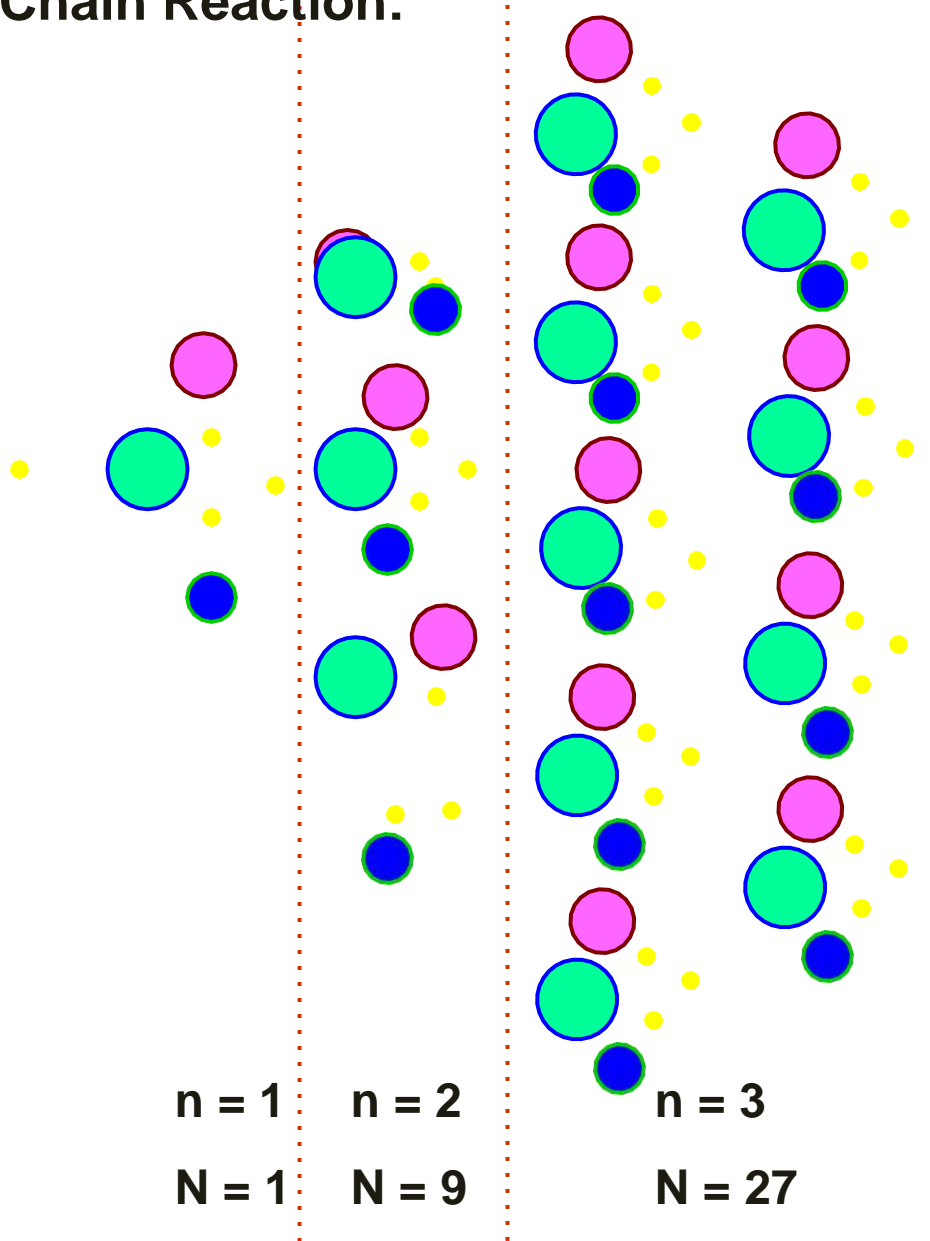


Note It

Chain Reaction:



Chain Reaction:



Critical Size:

For chain reaction to occur, the size of the fissionable material must be above the size called 'critical size'.

A released neutron must travel minimum through 10 cm so that it is properly slowed down (thermal neutron) to cause further fission.

If the size of the material is less than the critical size, then all the neutrons are lost.

If the size is equal to the critical size, then the no. of neutrons produced is equal to the no. of neutrons lost.

If the size is greater than the critical size, then the reproduction ratio of neutrons is greater than 1 and chain reaction can occur.

Nuclear Fusion:

Nuclear fusion is defined as a type of nuclear reaction in which two lighter nuclei merge into one another to form a heavier nucleus accompanied by a release of a large amount of energy.

Energy Source of Sun:

Proton – Proton Cycle:



Energy Source of Star:

Carbon - Nitrogen Cycle:

