

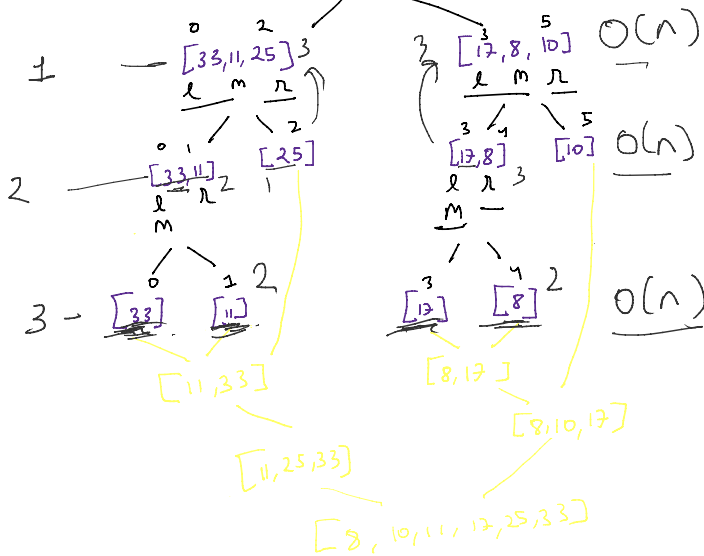
18th Feb

Merge Two Sorted Array: $\text{merge}(a1, a2)$

$a = [2, 4, 6, 8]$
 $b = [1, 3, 5, 7]$

Merge Sort:-

$[3, 3, 11, 25, 17, 8, 10]$, Size = 6



$n = 6$

$$\log_2(n) = 2 \dots$$

$$2 \approx 3$$

$$T.C \Rightarrow \log(n) \times (n) = O(n \log(n))$$

$$S.C \Rightarrow O(n)$$

int[] mergeSort(arr, l, r) {
 if (l == r) {
 int[] res = new int[1];
 res[0] = arr[l];
 return res;
 }
}

$$\text{mid} = (l + r) / 2;$$

$$lArr = \text{mergeSort}(arr, l, \text{mid});$$

$$rArr = \text{mergeSort}(arr, \text{mid} + 1, r);$$

$$\text{res} = \text{merge}(lArr, rArr);$$

return res

	l	r	m	lArr	rArr	?
8	4	4				1✓
7	3	3				1✓
6	3	4	3	[20]	[10]	2✓3✓4✓5
5	2	2				1✓
4	1	1				1✓
3	0	0				1✓2✓3✓4✓5
2	0	1	0	[50]	[40]	1✓2✓3✓4✓5

$[50, 40, 30, 20, 10]$

```
public static int[] mergeSort(int[] arr, int l, int r) {
    1. if (l == r) {...} return [l];
    2. int mid = (l + r) / 2;
    3. int[] lArr = mergeSort(arr, l, mid);
    4. int[] rArr = mergeSort(arr, mid + 1, r);
    5. return mergeTwoSortedArray(lArr, rArr);
}
```

3	0	0		$[50]$ ✓	$[40]$ ✓	1 2 3 4 5
2	0	1	0	$[50]$ ✓	$[30]$ ✓	1 2 3 4 5
1	0	2	1	$[40, 50]$ ✓		1 2 3 4 5
0	0	4	2	$[30, 40, 50]$	$[10, 20]$	1 2 3 4 5

→ $[10, 20, 30, 40, 50]$

Partion Inden :-

ans = [9, 8, 6, 18, 33, 27] Pivot = 18
 Element before 'i' are equal or smaller than pivot.

$[9, 8, 33, 27, 6, 18, 10, 2, 3]$ int $PI(ans) \{$

```

i = 0, j = 0
while (i < arr.length) {
    if (arr[i] <= p) {
        swap(arr, i, j)
        i++;
        j++;
    } else {
        i++;
    }
}
return j - 1;

```

$$[\overset{0}{\underset{-}{6}}, \overset{1}{\underset{-}{8}}, \overset{2}{9}, \overset{3}{1}, \overset{4}{\underset{1}{33}}, \overset{5}{\underset{1}{27}}] \quad \underline{\underline{p=9}}$$

```
public static int partitionIndex(int[] arr) {
    int pivot = arr[arr.length - 1];
    int i = 0, j = 0;
    while (i < arr.length) {
        if (arr[i] <= pivot) {
            if (i != j) swap(arr, i, j);
            j++;
        }
        i++;
    }
    return j - 1;
}
```

H. W \Rightarrow

[https://www.geeksforgeeks.org/
count-number-of-occurrences-
or-frequency-in-a-sorted-array/](https://www.geeksforgeeks.org/count-number-of-occurrences-or-frequency-in-a-sorted-array/)

[https://www.geeksforgeeks.org/
print-subsequences-string/](https://www.geeksforgeeks.org/print-subsequences-string/)