# Labs for Foundations of Applied Mathematics

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#### **Preface**

This lab manual is designed to accompany the textbooks *Foundations of Applied Mathematics* by Humpherys, Jarvis, Evans and Whitehead.

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https://github.com/Foundations-of-Applied-Mathematics/Labs as the original source of this work.

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