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**Course : Introduction To Data Science**

**Submitted To.**

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**Reg# : SP20-BCS-046**

**Semester : 6<sup>th</sup>**

**Assignment# : 5<sup>th</sup>**

**Question 1.**

S1 → Sunshine state enjoy sunshine.

S2 → Brown fox jump high, brown fox run..

S3 → Sunshine state fox run fast.

**Bag of Words:**

Documents	Vocabulary									Length
	sunshine	state	enjoy	brown	fox	jump	high	run	fast	
S1	2	1	1	0	0	0	0	0	0	4
S2	0	0	0	2	2	1	1	1	0	7
S3	1	1	0	0	1	0	0	1	1	5

**Term Frequency (TF)****Formula:**

$$TF = (\text{number of times term appears in document}) / (\text{total number of terms in document})$$
**S1:**

sunshine → 2/4

state → 1/4

enjoy → 1/4

**S2:**

brown → 2/7

fox → 2/7

jump → 1/7

high → 1/7

run → 1/7

**S3:**

sunshine → 1/5

state → 1/5

fox → 1/5

run → 1/5

fast → 1/5

**Table of TF**

Documents	Vocabulary								
	sunshine	state	enjoy	brown	fox	jump	high	run	fast
S1	2/4	1/4	1/4	0	0	0	0	0	0
S2	0	0	0	2/7	2/7	1/7	1/7	1/7	0
S3	1/5	1/5	0	0	1/5	0	0	1/5	1/5

**Inverse Document Frequency (IDF)****Formula:**IDF =  $\log(\text{total number of documents}) / (\text{number of documents containing the term})$ sunshine →  $\log(3/2) = 0.176$ state →  $\log(3/2) = 0.176$ enjoy →  $\log(3/1) = 0.477$ brown →  $\log(3/1) = 0.477$ fox →  $\log(3/2) = 0.176$ jump →  $\log(3/1) = 0.477$ high →  $\log(3/1) = 0.477$ run →  $\log(3/2) = 0.176$ fast →  $\log(3/1) = 0.477$ **Term Frequency-Inverse Document Frequency (TF-IDF)****S1:**sunshine →  $2/4 \times 0.176 = 0.088$ state →  $1/4 \times 0.176 = 0.044$ enjoy →  $1/4 \times 0.477 = 0.1192$ **S2:**brown →  $2/7 \times 0.477 = 0.136$ fox →  $2/7 \times 0.176 = 0.051$ jump →  $1/7 \times 0.477 = 0.068$

high  $\rightarrow 1/7 \times 0.477 = 0.068$

run  $\rightarrow 1/7 \times 0.176 = 0.025$

### **S3:**

sunshine  $\rightarrow 1/5 \times 0.176 = 0.0352$

state  $\rightarrow 1/5 \times 0.176 = 0.0352$

fox  $\rightarrow 1/5 \times 0.176 = 0.0352$

run  $\rightarrow 1/5 \times 0.176 = 0.0352$

fast  $\rightarrow 1/5 \times 0.477 = 0.0954$

**TF-IDF Table.**

Vocabulary	S1	S2	S3
sunshine	0.088	0	0.0352
state	0.044	0	0.0352
enjoy	0.11925	0	0
brown	0	0.136	0
fox	0	0.051	0.0352
jump	0	0.068	0
high	0	0.068	0
run	0	0.025	0.0352
fast	0	0	0.0954

### **Question 2.**

**Cosine similarity between S1 and S3.**

#### **Formula:**

$$\text{Cos } \Theta = S1.S3 \div |S1| |S3|$$

#### **Vector Representation of S1 and S3:**

$$S1 = [2,1,1,0,0,0,0,0,0]$$

$$S3 = [1,1,0,0,1,0,0,1,1]$$

#### **To Find S1.S3:**

$$S1.S3 = (2*1)+(1*1) + (1*0)+(0*0)+(0*1)+(0*0)+(0*0)+(0*1)+(0*1)$$

$$S1.S3 = 2+1$$

$$S1.S3 = 3$$

**To Find |S1| and |S2|:**

$$|S1| = (2*2 + 1*1 + 1*1)^{0.5}$$

$$= (4+1+1)^{0.5}$$

$$= (6)^{0.5}$$

$$= 2.45$$

$$|S2| = (1*1 + 1*1 + 1*1 + 1*1 + 1*1)^{0.5}$$

$$= (1+1+1+1+1)^{0.5}$$

$$= (5)^{0.5}$$

$$= 2.24$$

**Now put these values in Cos  $\Theta = S1.S3 \div |S1| |S3|$**

$$\text{Cos}(S1,S3) = 3 / (2.45)(2.24)$$

$$= 3 / 5.47$$

$$= \mathbf{0.547}$$

**Cosine similarity of S1 and S3 is,**

$$\text{Cos}(S1,S3) = 0.547$$

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