



Real Python

# NumPy, SciPy, and Pandas: Correlation With Python

by Mirko Stojiljković 5 Comments data-science intermediate

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**Correlation coefficients** quantify the association between [variables](#) or features of a dataset. These [statistics](#) are of high importance for science and technology, and Python has great tools that you can use to calculate them. [SciPy](#), [NumPy](#), and [Pandas](#) correlation methods are fast, comprehensive, and well-documented.

### In this tutorial, you'll learn:

- What Pearson, Spearman, and Kendall **correlation coefficients** are
- How to use SciPy, NumPy, and Pandas **correlation functions**
- How to **visualize** data, regression lines, and correlation matrices with Matplotlib

You'll start with an explanation of correlation of NumPy, SciPy and Pandas correlation.

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```
1 # How to merge two dicts
2 # in Python 3.5+
3
4 >>> x = {'a': 1, 'b': 2}
5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```



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## Correlation

[Statistics](#) and [data science](#) are often concerned about the relationships between two or more variables (or features) of a dataset. Each data point in the dataset is an **observation**, and the **features** are the properties or attributes of those observations.

Every dataset you work with uses variables and observations. For example, you might be interested in understanding the following:

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- How the height of basketball players is [correlated to their shooting accuracy](#).
- Whether there's a relationship between [employee work experience and salary](#).
- What mathematical dependence exists between the [population density](#) and the [gross domestic product](#) of different countries

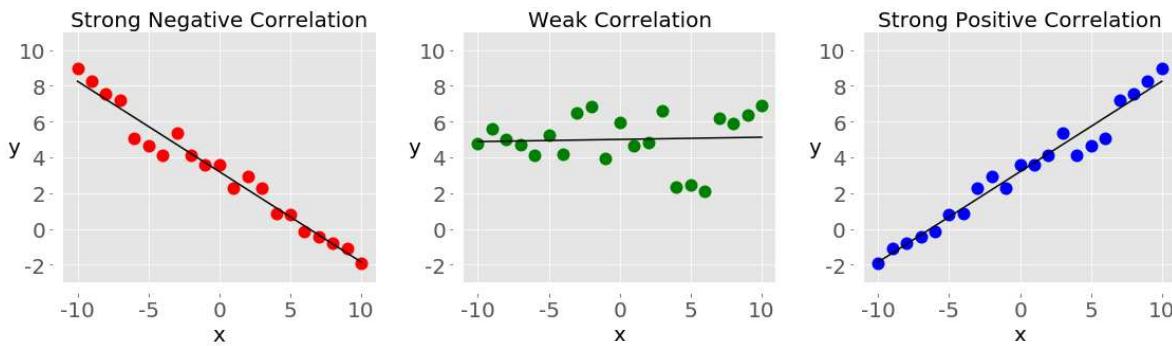
In the examples above, the height, shooting accuracy, years of experience, salary, population density, and gross domestic product are the features or variables. The data related to each player, employee, and each country are the observations.

When data is represented in the form of a table, the rows of that table are usually the observations, while the columns are the features. Take a look at this employee table:

Name	Years of Experience	Annual Salary
Ann	30	120,000
Rob	21	105,000
Tom	19	90,000
Ivy	10	82,000

In this table, each row represents one observation, or the data about one employee (either Ann, Rob, Tom, or Ivy). Each column shows one property or feature (name, experience, or salary) for all the employees.

If you analyze any two features of a dataset, then you'll find some type of **correlation** between those two features. Consider the following figures:



Each of these plots shows one of three different types of correlation:

**1. Negative correlation (red dots):**

This shows strong negative correlation, which occurs when large values of one feature correspond to small values of the other, and vice versa.

**2. Weak or no correlation (green dot):**

This illustrates weak or no correlation, which occurs when an association exists but it is not strong enough to be considered linear.

**3. Positive correlation (blue dots):**

This illustrates strong positive correlation, which occurs when large values of one feature correspond to large values of the other, and vice versa.

The next figure represents the data from the employee table above:

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The correlation between experience and salary is positive because higher experience corresponds to a larger salary and vice versa.

**Note:** When you're analyzing correlation, you should always have in mind that **correlation does not indicate causation**. It quantifies the strength of the relationship between the features of a dataset. Sometimes, the association is caused by a factor common to several features of interest.

Correlation is tightly connected to other statistical quantities like the mean, standard deviation, variance, and covariance. If you want to learn more about these quantities and how to calculate them with Python, then check out [Descriptive Statistics with Python](#).

There are several statistics that you can use to quantify correlation. In this tutorial, you'll learn about three correlation coefficients:

- [Pearson's r](#)
- [Spearman's rho](#)
- [Kendall's tau](#)

Pearson's coefficient measures [linear correlation](#), while the Spearman and Kendall coefficients compare the [ranks](#) of data. There are several NumPy, SciPy, and Pandas correlation functions and methods that you can use to calculate these coefficients. You can also use [Matplotlib](#) to conveniently illustrate the results.



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## Example: NumPy Correlation

NumPy has many [statistics routines](#), including correlation. You can start by importing NumPy and defining two arrays, `x` and `y`:

Python

```
>>> import numpy as np
>>> x = np.arange(10, 20)
>>> x
array([10, 11, 12, 13, 14, 15, 16, 17, 18, 19])
>>> y = np.array([2, 1, 4, 5, 8, 12, 18, 25, 96, 48])
>>> y
array([ 2,  1,  4,  5,  8, 12, 18, 25, 96, 48])
```

```
1 # How to merge two dicts
2 # in Python 3.5+
3
4 >>> x = {'a': 1, 'b': 2}
5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

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Here, you use `np.arange()` to create an array `x` of integers between 10 (inclusive) and 20 (exclusive). Then you use `np.array()` to create a second array `y` containing arbitrary integers.

Once you have two arrays of the same length, you can call `np.corrcoef()` with both arrays as arguments:

Python

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```
>>> r = np.corrcoef(x, y)
>>> r
array([[1.          , 0.75864029],
       [0.75864029, 1.          ]])
>>> r[0, 1]
0.7586402890911867
>>> r[1, 0]
0.7586402890911869
```

`corrcoef()` returns the [correlation matrix](#), which is a two-dimensional array with the correlation coefficients. Here's a simplified version of the correlation matrix you just created:

Text

	x	y
x	1.00	0.76
y	0.76	1.00

The values on the main diagonal of the correlation matrix (upper left and lower right) are equal to 1. The upper left value corresponds to the correlation coefficient for `x` and `x`, while the lower right value is the correlation coefficient for `y` and `y`. They are always equal to 1.

However, what you usually need are the lower left and upper right values of the correlation matrix. These values are equal and both represent the **Pearson correlation coefficient** for `x` and `y`. In this case, it's approximately 0.76.

This figure shows the data points and the correlation coefficients for the above example:

```

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8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}

```

The red squares are the data points. As you can see, the values for `x` are the coefficients.

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## Example: SciPy Correlation Calculation

SciPy also has many statistics routines contained in `scipy.stats`. You can use the following methods to calculate the three correlation coefficients you saw earlier:

- `pearsonr()`
- `spearmanr()`
- `kendalltau()`

Here's how you would use these functions in Python:

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Python

>>>

```

>>> import numpy as np
>>> import scipy.stats
>>> x = np.arange(10, 20)
>>> y = np.array([2, 1, 4, 5, 8, 12, 18, 25, 96, 48])
>>> scipy.stats.pearsonr(x, y)      # Pearson's r
(0.7586402890911869, 0.010964341301680832)
>>> scipy.stats.spearmanr(x, y)    # Spearman's rho
SpearmanResult(correlation=0.9757575757575757, pvalue=1.4675461874042197e-06)
>>> scipy.stats.kendalltau(x, y)   # Kendall's tau
KendalltauResult(correlation=0.9111111111111111, pvalue=2.9761904761904762e-05)

```

Note that these functions return objects that contain two values:

1. The correlation coefficient
2. The [p-value](#)

You use the **p-value** in statistical methods when you're testing a hypothesis. The p-value is an important measure that requires in-depth knowledge of probability and statistics to interpret. To learn more about them, you can read about [the basics](#) or check out [a data scientist's explanation of p-values](#).

You can extract the p-values and the correlation coefficients with their indices, as the items of [tuples](#):

Python

>>>

```

>>> scipy.stats.pearsonr(x, y)[0]      # Pearson's r
0.7586402890911869
>>> scipy.stats.spearmanr(x, y)[0]    # Spearman's rho
0.9757575757575757
>>> scipy.stats.kendalltau(x, y)[0]   # Kendall's tau

```

```
0.911111111111111
```

You could also use dot notation for the Spearman and Kendall coefficients:

Python

```
>>> scipy.stats.spearmanr(x, y).correlation # Spearman's rho  
0.9757575757575757  
>>> scipy.stats.kendalltau(x, y).correlation # Kendall's tau  
0.911111111111111
```

The dot notation is longer, but it's also more explicit.

If you want to get the Pearson correlation coefficient value:

Python

```
>>> r, p = scipy.stats.pearsonr(x, y)  
>>> r  
0.7586402890911869  
>>> p  
0.010964341301680829
```

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This approach exploits [Python unpacking](#) and the fact that `pearsonr()` returns a tuple with these two statistics. You can also use this technique with `spearmanr()` and `kendalltau()`, as you'll see later on.



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## Example: Pandas Correlation Calculation

[Pandas](#) is, in some cases, more convenient than NumPy and SciPy for calculating statistics. It offers statistical methods for [Series](#) and [DataFrame](#) instances. For example, given two [Series](#) objects with the same number of items, you can call `.corr()` on one of them with the other as the first argument:

```
>>> import pandas as pd
>>> x = pd.Series(range(10, 20))
>>> x
0    10
1    11
2    12
3    13
4    14
5    15
6    16
7    17
8    18
9    19
dtype: int64
>>> y = pd.Series([2, 1, 4, 5, 8, 12,
>>> y
0    2
1    1
2    4
3    5
4    8
5   12
6   18
7   25
8   96
9   48
dtype: int64
>>> x.corr(y)           # Pearson's r
0.7586402890911867
>>> y.corr(x)
0.7586402890911869
>>> x.corr(y, method='spearman') # Spearman's rho
0.9757575757575757
>>> x.corr(y, method='kendall')  # Kendall's tau
0.9111111111111111
```

```
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5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

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Here, you use `.corr()` to calculate all three correlation coefficients. You define the desired statistic with the parameter `method`, which can take on one of several values:

- 'pearson'
- 'spearman'
- 'kendall'
- a callable

The callable can be any function, method, or [object with `\_\_call\_\_\(\)`](#) that accepts two one-dimensional arrays and returns a floating-point number.

## Linear Correlation

**Linear correlation** measures the proximity of the mathematical relationship between variables or dataset features to a linear function. If the relationship between the two features is closer to some linear function, then their linear correlation is stronger and the absolute value of the correlation coefficient is higher.

### Pearson Correlation Coefficient

Consider a dataset with two features: **x** and **y**. Each feature has  $n$  values, so **x** and **y** are  $n$ -tuples. Say that the first value  $x_1$  from **x** corresponds to the first value  $y_1$  from **y**, the second value  $x_2$  from **x** to the second value  $y_2$  from **y**, and so on. Then, there are  $n$  pairs of corresponding values:  $(x_1, y_1), (x_2, y_2)$ , and so on. Each of these  $x$ - $y$  pairs represents a single observation.

The **Pearson (product-moment) correlation coefficient** is a measure of the linear relationship between two features. It's the ratio of the covariance of **x** and **y** to the product of their standard deviations. It's often denoted with the letter **r** and called **Pearson's r**. You can express this value mathematically with this equation:

$$r = \frac{\sum_i ((x_i - \text{mean}(x))(y_i - \text{mean}(y)))}{(\sqrt{\sum_i (x_i - \text{mean}(x))^2} \sqrt{\sum_i (y_i - \text{mean}(y))^2})^{-1}}$$

Here,  $i$  takes on the values 1, 2, ...,  $n$ . The [mean values](#) of  $x$  and  $y$  are denoted with  $\text{mean}(x)$  and  $\text{mean}(y)$ . This formula shows that if larger  $x$  values tend to correspond to larger  $y$  values and vice versa, then  $r$  is positive. On the other hand, if larger  $x$  values are mostly associated with smaller  $y$  values and vice versa, then  $r$  is negative.

Here are some important facts about the Pearson correlation coefficient:

- The Pearson correlation coefficient can take on any real value in the range  $-1 \leq r \leq 1$ .
- The maximum value  $r = 1$  corresponds to a perfect positive linear relationship between  $x$  and  $y$ . In other words, larger  $x$  values correspond to larger  $y$  values.
- The value  $r > 0$  indicates positive correlation.
- The value  $r = 0$  corresponds to the case where there is no linear relationship.
- The value  $r < 0$  indicates negative correlation.
- The minimal value  $r = -1$  corresponds to a perfect negative linear relationship between  $x$  and  $y$ . In other words, larger  $x$  values correspond to smaller  $y$  values.

```

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6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}

```

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The above facts can be summed up in the following table.

Pearson's r Value	Correlation Between x and y
equal to 1	perfect positive linear relationship
greater than 0	positive correlation
equal to 0	no linear relationship
less than 0	negative correlation
equal to -1	perfect negative linear relationship

In short, a larger absolute value of  $r$  indicates stronger correlation, closer to a linear function. A smaller absolute value of  $r$  indicates weaker correlation.

## Linear Regression: SciPy Implementation

[Linear regression](#) is the process of finding the linear function that is as close as possible to the actual relationship between features. In other words, you determine the linear function that best describes the association between the features. This linear function is also called the [regression line](#).

You can implement linear regression with SciPy. You'll get the linear function that best approximates the relationship between two arrays, as well as the Pearson correlation coefficient. To get started, you first need to import the libraries and prepare some data to work with:

```

Python >>>
>>> import numpy as np
>>> import scipy.stats
>>> x = np.arange(10, 20)
>>> y = np.array([2, 1, 4, 5, 8, 12, 18, 25, 96, 48])

```

Here, you import `numpy` and `scipy.stats` and define the variables  $x$  and  $y$ .

You can use `scipy.stats.linregress()` to perform linear regression for two arrays of the same length. You should provide the arrays as the arguments and get the outputs by using dot notation:

```

Python >>>
>>> result = scipy.stats.linregress(x, y)
>>> result.slope
7.436363636363635
>>> result.intercept

```

```

    // result.intercept
-85.92727272727274
>>> result.rvalue
0.7586402890911869
>>> result.pvalue
0.010964341301680825
>>> result.stderr
2.257878767543913

```

That's it! You've completed the linear regression and gotten the following results:

- `.slope`: the slope of the regression line
- `.intercept`: the intercept of the regression line
- `.pvalue`: the p-value
- `.stderr`: the standard error of the estimate

You'll learn how to visualize these results.

You can also provide a single argument to `linregress()` of length two:

Python

```

>>> xy = np.array([[10, 11, 12, 13, 14, 15, 16, 17, 18, 19],
...                 [2, 1, 4, 5, 8, 12, 18, 25, 96, 48]])
>>> scipy.stats.linregress(xy)
LinregressResult(slope=7.4363636363636365, intercept=-85.927272727274, rvalue=0.7586402890911869, pvalue=0.

```

The result is exactly the same as the previous example because `xy` contains the same data as `x` and `y` together. `linregress()` took the first row of `xy` as one feature and the second row as the other feature.

**Note:** In the example above, `scipy.stats.linregress()` considers the rows as features and columns as observations. That's because there are two rows.

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The usual practice in [machine learning](#) is the opposite: rows are observations and columns are features. Many machine learning libraries, like Pandas, [Scikit-Learn](#), [Keras](#), and others, follow this convention.

You should be careful to note how the observations and features are indicated whenever you're analyzing correlation in a dataset.

`linregress()` will return the same result if you provide the [transpose](#) of `xy`, or a NumPy array with 10 rows and two columns. In NumPy, you can transpose a matrix in many ways:

- `.transpose()`
- `.__transpose__()`
- `.T`

Here's how you might transpose `xy`:

```

Python
>>> xy.T
array([[10,  2],
       [11,  1],
       [12,  4],
       [13,  5],
       [14,  8],
       [15, 12],
       [16, 18],
       [17, 25],
       [18, 96],
       [19, 48]])

```

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Now that you know how to get the transpose, you can pass one to `linregress()`. The first column will be one feature and the second column the other feature:

Python

>>>

```
>>> scipy.stats.linregress(xy.T)
LinregressResult(slope=7.4363636363636365, intercept=-85.92727272727274, rvalue=0.7586402890911869, pvalue=0.
```

Here, you use `.T` to get the transpose of `xy`. `linregress()` works the same way with `xy` and its transpose. It extracts the features by splitting the array along the d

You should also be careful to note whether learning, you'll often find some missing or Pandas is by using [NaN](#) or **Not a Number** result with `linregress()`:

Python

```
1 # How to merge two dicts
2 # in Python 3.5+
3
4 >>> x = {'a': 1, 'b': 2}
5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

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In this case, your resulting object returns all `nan` values. In Python, `nan` is a special floating-point value that you can get by using any of the following:

- `float('nan')`
- `math.nan`
- `numpy.nan`

You can also check whether a variable corresponds to `nan` with `math.isnan()` or `numpy.isnan()`.



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## Pearson Correlation: NumPy and SciPy Implementation

You've already seen how to get the Pearson correlation coefficient with `corrcoef()` and `pearsonr()`:

Python

>>>

```
>>> r, p = scipy.stats.pearsonr(x, y)
>>> r
0.7586402890911869
>>> p
0.010964341301680829
>>> np.corrcoef(x, y)
array([[1.          , 0.75864029],
       [0.75864029, 1.          ]])
```

Note that if you provide an array with a `nan` value to `pearsonr()`, you'll get a [ValueError](#).

There are few additional details worth considering. First, recall that `np.corrcoef()` can take two NumPy arrays as arguments. Instead, you can pass a single two-dimensional array with the same values as the argument:

Python

>>>

```
>>> np.corrcoef(xy)
array([[1.          ,  0.75864029],
       [0.75864029,  1.          ]])
```

The results are the same in this and previous examples. Again, the first row of `xy` represents one feature, while the second row represents the other.

If you want to get the correlation coefficients for three features, then you just provide a numeric two-dimensional array with three rows as the argument:

Python

```
>>> xyz = np.array([[10, 11, 12, 13,
...                  [2, 1, 4, 5, 8, 1
...                  [5, 3, 2, 1, 0, -
>>> np.corrcoef(xyz)
array([[ 1.          ,  0.75864029, -0.
       [ 0.75864029,  1.          , -0.
       [-0.96807242, -0.83407922,  1.
```

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X

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You'll obtain the correlation matrix again

Text

	x	y	z
x	1.00	0.76	-0.97
y	0.76	1.00	-0.83
z	-0.97	-0.83	1.00

This is because `corrcoef()` considers each row of `xyz` as one feature. The value `0.76` is the correlation coefficient for the first two features of `xyz`. This is the same as the coefficient Pearson's r for the first and second features, while `-0.83` is Pearson's r for the first and third features.

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Here's an interesting example of what happens when you pass `nan` data to `corrcoef()`:

Python

>>>

```
>>> arr_with_nan = np.array([[0, 1, 2, 3],
...                           [2, 4, 1, 8],
...                           [2, 5, np.nan, 2]])
>>> np.corrcoef(arr_with_nan)
array([[1.          ,  0.62554324,      nan],
       [0.62554324,  1.          ,      nan],
       [      nan,      nan,      nan]])
```

In this example, the first two rows (or features) of `arr_with_nan` are okay, but the third row `[2, 5, np.nan, 2]` contains a `nan` value. Everything that doesn't include the feature with `nan` is calculated well. The results that depend on the last row, however, are `nan`.

By default, `numpy.corrcoef()` considers the rows as features and the columns as observations. If you want the opposite behavior, which is widely used in machine learning, then use the argument `rowvar=False`:

Python

>>>

```
>>> xyz.T
array([[ 10,     2,     5],
       [ 11,     1,     3],
       [ 12,     4,     2],
       [ 13,     5,     1],
       [ 14,     8,     0],
       [ 15,    12,    -2],
       [ 16,    18,    -8],
       [ 17,    25,   -11],
       [ 18,    96,   -15],
       [ 19,    48,   -16]])
>>> np.corrcoef(xyz.T, rowvar=False)
```

```
array([[ 1.          ,  0.75864029, -0.96807242],
       [ 0.75864029,  1.          , -0.83407922],
       [-0.96807242, -0.83407922,  1.          ]])
```

This array is identical to the one you saw earlier. Here, you apply a different convention, but the result is the same.

## Pearson Correlation: Pandas Implementation

So far, you've used `Series` and `DataFrame` object methods to calculate correlation coefficients. Let's explore these methods in more detail. First, you need to import Pandas and create some instances of `Series` and `DataFrame`:

```
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8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

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Python

>>>

```
>>> import pandas as pd
>>> x = pd.Series(range(10, 20))
>>> x
0    10
1    11
2    12
3    13
4    14
5    15
6    16
7    17
8    18
9    19
dtype: int64
>>> y = pd.Series([2, 1, 4, 5, 8, 12, 18, 25, 96, 48])
>>> y
0     2
1     1
2     4
3     5
4     8
5    12
6    18
7    25
8    96
```

```

9     48
dtype: int64
>>> z = pd.Series([5, 3, 2, 1, 0, -2, -8, -11, -15, -16])
>>> z
0    5
1    3
2    2
3    1
4    0
5   -2
6   -8
7   -11
8  -15
9  -16
dtype: int64
>>> xy = pd.DataFrame({'x-values': x,
>>> xy
   x-values  y-values
0         10        2
1         11        1
2         12        4
3         13        5
4         14        8
5         15       12
6         16       18
7         17       25
8         18       96
9         19       48
>>> xyz = pd.DataFrame({'x-values': x, 'y-values': y, 'z-values': z})
>>> xyz
   x-values  y-values  z-values
0         10        2        5
1         11        1        3
2         12        4        2
3         13        5        1
4         14        8        0
5         15       12       -2
6         16       18       -8
7         17       25      -11
8         18       96      -15
9         19       48      -16

```

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You now have three Series objects called x, y, and z. You also have two DataFrame objects, xy and xyz.

**Note:** When you work with DataFrame instances, you should be aware that the rows are observations and the columns are features. This is consistent with the usual practice in machine learning.

You've already learned how to use .corr() with Series objects to get the Pearson correlation coefficient:

```

Python >>>
>>> x.corr(y)
0.7586402890911867

```

Here, you call .corr() on one object and pass the other as the first argument.

If you provide a nan value, then .corr() will still work, but it will exclude observations that contain nan values:

```

Python >>>
>>> u, u_with_nan = pd.Series([1, 2, 3]), pd.Series([1, 2, np.nan, 3])
>>> v, w = pd.Series([1, 4, 8]), pd.Series([1, 4, 154, 8])
>>> u.corr(v)
0.9966158955401239
>>> u_with_nan.corr(w)
0.9966158955401239

```

You get the same value of the correlation coefficient in these two examples. That's because .corr() ignores the pair of values (np.nan, 154) that has a missing value.

You can also use [.corr\(\)](#) with DataFrame objects. You can use it to get the correlation matrix for their columns:

Python

```
>>> corr_matrix = xy.corr()  
>>> corr_matrix  
          x-values  y-values  
x-values    1.00000  0.75864  
y-values    0.75864  1.00000
```

>>>

The resulting correlation matrix is a new instance of `DataFrame` and holds the correlation coefficients for the columns `xy['x-values']` and `xy['y-values']`. Such labeled results are usually very convenient to work with because you can access them with either their labels or their positions:

Python

```
>>> corr_matrix.at['x-values', 'y-values']  
0.7586402890911869  
>>> corr_matrix.iat[0, 1]  
0.7586402890911869
```

```
1 # How to merge two dicts  
2 # in Python 3.5+  
3  
4 >>> x = {'a': 1, 'b': 2}  
5 >>> y = {'b': 3, 'c': 4}  
6  
7 >>> z = {**x, **y}  
8  
9 >>> z  
10 {'c': 4, 'a': 1, 'b': 3}
```

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This example shows two ways of accessing values:

1. Use `.at[]` to access a single value by its labels.
2. Use `.iat[]` to access a value by the positions of its row and column.

You can apply `.corr()` the same way with `DataFrame` objects that contain three or more columns:

Python

```
>>> xyz.corr()  
          x-values  y-values  z-values  
x-values    1.00000  0.758640 -0.968072  
y-values    0.758640  1.000000 -0.834079  
z-values   -0.968072 -0.834079  1.000000
```

>>>

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You'll get a correlation matrix with the following correlation coefficients:

- 0.758640 for `x-values` and `y-values`
- -0.968072 for `x-values` and `z-values`
- -0.834079 for `y-values` and `z-values`

Another useful method is `.corrwith()`, which allows you to calculate the correlation coefficients between the rows or columns of one `DataFrame` object and another `Series` or `DataFrame` object passed as the first argument:

Python

```
>>> xy.corrwith(z)  
x-values   -0.968072  
y-values   -0.834079  
dtype: float64
```

>>>

In this case, the result is a new `Series` object with the correlation coefficient for the column `xy['x-values']` and the values of `z`, as well as the coefficient for `xy['y-values']` and `z`.

`.corrwith()` has the optional parameter `axis` that specifies whether columns or rows represent the features. The default value of `axis` is 0, and it also defaults to columns representing features. There's also a `drop` parameter, which indicates what to do with missing values.

Both `.corr()` and `.corrwith()` have the optional parameter `method` to specify the correlation coefficient that you want to calculate. The Pearson correlation coefficient is returned by default, so you don't need to provide it in this case.



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# Rank Correlation

**Rank correlation** compares the ranks or the orderings of the data related to two variables or dataset features. If the orderings are similar, then the correlation is strong, positive, and high. However, if the orderings are close to reversed, then the correlation is strong, negative, and low. In other words, rank correlation is concerned only with the order of values, not with the particular values from the dataset.

To illustrate the difference between linear and rank correlation, consider the following figure:

```
1 # How to merge two dicts
2 # in Python 3.5+
3
4 >>> x = {'a': 1, 'b': 2}
5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

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The left plot has a perfect positive linear correlation and the right one shows negative correlation. However, neither of them is a linear function, so  $r$  is different than  $-1$  or  $1$ .

When you look only at the orderings or ranks, all three relationships are perfect! The left and central plots show the observations where larger  $x$  values always correspond to larger  $y$  values. This is perfect positive rank correlation. The right plot illustrates the opposite case, which is perfect negative rank correlation.

## Spearman Correlation Coefficient

The **Spearman correlation coefficient** between two features  rank values. It's calculated the same way as the Pearson correlation coefficient, but instead of their values. It's often denoted with the Greek letter rho ( $\rho$ ) and called **Spearman's rho**.

Say you have two n-tuples,  $\mathbf{x}$  and  $\mathbf{y}$ , where  $(x_1, y_1), (x_2, y_2), \dots$  are the observations as pairs of corresponding values. You can calculate the Spearman correlation coefficient  $\rho$  the same way as the Pearson coefficient. You'll use the ranks instead of the actual values from  $\mathbf{x}$  and  $\mathbf{y}$ .

Here are some important facts about the Spearman correlation coefficient:

- It can take a real value in the range  $-1 \leq \rho \leq 1$ .
- Its maximum value  $\rho = 1$  corresponds to the case when there's a [monotonically](#) increasing function between  $\mathbf{x}$  and  $\mathbf{y}$ . In other words, larger  $x$  values correspond to larger  $y$  values and vice versa.
- Its minimum value  $\rho = -1$  corresponds to the case when there's a monotonically decreasing function between  $\mathbf{x}$  and  $\mathbf{y}$ . In other words, larger  $x$  values correspond to smaller  $y$  values and vice versa.

You can calculate Spearman's rho in Python in a very similar way as you would Pearson's  $r$ .

## Kendall Correlation Coefficient

Let's start again by considering two n-tuples,  $\mathbf{x}$  and  $\mathbf{y}$ . Each of the  $x$ - $y$  pairs  $(x_1, y_1), (x_2, y_2), \dots$  is a single observation. A pair of observations  $(x_i, y_i)$  and  $(x_j, y_j)$ , where  $i < j$ , will be one of three things:

- **concordant** if either  $(x_i > x_j \text{ and } y_i > y_j)$  or  $(x_i < x_j \text{ and } y_i < y_j)$
- **discordant** if either  $(x_i < x_j \text{ and } y_i > y_j)$  or  $(x_i > x_j \text{ and } y_i < y_j)$
- **neither** if there's a tie in  $\mathbf{x}$  ( $x_i = x_j$ ) or a tie in  $\mathbf{y}$  ( $y_i = y_j$ )

The **Kendall correlation coefficient** compares the number of concordant and discordant pairs of data. This coefficient is based on the difference in the counts of concordant and discordant pairs relative to the number of  $x$ - $y$  pairs. It's often denoted with the Greek letter tau ( $\tau$ ) and called **Kendall's tau**.

According to the [scipy.stats official docs](#), the Kendall correlation coefficient is calculated as  $\tau = (n^+ - n^-) / \sqrt{(n^+ + n^- + n^0)} / n$

$n^+ (n^+ + n^- + n^y)$ , where:

- $n^+$  is the number of concordant pairs
- $n^-$  is the number of discordant pairs
- $n^x$  is the number of ties only in  $x$
- $n^y$  is the number of ties only in  $y$

If a tie occurs in both  $x$  and  $y$ , then it's not included in either  $n^x$  or  $n^y$ .

The [Wikipedia page](#) on Kendall rank correlation coefficient gives the following expression:  $\tau = (2 / (n(n - 1))) \sum_{i < j} (\text{sign}(x_i - x_j) \text{sign}(y_i - y_j))$  for  $i < j$ , where  $i = 1, 2, \dots, n > 0$ .  $n(n - 1) / 2$  is the total number of  $x$ - $y$  pairs.

Some important facts about the Kendall rank correlation coefficient:

- It can take a real value in the range  $[-1, 1]$ .
- Its maximum value  $\tau = 1$  corresponds to all pairs being concordant. In other words, all pairs are correctly ordered.
- Its minimum value  $\tau = -1$  corresponds to all pairs being discordant. In other words, all pairs are discordant.

```
1 # How to merge two dicts
2 # in Python 3.5+
3
4 >>> x = {'a': 1, 'b': 2}
5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

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You can calculate Kendall's tau in Python similarly to how you would calculate Pearson's r.



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## Rank: SciPy Implementation

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You can use `scipy.stats` to determine the rank for each value in an array. First, you'll import the libraries and create NumPy arrays:

```
Python >>>
>>> import numpy as np
>>> import scipy.stats
>>> x = np.arange(10, 20)
>>> y = np.array([2, 1, 4, 5, 8, 12, 18, 25, 96, 48])
>>> z = np.array([5, 3, 2, 1, 0, -2, -8, -11, -15, -16])
```

Now that you've prepared data, you can determine the rank of each value in a NumPy array with `scipy.stats.rankdata()`:

```
Python >>>
>>> scipy.stats.rankdata(x)
array([ 1.,  2.,  3.,  4.,  5.,  6.,  7.,  8.,  9., 10.])
>>> scipy.stats.rankdata(y)
array([ 2.,  1.,  3.,  4.,  5.,  6.,  7.,  8., 10.,  9.])
>>> scipy.stats.rankdata(z)
array([10.,  9.,  8.,  7.,  6.,  5.,  4.,  2.,  1.])
```

The arrays  $x$  and  $z$  are monotonic, so their ranks are monotonic as well. The smallest value in  $y$  is 1 and it corresponds to the rank 1. The second smallest is 2, which corresponds to the rank 2. The largest value is 96, which corresponds to the largest rank 10 since there are 10 items in the array.

`rankdata()` has the optional parameter `method`. This tells Python what to do if there are ties in the array (if two or more values are equal). By default, it assigns them the average of the ranks:

```
Python >>>
>>> scipy.stats.rankdata([8, 2, 0, 2])
array([4., 2.5, 1., 2.5])
```

There are two elements with a value of 2 and they have the ranks 2.0 and 3.0. The value 0 has rank 1.0 and the value 8 has rank 4.0. Then, both elements with the value 2 will get the same rank 2.5.

`rankdata()` treats nan values as if they were large:

Python

```
>>> scipy.stats.rankdata([8, np.nan, 0, 2])
array([3., 4., 1., 2.])
```

>>>

In this case, the value `np.nan` corresponds to a rank of 2.5.

Python

```
>>> np.argsort(y) + 1
array([ 2,  1,  3,  4,  5,  6,  7,  8,  9, 10])
```

```
1 # How to merge two dicts
2 # in Python 3.5+
3
4 >>> x = {'a': 1, 'b': 2}
5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

`argsort()` returns the indices that the array `y`. You'll need to add 1 to all of them.

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## Rank Correlation: NumPy and SciPy Implementation

You can calculate the Spearman correlation coefficient with `scipy.stats.spearmanr()`:

Python

```
>>> result = scipy.stats.spearmanr(x, y)
>>> result
SpearmanResult(correlation=0.9757575757575757, pvalue=1.4675461874042197e-06)
>>> result.correlation
0.9757575757575757
>>> result.pvalue
1.4675461874042197e-06
>>> rho, p = scipy.stats.spearmanr(x, y)
>>> rho
0.9757575757575757
>>> p
1.4675461874042197e-06
```

Improve Your Python

`spearmanr()` returns an object that contains the value of the Spearman correlation coefficient and p-value. As you can see, you can access particular values in two ways:

1. Using dot notation (`result.correlation` and `result.pvalue`)
2. Using Python unpacking (`rho, p = scipy.stats.spearmanr(x, y)`)

You can get the same result if you provide the two-dimensional array `xy` that contains the same data as `x` and `y` to `spearmanr()`:

Python

```
>>> xy = np.array([[10, 11, 12, 13, 14, 15, 16, 17, 18, 19],
...                 [2, 1, 4, 5, 8, 12, 18, 25, 96, 48]])
>>> rho, p = scipy.stats.spearmanr(xy, axis=1)
>>> rho
0.9757575757575757
>>> p
1.4675461874042197e-06
```

>>>

The first row of `xy` is one feature, while the second row is the other feature. You can modify this. The optional parameter `axis` determines whether columns (`axis=0`) or rows (`axis=1`) represent the features. The default behavior is that the rows are observations and the columns are features.

Another optional parameter `nan_policy` defines how to handle nan values. It can take one of three values:

- '`propagate`' returns nan if there's a nan value among the inputs. This is the default behavior.
- '`raise`' raises a `ValueError` if there's a nan value among the inputs.

- `'omit'` ignores the observations with nan values.

If you provide a two-dimensional array with more than two features, then you'll get the correlation matrix and the matrix of the p-values:

Python

```
>>> xyz = np.array([[10, 11, 12, 13, 14, 15, 16, 17, 18, 19],
...                 [2, 1, 4, 5, 8, 12, 18, 25, 96, 48],
...                 [5, 3, 2, 1, 0, -2, -8, -11, -15, -16]])
>>> corr_matrix, p_matrix = scipy.stats.spearmanr(xyz, axis=1)
>>> corr_matrix
array([[ 1.          ,  0.97575758, -1.
       [ 0.97575758,  1.          , -0.
       [-1.          , -0.97575758,  1.
>>> p_matrix
array([[6.64689742e-64, 1.46754619e-6
       [1.46754619e-06, 6.64689742e-6
       [6.64689742e-64, 1.46754619e-6
```

The value `-1` in the correlation matrix shows that is that larger values in the first row are

You can obtain the Kendall correlation coefficient with `kendalltau()`:

Python

```
>>> result = scipy.stats.kendalltau(x, y)
>>> result
KendalltauResult(correlation=0.911111111111111, pvalue=2.9761904761904762e-05)
>>> result.correlation
0.911111111111111
>>> result.pvalue
2.9761904761904762e-05
>>> tau, p = scipy.stats.kendalltau(x, y)
>>> tau
0.911111111111111
>>> p
2.9761904761904762e-05
```

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`kendalltau()` works much like `spearmanr()`. It takes two one-dimensional arrays, has the optional parameter `nan_policy`, and returns an object with the values of the correlation coefficient and p-value.

However, if you provide only one two-dimensional array as an argument, then `kendalltau()` will raise a [TypeError](#). If you pass two multi-dimensional arrays of the same shape, then they'll be flattened before the calculation.



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## Rank Correlation: Pandas Implementation

You can calculate the Spearman and Kendall correlation coefficients with Pandas. Just like before, you start by importing `pandas` and creating some `Series` and `DataFrame` instances:

Python

```
>>> import pandas as pd
>>> x, y, z = pd.Series(x), pd.Series(y), pd.Series(z)
>>> xy = pd.DataFrame({'x-values': x, 'y-values': y})
>>> xyz = pd.DataFrame({'x-values': x, 'y-values': y, 'z-values': z})
```

»

Now that you have these Pandas objects, you can use `.corr()` and `.corrwith()` just like you did when you calculated the Pearson correlation coefficient. You just need to specify the desired correlation coefficient with the optional parameter `method`, which defaults to `'pearson'`.

To calculate Spearman's rho, pass `method=spearman`:

Python

```
>>> x.corr(y, method='spearman')
0.9757575757575757
>>> xy.corr(method='spearman')
      x-values  y-values
x-values  1.000000  0.975758
y-values  0.975758  1.000000
>>> xyz.corr(method='spearman')
      x-values  y-values  z-values
x-values  1.000000  0.975758 -1.000000
y-values  0.975758  1.000000 -0.975758
z-values -1.000000 -0.975758  1.000000
>>> xy.corrwith(z, method='spearman')
x-values   -1.000000
y-values   -0.975758
dtype: float64
```

```
1 # How to merge two dicts
2 # in Python 3.5+
3
4 >>> x = {'a': 1, 'b': 2}
5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

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If you want Kendall's tau, then you use `method=kendall`:

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Python

```
>>> x.corr(y, method='kendall')
0.9111111111111111
>>> xy.corr(method='kendall')
      x-values  y-values
x-values  1.000000  0.911111
y-values  0.911111  1.000000
>>> xyz.corr(method='kendall')
      x-values  y-values  z-values
x-values  1.000000  0.911111 -1.000000
y-values  0.911111  1.000000 -0.911111
z-values -1.000000 -0.911111  1.000000
>>> xy.corrwith(z, method='kendall')
x-values   -1.000000
y-values   -0.911111
dtype: float64
```

>>>

As you can see, unlike with SciPy, you can use a single two-dimensional data structure (a dataframe).

## Visualization of Correlation

**Data visualization** is very important in statistics and data science. It can help you better understand your data and give you a better insight into the relationships between features. In this section, you'll learn how to visually represent the relationship between two features with an x-y plot. You'll also use heatmaps to visualize a correlation matrix.

You'll learn how to prepare data and get certain visual representations, but you won't cover many other explanations. To learn more about Matplotlib in-depth, check out [Python Plotting With Matplotlib \(Guide\)](#). You can also take a look at the [official documentation](#) and [Anatomy of Matplotlib](#).

To get started, first import `matplotlib.pyplot`:

Python

>>>

```
>>> import matplotlib.pyplot as plt  
>>> plt.style.use('ggplot')
```

Here, you use `plt.style.use('ggplot')` to set the style of the plots. Feel free to skip this line if you want.

You'll use the arrays `x`, `y`, `z`, and `xyz` from the previous sections. You can create them again to cut down on scrolling:

Python

```
>>> import numpy as np  
>>> import scipy.stats  
>>> x = np.arange(10, 20)  
>>> y = np.array([2, 1, 4, 5, 8, 12,  
>>> z = np.array([5, 3, 2, 1, 0, -2,  
>>> xyz = np.array([[10, 11, 12, 13,  
...           [2, 1, 4, 5, 8, 1  
...           [5, 3, 2, 1, 0, -
```

```
1 # How to merge two dicts  
2 # in Python 3.5+  
3  
4 >>> x = {'a': 1, 'b': 2}  
5 >>> y = {'b': 3, 'c': 4}  
6  
7 >>> z = {**x, **y}  
8  
9 >>> z  
10 {'c': 4, 'a': 1, 'b': 3}
```

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Now that you've got your data, you're ready to plot.

## X-Y Plots With a Regression Line

First, you'll see how to create an x-y plot with the regression line, its equation, and the Pearson correlation coefficient. You can get the slope and the intercept of the regression line, as well as the correlation coefficient, with `linregress()`:

Python

```
>>> slope, intercept, r, p, stderr = scipy.stats.linref
```

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>>>

Now you have all the values you need. You can also get the string with the equation of the regression line and the value of the correlation coefficient. [f-strings](#) are very convenient for this purpose:

Python

```
>>> line = f'Regression line: y={intercept:.2f}+{slope:.2f}x, r={r:.2f}'  
>>> line  
'Regression line: y=-85.93+7.44x, r=0.76'
```

>>>

Now, create the x-y plot with [plt.plot\(\)](#):

Python

```
fig, ax = plt.subplots()  
ax.plot(x, y, linewidth=0, marker='s', label='Data points')  
ax.plot(x, intercept + slope * x, label=line)  
ax.set_xlabel('x')  
ax.set_ylabel('y')  
ax.legend(facecolor='white')  
plt.show()
```

Your output should look like this:

The red squares represent the observations, while the blue line is the regression line. Its equation is listed in the legend, together with the correlation coefficient.



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```
1 # How to merge two dicts
2 # in Python 3.5+
3
4 >>> x = {'a': 1, 'b': 2}
5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

## Heatmaps of Correlation M

The correlation matrix can become really present it visually as a heatmap where ea correlation matrix:

Python

```
>>> corr_matrix = np.corrcoef(xyz).round(decimals=2)
>>> corr_matrix
array([[ 1. ,  0.76, -0.97],
       [ 0.76,  1. , -0.83],
       [-0.97, -0.83,  1. ]])
```

It can be convenient for you to round the numbers in the co shown be on the heatmap.

Finally, create your heatmap with [.imshow\(\)](#) and the correlation matrix as its argument:

Python

```
fig, ax = plt.subplots()
im = ax.imshow(corr_matrix)
im.set_clim(-1, 1)
ax.grid(False)
ax.xaxis.set(ticks=(0, 1, 2), ticklabels=('x', 'y', 'z'))
ax.yaxis.set(ticks=(0, 1, 2), ticklabels=('x', 'y', 'z'))
ax.set_xlim(2.5, -0.5)
for i in range(3):
    for j in range(3):
        ax.text(j, i, corr_matrix[i, j], ha='center', va='center',
                color='r')
cbar = ax.figure.colorbar(im, ax=ax, format='% .2f')
plt.show()
```

Your output should look like this:

```
1 # How to merge two dicts
2 # in Python 3.5+
3
4 >>> x = {'a': 1, 'b': 2}
5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

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The result is a table with the coefficients. It sort of looks like the Pandas output with colored backgrounds. The colors help you interpret the output. In this example, the yellow color represents the number 1, green corresponds to 0.76, and purple is used for the negative numbers.

## Conclusion

You now know that **correlation coefficients** are statistics that measure the association between variables or features of datasets. They're very important in data science and machine learning.

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You can now use Python to calculate:

- **Pearson's** product-moment correlation coefficient
- **Spearman's** rank correlation coefficient
- **Kendall's** rank correlation coefficient

Now you can use NumPy, SciPy, and Pandas correlation functions and methods to effectively calculate these (and other) statistics, even when you work with large datasets. You also know how to **visualize** data, regression lines, and correlation matrices with Matplotlib plots and heatmaps.

If you have any questions or comments, please put them in the comments section below!

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## Python Tricks

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```
1 # How to merge two dicts
2 # in Python 3.5+
3
4 >>> x = {'a': 1, 'b': 2}
5 >>> y = {'b': 3, 'c': 4}
6
7 >>> z = {**x, **y}
8
9 >>> z
10 {'c': 4, 'a': 1, 'b': 3}
```

## About Mirko Stojiljković

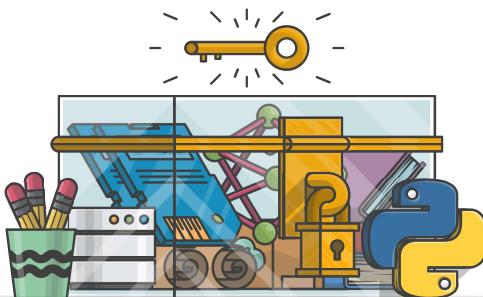
Mirko has a Ph.D. in Mechanical Engineering and works as a university professor. He is a Pythonist who applies hybrid optimization and machine learning methods to support decision making in the energy sector.

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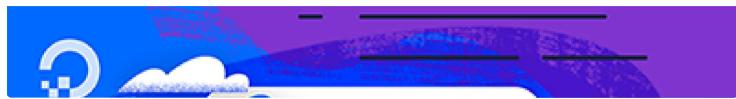
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