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Moore's Law is one small component in an exponentially growing planetary computing ecosystem.

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Exponential Laws of Computing Growth

IN A FORECASTING exercise, Gordon Earle Moore, co-founder of Intel, plotted data on the number of components—transistors, resistors, and capacitors—in chips made from 1959 to 1965. He saw an approximate straight line on log paper (see Figure 1). Extrapolating the line, he speculated that the number of components would grow from 2^6 in 1965 to 2^{16} in 1975, doubling every year. His 1965–1975 forecast came true. In 1975, with more data, he revised the estimate of the doubling period to two years. In those days, doubling components also doubled chip speed because the greater number of components could perform more powerful operations and smaller circuits allowed faster clock speeds. Later, Moore's Intel colleague David House claimed the doubling time

for speed should be taken as 18 months because of increasing clock speed, whereas Moore maintained that the doubling time for components was 24 months. But clock speed stabilized around 2000 because faster speeds caused more heat dissipation than chips could withstand. Since then, the faster speeds are achieved with multicore chips at the same clock frequency.

Moore's Law is one of the most durable technology forecasts ever made.^{10,20,31,33} It is the emblem of the information age, the relentless march of the computer chip enabling a technical, economic, and social revolution never before experienced by humanity.

The standard explanation for Moore's Law is that the law is not really a law at all, but only an empirical, self-fulfilling relationship driven by economic forces. This explanation is too weak, however, to explain why the law has worked for more than 50 years and why exponential growth works not only at the chip level but also at the system and market levels. Consider two prominent cases of systems evolution.

Supercomputers are complete systems, including massively parallel arrays of chips, interconnection networks, memory systems, caches, I/O systems, cooling systems, languages for expressing parallel computations, and compilers. Various groups have tracked these systems over the years. Figure 2 is a composite graph of data from these groups on the speeds of the fastest computers since 1940. The performance of these computers has grown exponentially. One of

» key insights

- Exponential growth seems to be unique to computing and information technologies and their markets, stimulating continued economic, social, and political disruptions.
- Exponential growth occurs simultaneously at all levels of the computing ecosystem—chips, systems, adopting communities.
- Technology jumping sustains exponential growth as companies switch to new technologies when the current ones reach their points of diminishing return.

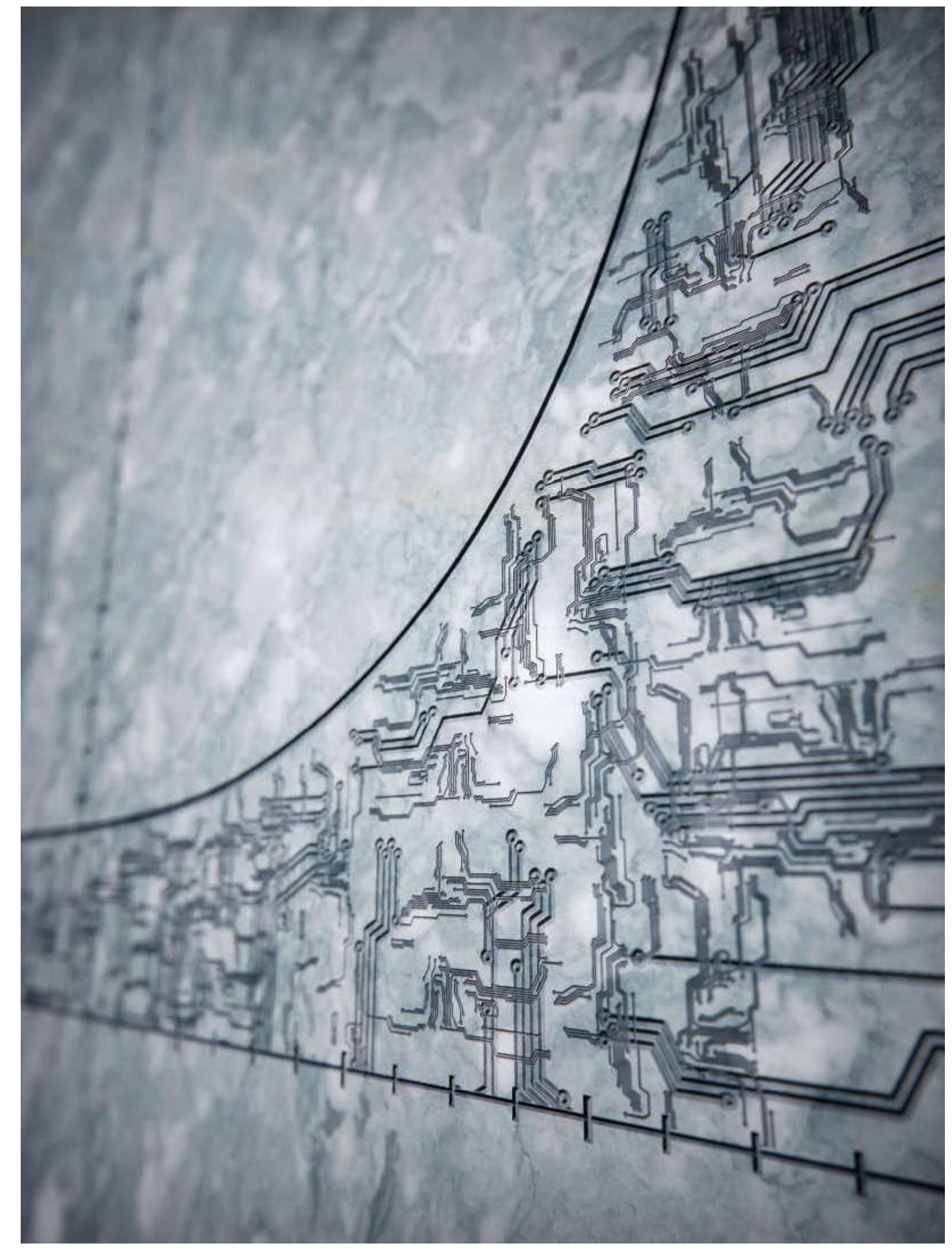


Figure 1. Moore's original prediction graph showed component count followed a straight line when plotted on log paper.²⁶

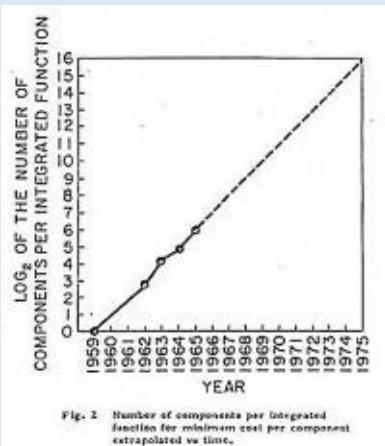
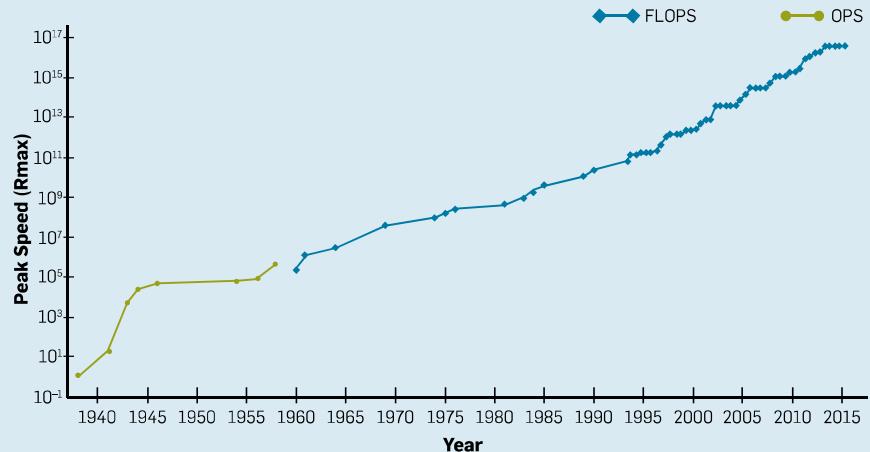


Figure 2. Speeds of the fastest computers from 1940 show an exponential rise in speed. From 1965 to 2015, the growth was a factor of 12 orders of 10 over 50 years, or a doubling approximately every 1.3 years.



Source: Wikipedia Creative Commons.

the tracking groups, TOP500 (<https://www.top500.org/>), has used a Linpack benchmark since 1993 to compare the fastest machines at each point in time for mathematical software, noting that the growth rate may be slowing because the market for such machines is slowing. The speeds of supercomputing systems depend on at least eight technologies besides the chips. How do we explain the exponential growth in this case?

Ray Kurzweil, futurist and author of *The Singularity Is Near: When Humans Transcend Biology*, formulated a set of predictions about information technology by constructing a graph of the computational speed growth over five generations of information technol-

ogy (see Figure 3).²⁵ He projected that this remarkable exponential doubling trend would continue for another 100 years, relying on jumps to new technologies every couple of decades. He also forecast a controversial claim—a “singularity” around 2040 when artificial intelligence will exceed human intelligence.^{25,32} The exponential growth in this case clearly does not depend on Moore's Law at all. How do we explain the exponential growth in this case?

The three kinds of exponential growth, as noted—doubling of components, speeds, and technology adoptions—have all been lumped under the heading of Moore's Law. Because the

original Moore's Law applies only to components on chips, not to systems or families of technologies, other phenomena must be at work. We will use the term “Moore's Law” for the component-doubling rule Moore proposed and “exponential growth” for all the other performance measures that plot as straight lines on log paper. What drives the exponential growth effect? Can we continue to expect exponential growth in the computational power of our technologies?

Exponential growth depends on three levels of adoption in the computing ecosystem (see the table here). The chip level is the domain of Moore's Law, as noted. However, the faster chips cannot realize their potential unless the host computer system supports the faster speeds and unless application workloads provide sufficient parallel computational work to keep the chips busy. And the faster systems cannot reach their potential without rapid adoption by the user community. The improvement process at all three levels must be exponential; otherwise, the system or community level would be a bottleneck, and we would not observe the effects often described as Moore's Law.

With supporting mathematical models, we will show what enables exponential doubling at each level. Information technology may be unique in being able to sustain exponential growth at

Three levels of exponential growth in the computing ecosystem.

Level	Explanation
Chip	Chip designers found technology paths for reducing component dimensions using Dennard Scaling ⁶ until around 2000, when heat-dissipation problems prevented clocks faster than about 3GHz. Since then, they have considered a host of methods, including multicore and clock distribution, to reduce power consumption and keep the components busy.
System	Improvements in chips, parallelism, cache, memory interconnects, networks, languages, compilers, and cooling enable a computer system to periodically double its speed and relieve performance bottlenecks in the system. Data-intensive workloads present a wealth of parallel threads sufficient to keep any multicore system busy.
Community	New system generations are highly attractive innovation enablers, and their adoption spreads exponentially in user communities.

all three levels. We will conclude that Moore's Law and exponential doubling have scientific bases. Moreover, the exponential doubling process is likely to continue across multiple technologies for decades to come.

Self-Fulfillment

The continuing achievement signified by Moore's Law is critically important to the digital economy. Economist Richard G. Anderson said, "Numerous studies have traced the cause of the productivity acceleration to technological innovations in the production of semiconductors that sharply reduced the prices of such components and of the products that contain them (as well as expanding the capabilities of such products)."¹ Robert Colwell, Director of DARPA's Microsystems Technology Office, echoes the same conclusion, which is why DARPA has invested in overcoming technology bottlenecks in post-Moore's-Law technologies.⁵ If and when Moore's Law ends, that end's impact on the economy will be profound.

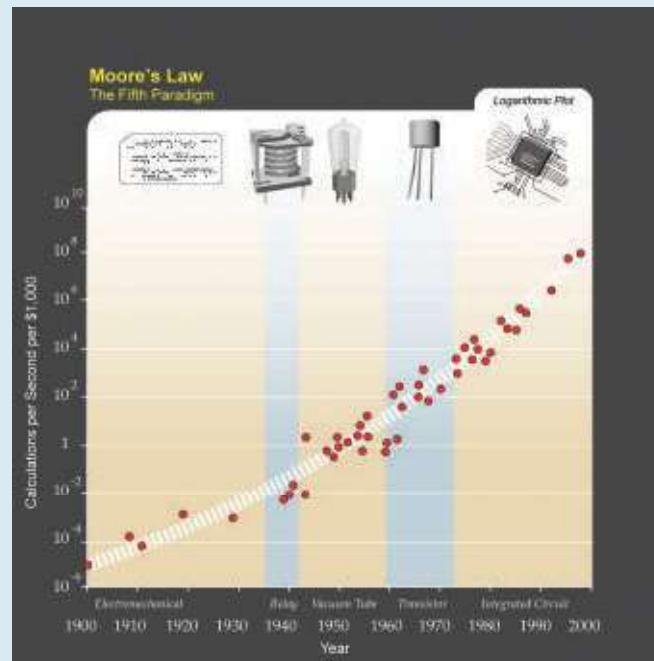
It is no wonder then that the standard explanation of the law is economic; it became a self-fulfilling prophecy of all chip companies to push the technology to meet the expected exponential growth and sustain their markets. A self-fulfilling prophecy is a prediction that causes itself to become true. For most of the past 50-plus years of computing, designers have emphasized performance. Faster is better. To achieve greater speed, chip architects increased component density by adding more registers, higher-level functions, cache memory, and multiple cores to the same chip area and the same power dissipation. Moore's Law became a design objective.

Designers optimize placement of components on highly constrained real estate, seeking to fill every square nanometer of area. Doubling component density—and therefore the number of components per nanometer of area—was not an outrageous objective because it requires only a reduction of 30% in both dimensions of 2D components. To achieve the next generation of Moore's Law, designers halve the area of each component, which means reducing each dimension to $\sqrt{1/2} = 0.71$ of its former value; we call this the "square

root reduction rule." Figure 4 shows that the die size of chips has consistently followed this rule over many generations. Wu et al.³² extended a

quantum-limit argument offered by Nobel physicist Richard Feynman¹² in 1985 to conclude that this downward scaling process could continue until

Figure 3. Kurzweil's graph of speed of information technologies since 1900 spans five families of technologies. From 1900 to 2000, the growth was 14 orders of 10 over 100 years, or a doubling approximately every 1.3 years.



Source: <http://www.kurzweilai.net>

Figure 4. Logarithm of actual versus predicted feature size since 1970 matches a straight line with regression coefficient $R^2 = 0.97$. Future sizes are predicted by dividing the previous size by $\sqrt{2}$; see the open triangles and dotted line. Future sizes two generations into the future are close to half the current sizes; see the square dots.

Data from David Harris, Lecture 21: "Scaling and Economics," Harvey Mudd College, Claremont, CA, 2004 (<http://pages.hmc.edu/harris/class/e158/04/lect21.pdf>) and Zvi Or-Bach, "Is the Cost Reduction Associated with Scaling Over?" Monolithic3D, San Jose, CA, 2004 (<http://www.monolithic3d.com/blog/is-the-cost-reduction-associated-with-scaling-over>).

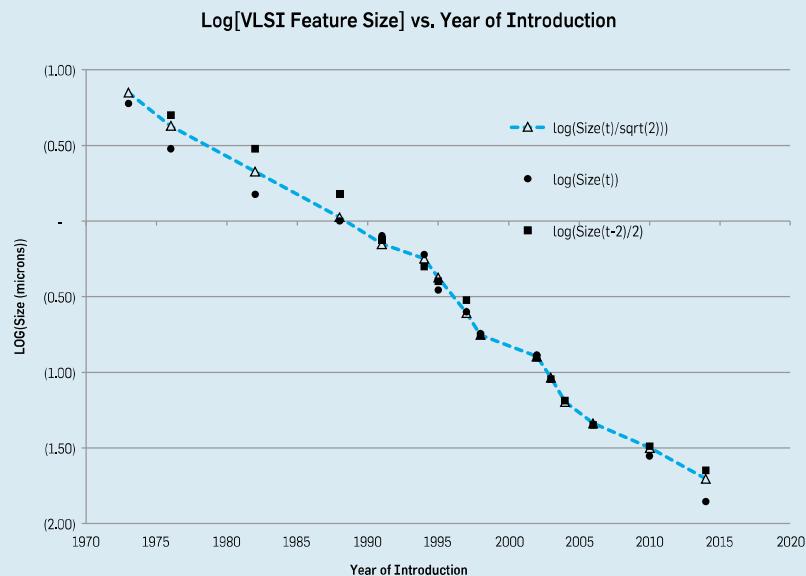


Figure 5. Computer subsystems are organized as stateless logic circuits (AND, OR, NOT gates without feedback loops) driving flip-flops that record the subsystem's state. Clock pulses trigger the flip-flops (x_1, \dots, x_k) to assume the states generated by the logic outputs. Too short a clock interval risks a metastable state because the logic outputs driving the flip-flops may not have settled since the last clock pulse.

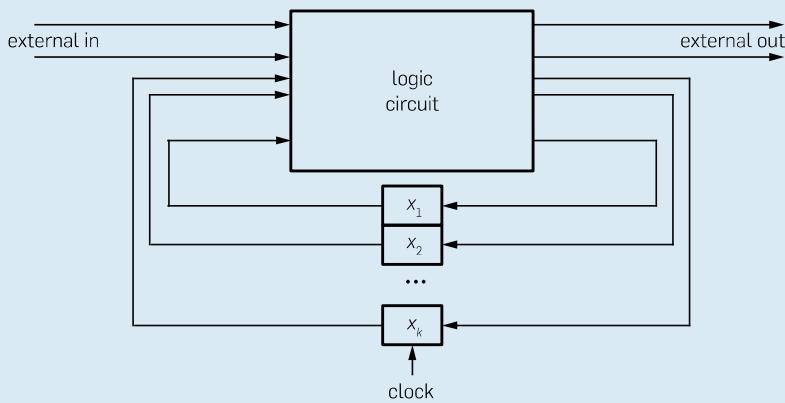
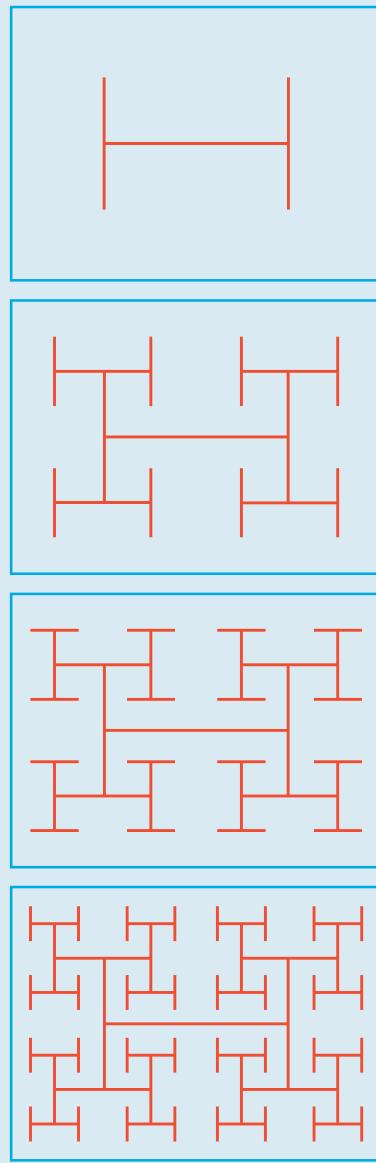


Figure 6. Four iterations of the space-filling H-tree fractal show how to quadruple the number of terminal nodes by halving the size of each "H." Each iteration appends a half-size "H" to the terminal nodes of the previous "H." A clock signal is injected at the center and arrives at all the terminal nodes simultaneously because the H-tree is balanced; see <http://www.tamurajones.net/FractalGenealogy.xhtml>



device sizes approached the Compton wavelength of an electron, which will happen by approximately 2036.

Motivated by the promise of enormous economic payoffs, designers overcame many challenges to sustain this rule. Even so, we find self-fulfillment to be an unsatisfying explanation of the persistence of Moore's Law. Why does the law not work for other technologies? What if systems had too many bottlenecks or workloads contained insufficient parallelism? What if people failed to adopt new technologies?

Moore's Law at the Chip Level

What is special about information technologies that makes exponential growth a possibility? This possibility is not available for every technology. We might wish for automobiles that travel 1,600 miles on a gallon of gasoline—approximately six doublings (2^6) better than today's most efficient automobiles—but wishing will not make it happen. There is no technology path leading to that level of automobile efficiency. What is different about chip technology?

The answer is that the basic performance measure of computing systems is computational steps per unit time (or energy). Twice as many components enable twice as many computational steps. And the regularity of components enables doubling them by scaling down size.

A chip is made of a very large number of simple basic components, mostly transistors and interconnecting wires. Doubling the number of components

in a chip generation is a feasible goal, as in Figure 2, and a method called "Dennard scaling" (described in the following paragraphs) was invented to accomplish it. Few other technologies (such as automobiles) feature complex systems composed of large numbers of identical parts.

Component doubling every chip generation may be feasible but is not easy. The underlying silicon technology, CMOS, cannot support the continued component reductions. What are the problems? And what options are available to overcome them? We cover three main ones:

Path to the square root reduction rule. Dennard scaling, which defined a path to the square root reduction rule for nearly 30 years, why it came to an end, and what has been done to increase computational speed since then;

Clock trees and clock distribution. Why do we have clocks? What is the problem with clocked circuits? Could it be solved with an additional clock distribution layer on the chip? Or by replacing clocked circuits with fast asynchronous (unclocked) circuits?; and

Taxonomy. A taxonomy of issues needed to keep Moore's Law at chip level going for more generations.

Dennard Scaling. In 1974, electrical engineer and inventor Robert Dennard and his team at IBM proposed a method to scale down transistors while maintaining a constant power density.⁶ The power density is energy dissipated in a square unit of chip area. It is proportional to the switching speed and

the number of transistors in a unit area. Greater power densities mean more heat to dissipate—and too much heat will burn up the chip. Dennard scaling says that power density stays constant as transistors get smaller so the power used is proportional to area.

Reducing the size of a subsystem and its components can allow for the clock interval to be shortened because the

logic gates switch faster and the wires connecting them are shorter. As noted, however, there is a limit to this approach because the increased number of state switches produces more heat. Engineers were able to increase clock speeds from approximately 5MHz in 1981 (IBM PC) to approximately 2GHz in 2000, leveling off at approximately 3.5GHz since 2002 (Intel Pentium 4). The cost of heat-sink technology to support greater clock speeds is prohibitive.

Even when clock speeds were held constant, chip engineers started to discover in the 1990s that leakage and quantum-tunneling effects became significant at small dimensions and produced more heat than Dennard scaling predicted. Dennard scaling was no longer a reliable pathway to reducing component size.

Multicore architectures were the response to the demise of Dennard scaling. The first two-core chips had twice as many components as the previous one-core chips. They were organized as two CPUs running in parallel at the same limiting clock speed (approximately 3.5GHz). Two cores could achieve twice the one-core speed if the computational workload had multiple computational threads. However, doubling on-chip cores every generation has its own heat-dissipation problems that will limit how many cores can be usefully placed on a chip.¹¹ Moreover, multicore architecture pushed some of the responsibility for speedup to multi-threaded programming and parallelizing compilers. Multicore parallelism is a fine strategy but draws programmers into parallel programming, something many were never trained to do.²

Metastability, clocks, and clock trees. Clocks became an integral feature of computer logic circuits in the 1940s because engineers could quickly and simply avoid a host of timing-dependent failures that result from metastable behavior in computer circuits. If the clock interval is too short, the flip-flops recording a subsystem's state can be triggered before their inputs have settled down, risking internal oscillations that freeze circuits or cause other malfunctions (see Figure 5).⁷

Metastability is also an issue when asynchronous subsystems (no common clock) can sense unsettled signals in an attempt to synchronize with each

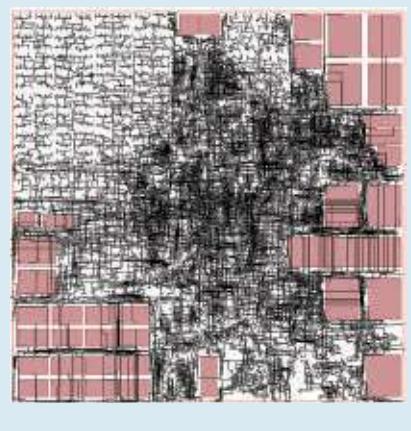
Few other technologies (such as automobiles) feature complex systems composed of large numbers of identical parts.

other. Designers use special protocols (such as ready-acknowledge signaling) to minimize the risk of synchronization failure in those cases.⁷

A major design problem is transmitting signals from a clock to all the components that need clock signals. The wires that do this take space on the chip, and there is a propagation delay along each wire. The term "clock skew" refers to the difference between the path with shortest delay and the path with longest delay. To avoid metastability, engineers must choose the clock time long enough to overcome skew.

The ideal circuit to distribute clock signals is a balanced tree with the clock at its root and the components at its leaves. In a balanced tree, all paths are the same length, and there is no skew. Many designers considered the H-tree fractal, a mathematical model of a geometric tree structure that replicates at ever-finer dimensions with each generation (see Figure 6). However, the H-fractal is space-filling, meaning that as the dimension of the tree gets larger the area occupied by the wires eventually fills the chip, leaving little room for active components. This forces chip designers to use more ad hoc methods that depend on unbalanced trees restricted to a portion of the area (see Figure 7). The unbalanced trees have a much larger number of leaf nodes than needed, so the designer can choose leaf nodes nearest the components needing signals and minimize clock skew. Some designers propose to put

Figure 7. Design of an actual chip has approximately half its area devoted to the clock tree (dense lines) and half to its actual components (colored boxes). Image courtesy of Sung Kyu Lim at The Georgia Institute of Technology.²⁷



Technology Jumping in Pursuit of Moore's Law

Wu et al.³³ conducted a study of possible directions for continuing the Moore's Law effect, citing seven major barriers to the continuation of the current Moore's Law with CMOS technology:

- Performance demand of the processor.* Exponential growth cannot be sustained inside a single technology;
- Power consumption and heat dissipation.* They grow worse per unit area as component size decreases;
- Communication costs of moving data through networks, interconnects, and caches.* They grow with the number of cores served;
- Tunneling effect.* Electrons jump narrow insulating barriers;
- Quantum limit to Moore's Law.* Compton wavelength is the fundamental limit to measuring the position of electrons; if component dimensions become that small, it will no longer be possible to tell where electrons are and whether they are being switched properly;
- Economic limit to Moore's Law.* Costs of R&D and manufacturing are rising exponentially, making it increasingly difficult for each next generation to be economically viable;
- On-board limits.* As designers move more functions onto a chip, the chip's performance depends on all the technologies, not just the logic circuits; for example, mixed-signal circuits (such as analog-digital converters and digital signal processors) are limited by sampling frequencies and sensitive to fabrication variations in transistors; and
- Mobile technologies.* Smartphones and multimedia phones present a phalanx of barriers to performance improvement, including increasing demand for bandwidth, concern for power reduction and battery life, limits on size and weight, and limits on what consumers are willing to pay.

Despite these barriers, Wu et al. saw eight ways new technology could address them:

- DNA scaffolding.* Employ DNA scaffolding technologies to build (grow) circuit boards.
- 3D fabrication.* Move to 3D fabrication;
- Carbon nanotubes and graphene.* Build components from carbon nanotubes and graphene;
- Single-atom transistor.* Develop a single-atom transistor;
- Quantum dots.* Design logic around quantum dots;
- Spintronics.* Employ spintronics to represent and process data;
- DNA computing.* Employ DNA computing to represent and process data; and
- Quantum computers.* Employ quantum computers to represent and process data.

Although the last three might produce benefits only in specialized cases (such as certain massively parallel search problems), some of them are so widespread that special processors may be economically viable.

An IEEE group called "Rebooting Computing" (<http://rebootingcomputing.ieee.org/>) is examining how to continue technology scaling in a post-Moore's Law era.²⁹ John Shalf of the National Energy Research Scientific Computing Center and Robert Leland of Sandia National Laboratory discussed a comprehensive study to form a taxonomy of possible CMOS-successor technologies,²⁹ identifying five possible categories in which successors might be found:

- Architectures and software advances.* Energy management, new kinds of circuits, system on a chip, neuronal chips,¹⁹ specialized chips, dark silicon, and near-threshold voltage operation;
- 3D integration and packaging.* Multiple tiered stacked chip, metal layers, and other types of active layers;
- Resistance reduction.* Superconductors and crystalline metals;
- Millivolt switches (better transistors).* Tunnel field-effect transistors, heterogeneous semiconductors, carbon nanotubes, graphene, and piezoelectric transistors; and
- New logic paradigms.* Spintronics, topological insulators, nanophotonics, biological computing, and chemical computing.

It is noteworthy that many of these directions involve technology jumping, a phenomenon observed in the Kurzweil charts,²⁵ as in Figure 3. The search for CMOS successors aims to jump to a new technology and continue the exponential growth from there.

Wu et al. are confident these lines of development will produce exponential growth advances for another 50 years. Shalf and Leland are more cautious but still show considerable optimism. Only time will tell, but you can be sure that some very good people are working each of these angles.

a balanced H-tree on a new layer of the chip,²⁷ but layering is controversial because putting other circuits (such as memory) on the new layer might benefit computing capacity more.

Due to these practical difficulties with clock-signal distribution, many designers have looked to asynchronous circuits. Two subsystems can exchange data by following a ready-acknowledge protocol. The sender signals that it has some data to send by setting a "ready" line to 1. On receipt of the signal, the receiver acknowledges by setting an "acknowledge" line to 1. When the sender sees the acknowledge, it deposits the data in a buffer and signals completion by returning "ready" to 0. Finally, the receiver takes the data from the buffer and sets "acknowledge" to 0. One unit of data can be transmitted at each cycle of this protocol.

Circuit designers have studied asynchronous signaling since the 1960s and developed reliable asynchronous circuits. Because these circuits are somewhat slower than clocked circuits, ready-acknowledge signaling is used only when there is no alternative (such as a CPU interacting with an I/O device).

Modern chips sometimes use asynchronous signaling (judiciously) to overcome clock distribution and skew problems. The chip is divided into modules, each with its own clock. Clocked circuits are used inside a module with asynchronous signaling between modules. For example, the module that displays a graphical image can be turned on just when a user wants to display the image and run at the clock speed necessary to render the image well; communication with the display module can be asynchronous.

Designing an all-asynchronous computer has been a holy grail among circuit designers for years. Intel is said to have demonstrated an asynchronous circuit for the fetch-execute control of a CPU but has not yet succeeded at creating an arithmetic-logic unit (ALU). The main research problem is finding a way for the ALU to report when it is done with an operation, given that the time of the operation can vary significantly depending on the inputs. Computer graphics pioneer Ivan Sutherland has long advocated for all-asynchronous circuits and demonstrated asynchronous pipeline chips.³⁰

Perhaps the most complete design of a computer that has no clocks is the data-flow architecture proposed by computer scientist Jack Dennis.⁹ It did not inspire sufficient commercial interest because its circuits ran slower than conventional clocked circuits; the machine got its throughput from massive data parallelism, which was not common at the time. Because the number of data-intensive applications continues to grow, the massively parallel dataflow architecture may yet find acceptance.

Potential technology directions.

Many engineers have been studying how to enable the continued growth of Moore's Law, given that the existing CMOS technology cannot be pushed much further; for more on the intensive research in this area, see the sidebar "Technology Jumping in Pursuit of Moore's Law."

Exponential Growth at the System Level

Users of computation are hungry for performance, measured as calculations per second or (more recently) calculations per watt-hour. But it does little good to embed faster chips in systems that are limited by other bottlenecks (such as communication bandwidth and cooling systems).

Bottlenecks are the main barrier to performance in systems. Engineers spend a lot of time identifying bottlenecks and speeding them up. Each generation of system improvement is more challenging because engineers must search multiple new technologies to resolve all bottlenecks.

Colwell⁵ discussed bottlenecks generated by "neighboring technologies," or technologies from other fields on which microchips depend. Wu et al.³³ gave a nice example with ubiquitous modern analog-digital converters (ADC). ADCs sample a continuous input signal at twice its highest frequency, producing a series of digital snapshots; according to the Nyquist sampling theorem, no information is lost at this sampling rate because the continuous signal can be regenerated from the samples. As logic circuits get faster, the ADC sampling rate is itself eventually a bottleneck. Engineers are searching for new sampling methods with higher rates.

The memory system is another potential bottleneck. Caches are a critical driver

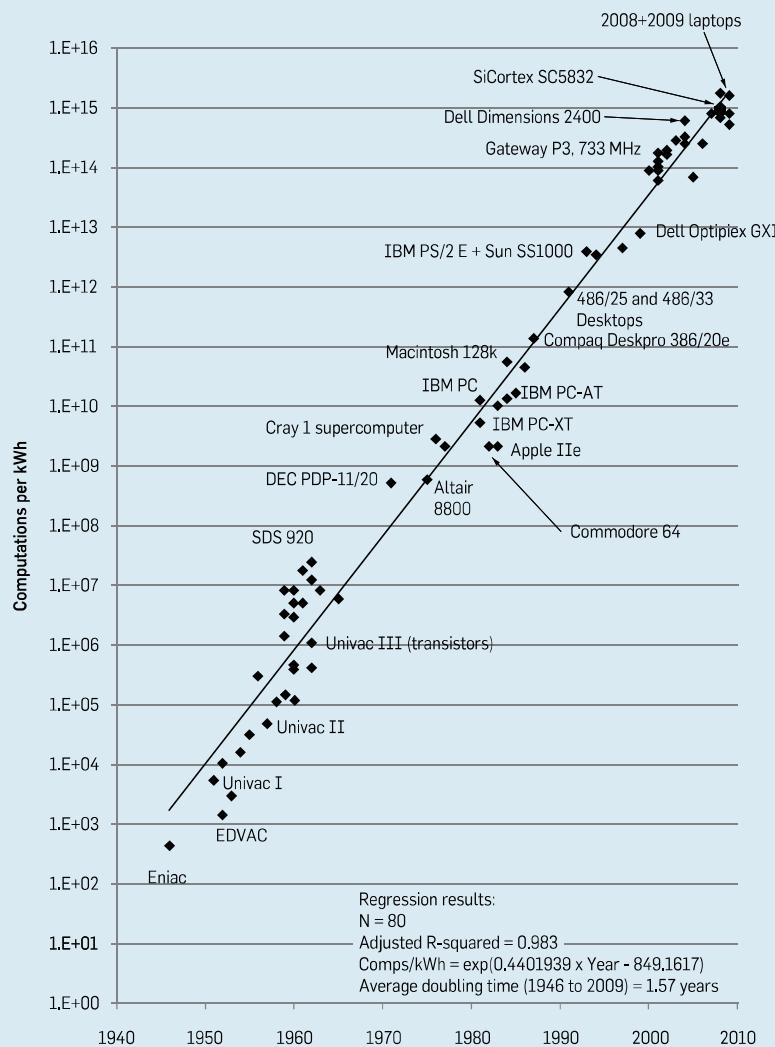
of performance; modern chips rely extensively on caches to position needed data near the processor, and poorly positioned data slows the cache and, in turn, the processor. Considerable research effort has gone into measuring locality of workloads and designing the caches for optimal performance with those workloads. Cache designers are under constant pressure to produce memory improvements matching CPU improvements.

Despite these challenges, computer engineers have been very successful over the years at producing complete systems with performance that has grown exponentially. Koomey^{22,23} gathered data for a large number of different

computers from 1946 to 2009 and found exponential growth in two measures: computation speeds per computer and computations per kilowatt-hour (kwh); see Figure 8 for his graph of computations per kwh. The doubling times were about the same—1.57 years—in both graphs. The improvements relative to energy consumption, summarized as Koomey's Law,¹⁰ have assumed great importance in an energy-constrained world, from large data centers with fixed power draw to mobile devices with fixed battery life. This trend could continue for at least another several decades.

Even when systems are designed so no bottlenecks stand in the way of

Figure 8. Koomey's Law graph illustrates the continuing success of designing systems that produce more computation for the same power consumption. Careful power management over the past decade has enabled the explosion of mobile devices that depend critically on technologies that minimize power use.



Source: Koomey's blog, creative commons license.

performance, it is possible that the workloads presented to those systems are not sufficient to use all the available computing power. In 1967, Gene Amdahl, a mainframe computer designer at IBM, investigated whether it would be better to get faster speed through a faster CPU or through several slower parallel CPUs. Based on his experience designing instruction-lookahead CPUs, he realized that substantial parts of code must be executed sequentially in the given compiled sequence; only some of the instructions could be speeded up by parallel execution. He derived a formula that became known as Amdahl's Law to express the speedup potential from a set of n processors (cores) working on a program. Amdahl's idea—expressing the parallelizable part as a set of parallel instruction streams—was known in his time as “control parallelism.” Suppose the time of the job using 1 stream is $T(1) = a+b$, where a is the time for the serial part, and b is the time for the parallelizable part. The serial fraction is $p = a/(a+b)$, and parallelizable fraction is $1-p$. The time to execute on n streams is $T(n) = a + b/n$ because only the control-parallel portion of the algorithm can benefit from n processors. Amdahl's Law says the speedup is

$$(1) \quad S_A(n) = \frac{T(1)}{T(n)} = \frac{a+b}{a+b/n} = \frac{n}{np+(1-p)} < \frac{1}{p}$$

For example, an application 10% serial would run at most 10 times faster than its single-stream time, even with a large number of parallel processing cores. That is, even if a small part of the overall computation is serial, it is impossible to achieve much multicore speedup with control parallelism.¹⁸

Amdahl's Law would seem to limit the speedup to considerably less than the number of cores, because it assumes parallelism comes from remodelling a serial algorithm into a parallel algorithm. However, Amdahl's Law overlooks parallelism inherent in data. Data-parallel workloads are now common in data-intensive applications (such as MapReduce operations on the Web). In a data-intensive problem, the data space can be partitioned into many small subsets, each of which can be processed by its own thread. The finer the grain of the partition, the larger the number of threads. The same algorithm runs in each thread on the data subset

belonging to that thread. Computer scientist John Gustafson observed that large data-intensive problems could always be partitioned into as many grains as could be supported by cores in the processors when there is sufficient data parallelism.¹⁶ In this case, the computational work completed on one core is $W(1) = a+b$, as outlined earlier. With n cores, it jumps to $W(n) = a+bn$ because each of the n cores is performing the same operation on its thread's (different) data items. Gustafson's Law says the speedup is linear in n

$$(2) \quad S_G(n) = \frac{W(n)}{W(1)} = \frac{a+bn}{a+b} = p+n(1-p) > n(1-p)$$

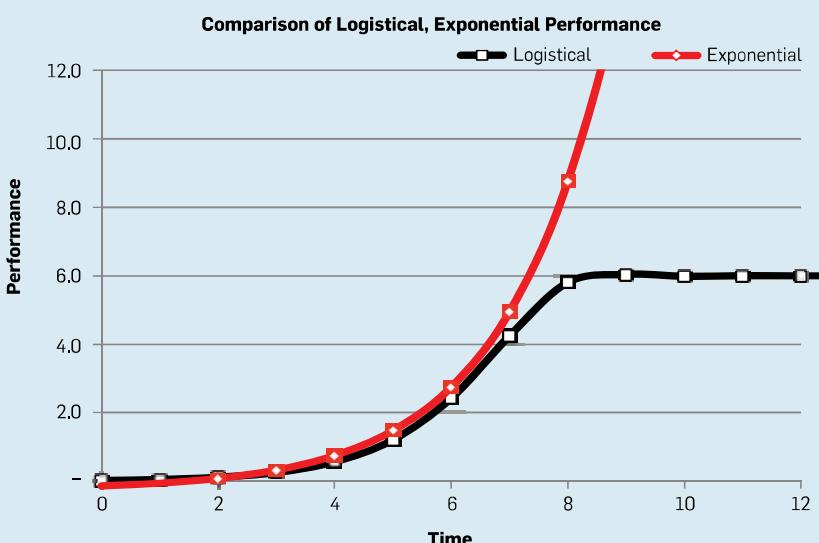
That is, for data-intensive applications with small serial fraction p , adding cores increases the computational work in direct proportion to the number of cores.

Rather than parallelizing the algorithm, data-parallel programming parallelizes the data. Gustafson's Law models data-parallel computing, where the speedup scales with the size of the data, not the number of control-parallel paths specified in the algorithm.

Parallelizing data instead of algorithms was a paradigm shift that began in the 1980s.⁸ Today, it exploits multicore systems even when algorithms cannot be parallelized. It extends to heterogeneous data parallelism for common applications on the Internet (such as querying databases, serving email, and executing graphics-intensive applications, as in games). Peer-to-peer computing is a form of loosely coupled data parallelism, and cloud computing with multicore servers is a form of tightly coupled data parallelism.

Data parallelism and its variants is why multicore systems can continue to double output without increasing clock frequency. At the system level, as long as the applications contain many parallel tasks, there is always work available for the new cores in next-generation systems. This paradigm is especially useful for processing big data now being routinely provided by users of products from companies like Google, Facebook, Twitter, and LinkedIn.

Figure 9. The logistics function—the mathematical model for growth of a population (such as adopters of a technology)—plots as an S-curve (black) over time. Initially, the curve follows an exponential (red) curve, but after an inflection point (here at time 6) it flattens out because of market saturation.



Technology Diffusion at the Community Level

Moore spoke of a second law, also known as Rock's Law, which is less well known than Moore's own component-doubling law. The second law says that the cost of the fabrication facility for new chips doubles approximately every four years. This is due to the greater precision and ever-smaller size of lithography. An important implication is that the market for a new generation of chips at the same price must be at least double the market for the current generation, just to pay for the new fabrication facility. That is, Moore and Rock recognized that the markets had to expand exponentially to support the continuation of the basic Moore's Law. Without exponential expansion of adoption at the community level, Moore's Law at the chip level would be unsustainable.

Many business strategists believe in the S-curve model whereby the number of people using a technology initially grows exponentially to an inflection point and then flattens out (see Figure 9). The flattening out is caused by the saturation of the market—no more new adopters. Businesses try to time their entry into new technologies whose new S-curves are in their exponential growth stage when the older technology starts to flatten, or "tech-

nology jumping." Businesses ride a series of S-waves and experience continuous exponential growth as they hop from one wave to the next.

Technology jumping is an integral, recurrent theme in computing. We noted earlier that Kurzweil explained exponential growth in the power of information technology by five massive switches to new technology that made older ones obsolete.²⁵ He assumed that the process of technology jumping will continue well into the 21st century. Steve Jobs of Apple spoke frequently about his strategy of timing his jump to the next technology with the inflection point of the S-curve for the current technology. Andy Grove of Intel took the emergence of a new technology that did a job 10 times better than the current technology as a sign of an inflection point and built his company's strategy around well-timed jumps.¹⁵

Whether or not a new technology is adopted depends on whether people use it instead of something else to accomplish something they care about.¹³ Innovators play an important role in this process by making products and services that influence community members to commit to adopt the new technology into their practice.

A simple argument shows why initial growth of adoption is exponential. Sup-

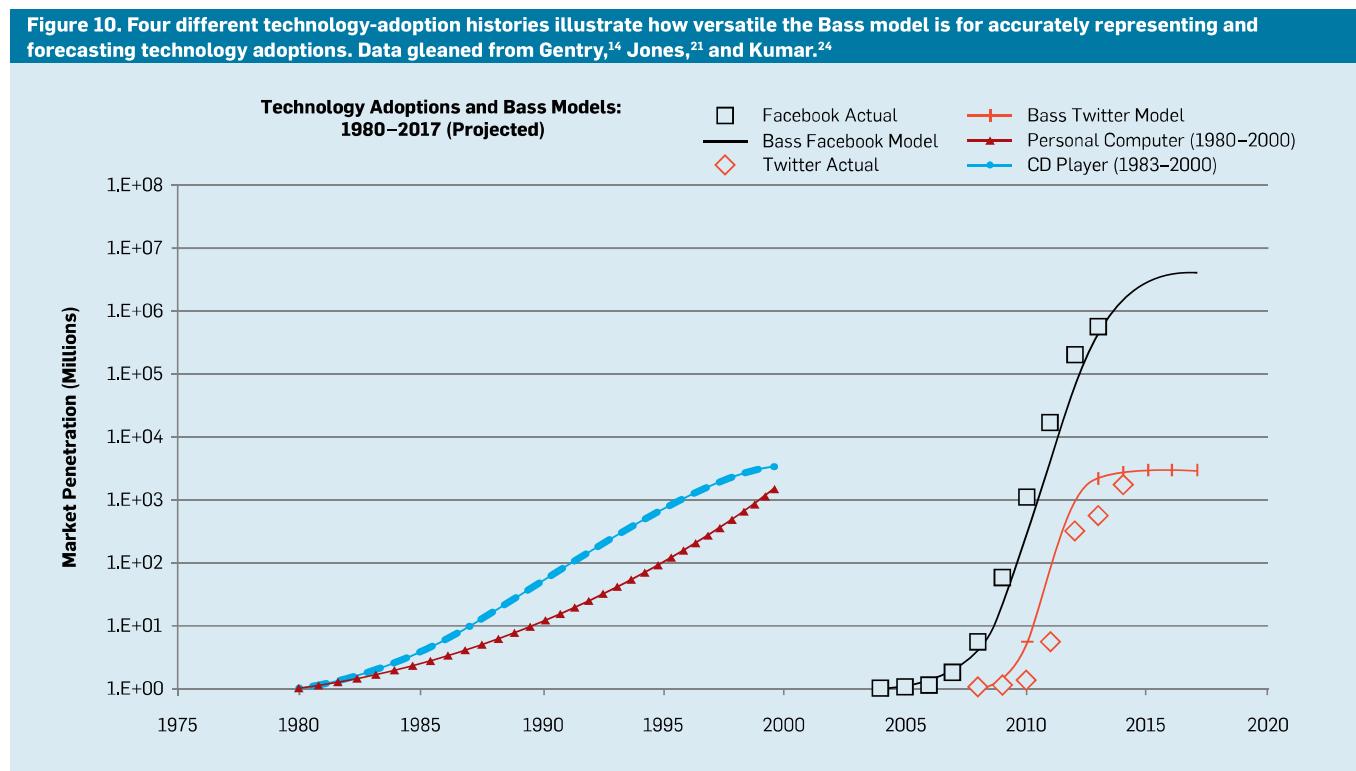
pose $n(t)$ is the number of members of a population who have adopted a technology as of time t . Each adopter demonstrates the value of the new technology to the rest of the population. Let a be the rate at which one adopter influences a non-adopter to adopt. In a small time interval h , the probability that a new adopter comes on board is ah . At time $t+h$, there are thus $ahn(t)$ new adopters, giving $n(t+h)-n(t) = ahn(t)$. Rearranging this equation and letting h go to 0 yields the differential equation

$$(3) \quad \frac{d}{dt} n(t) = an(t)$$

The solution to this equation is $n(t) = e^{at}$. The size of the adopting population increases exponentially and the mean time between adoptions is $1/a$. We can conclude from this simple equation that exponential growth happens when the rate of change also increases with current state.

This model is also too simple because it does not account for diminishing returns due to market saturation or technology reaching a limit where growth stops, when, for example, everyone in the population has adopted the technology. We can extend the model to account for the diminishing population of non-adopters. As before, let $n(t)$ denote the number of members

Figure 10. Four different technology-adoption histories illustrate how versatile the Bass model is for accurately representing and forecasting technology adoptions. Data gleaned from Gentry,¹⁴ Jones,²¹ and Kumar.²⁴



in a population of size N who have adopted a technology. The change in the number of adopters from time t to time $t+h$ would then be proportional to two quantities: the number who have already adopted, as in equation 3, and the fraction who have not yet adopted. This gives the differential equation

$$(4) \quad \frac{d}{dt}n(t) = an(t)\left(\frac{N-n(t)}{N}\right)$$

which is called the “logistics equation” in the literature; its solution is

$$(5) \quad n(t) = \frac{N}{1+(N-1)e^{-at}}$$

This function grows exponentially to its inflection point. Initially, when $t=0$, there is only one adopter, $n(0) = 1$, and after a long period of time there are N adopters.

Reality is more complicated because individuals have their own adoption time constants. Sociologist Everett Rogers discovered in 1962 that individuals fall into five groups according to the time they take to commit to an adoption—innovator, early adopter, early majority, late majority, and laggard.²⁸ The histogram of adoption times follows a Bell curve. The five categories correspond to five zones of standard deviations. For example, innovators are 2.5% of the population, with adoption times at least two standard deviations below the mean; early adopters are 13.5% and are one to two standard deviations below the mean; early majority are 34% and zero to one standard deviations below the mean. In 1969, professor of marketing Frank Bass modified the Rogers diffusion model by quantifying the impact of early-adopter and word-of-mouth (all other) followers, inserting parameters p (early adoption rate), q (word-of-mouth follower rate), and N into the simple logistics curve.^{3,4} Ashish Kumar and others have since validated Bass's extensions for real products by finding parameters p , q , and N for a number of technology products.^{14,24} Setting $a=p+q$ and $r=q/p$, the Bass model then gives

$$(6) \quad n(t) = \frac{N(1-e^{-at})}{1+re^{-at}}$$

Bass's equation is still a logistics model that more accurately forecasts sales and also reaches an inflection point where the exponential growth

Data parallelism and its variants is why multicore systems can continue to double output without increasing clock frequency.

begins to slow as diminishing returns set in. Figure 10 depicts four different technology adoptions since 1980. Bass's model can be solved to find the inflection-point value of at , helping fit the model to data.

No matter what, the initial growth up to the inflection point is exponential. Historically, information technologists have jumped from one technology to another when an incumbent technology nears its inflection point. After each jump, they are on a new curve growing exponentially toward a new inflection point. Moore's Law, and others like it, are intrinsically exponential because their rate of change is proportional to their current state.

Conclusion

The original 1965 Moore's Law was an empirical observation that component density on a computer chip doubled every two years. Similar doubling rates have been observed in chip speeds, computer speeds, and computations per unit of energy. However, the durability of these technology forecasts suggests deeper phenomena.

We have argued that exponential growth would not have succeeded without sustained exponential growth at three levels of the computing ecosystem—chip, system, and adopting community. Growth (progress) feeds on itself up to the inflection point. Diminishing returns then set in, signaling the need to jump to another technology, system design, or class of application or community.

At the chip level, there are strong economic motivations for chip companies and their engineers to feed on previous improvements, building faster chips that grow exponentially up to the inflection point. The first significant technology path for exponential chip growth appeared in the form of Dennard scaling, which showed how to reduce component dimension without increasing power density. Dennard scaling reached an inflection point in the 1990s due to heat-dissipation problems that limited clock speed to approximately 3.5Ghz. Engineers responded with a technology jump to multicore chips, which gave speedup through parallelism. This jump has been enormously effective. Cloud platforms and supercomput-

ers achieve high computation rates through massive parallelism among many chips.

A major technology barrier to chip growth has been the distribution of clock signals to all components on a chip. The theoretically most efficient distribution mechanism is the space-filling fractal H-tree that reaches diminishing returns when the tree itself starts to consume most of the physical space on the chip. Engineers are experimenting with hybrids that feature subsystems (such as cores) with their own clocks interacting via asynchronous signaling. Some engineers have been exploring the design of all-asynchronous circuits (no clocks), but these systems cannot yet compete in speed with clocked systems.

Engineers have been systematically examining the barriers that prevent the continuation of Moore's Law for CMOS technologies. As alternatives mature, it will be feasible to jump to the new technologies and continue the exponential growth. Although there is controversy about how successful some of the alternatives may be, there is considerable optimism that some will work out and exponential growth can continue with new base technologies.

When chips and other components are assembled into complete computer systems, engineers have located and relieved technology bottlenecks that would prevent the systems from scaling up in speed as fast as their component chips scale. Koomey's Laws document exponential growth of computations per computer and per unit of energy from 1946 to 2009. Koomey's Law for computations per unit of energy is especially important throughout an energy-constrained industry. Additionally, the technology jump from algorithm parallelism to data parallelism further assures us we can grow systems performance as long as the workloads have sufficient parallelism, which has turned out to be the case for cloud and supercomputing systems.

Finally, we demonstrated that simple assumptions about adoption process lead to the S-curve model in which adoptions grow exponentially until an inflection point and then slow down because of market saturation. Business leaders use the S-curve model to guide them in jumping to new technologies when the older ones start to encounter their limits. Exponential growth in

sales through ever-expanding applications and communities provides the financial stimulus to advance the chip-and system-level technologies (Rock's Law). It is a complete cycle.

These analyses show that the conditions exist at all three levels of the computing ecosystem to sustain exponential growth. They support the optimism of many engineers that many additional years of exponential growth are likely. Moore's Law was sustained for five decades. Exponential growth is likely to be sustained for many more.

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References

- Anderson, R.G. *How Well Do Wages Follow Productivity Growth?* Federal Reserve Bank of St. Louis Economic Synopses, St. Louis, MO, 2007; <https://research.stlouisfed.org/publications/es/07/ES0707.pdf>
- Asanovic, K., Bodik, R., Demmel, J., Keaveny, T., Keutzer, K., Kubiatowicz, J., Morgan, N., Patterson, D., Sen, K., Wawrzynek, J., Wessel, D., and Yelick, K. A view of the parallel computing landscape. *Commun. ACM* 52, 10 (Oct. 2009), 56–67.
- Bass, F. A new product growth model for consumer durables. *Management Science* 15, 5 (Jan. 1969), 215–227.
- Bass, F., Krishnan, T., and Jain, D. Why the Bass model fits without decision variables. *Marketing Science* 13, 3 (Summer 1994), 203–223.
- Colwell, R. The chip design game at the end of Moore's Law. In *Proceedings of the IEEE/ACM Symposium on High-Performance Chips (Hot Chips)* (Palo Alto, CA, Aug. 25–27). ACM Press, New York, 2013; http://www.hotchips.org/wp-content/uploads/hc_archives/hc25/HC25.15-keynote1-Chipdesign-epub/HC25.26.190-Keynote1-ChipDesignGame-Colwell-DARPA.pdf
- Dennard, R., Gaenslen, F., Yu, H.-N., Rideout, V.L., Bassous, E., and LeBlanc, A. Design of ion-implanted mosfets with very small physical dimensions. *IEEE Journal of Solid State Circuits* (1974), 256–268.
- Denning, P. The choice uncertainty principle. *Commun. ACM* 50, 11 (Nov. 2007), 9–14.
- Denning, P. and Tichy, W. Highly parallel computation. *Science* 250 (Nov. 1990), 1217–1222.
- Dennis, J. and Misunas, D. A preliminary architecture for a basic data-flow processor. In *Proceedings of the Second Annual Symposium on Computer Architecture (ISCA)* (Houston, TX, Jan. 20–22). ACM Press, New York, 1975, 126–132.
- Economist. A deeper law than Moore's? *Economist* blog (Oct. 10, 2011); <http://www.economist.com/blogs/dailychart/2011/10/computing-power>
- Esmaelzadeh, H., Blen, E., St. Amant, R., Sankaralingam, K., and Burger, D. Dark silicon and the end of multicore scaling. In *Proceedings of the 38th International Symposium on Computer Architecture (ISCA)* (San Jose, CA, June 4–8). ACM Press, New York, 2011, 365–376.
- Feynman, R. *The Pleasure of Finding Things Out: The Best Short Works of Richard P. Feynman*. Penguin Books, New York, 2001.
- Flores, F. and Denning, P. Emergent innovation. Interview by Peter J. Denning. *Commun. ACM* 58, 6 (June 2015), 28–31.
- Gentry, L. and Calantone, R. *Forecasting Consumer Adoption of Technological Innovation: Choosing the Appropriate Diffusion Models for New Products and Services Before Launch*. Faculty Research & Creative Works, Paper 662. Missouri University of Science and Technology, Rolla, MO, 2007; http://scholarsmine.mst.edu/faculty_work/662
- Grove, A. *Only the Paranoid Survive*. Doubleday, New York, 1996.
- Gustafson, J. Re-evaluating Amdahl's Law. *Commun. ACM* 31, 5 (May 1988), 522–533.
- Henderson, B. The Experience Curve—Reviewed (Part II). *BCG Perspectives* (Jan. 1973); https://www.bcgperspectives.com/content/classics/corporate_finance_corporate_strategy_portfolio_management_the_experience_curve_reviewed_history/
- Hill, M. Amdahl's Law in the multicore era. *IEEE Computer* 41, 7 (July 2008), 33–38.
- IBM. Announcement of SyNAPSE Chip: New IBM SyNAPSE Chip Could Open Era of Vast Neural Networks. IBM, San Jose, CA, Aug. 7, 2014; <http://www-03.ibm.com/press/us/en/pressrelease/44529.wss>
- IEEE Spectrum. Special Report on 50 Years of Moore's Law. *IEEE Spectrum* (Apr. 2015); <http://spectrum.ieee.org/static/special-report-50-years-of-moores-law>
- Jones, K. Growth of Social Media v2.0. *Search Engine Journal Blog*, Nov. 15, 2013; <https://www.searchengineweekly.com/growth-social-media-2-0-infographic/77055/>
- Koomey, J., Berard, S., Sanchez, M., and Wong, H. Implications of historical trends in the electrical efficiency of computing. *IEEE Annals of the History of Computing* 33, 3 (July–Sept. 2011) 46–54.
- Koomey, J. More on efficiency trends in computing, from my forthcoming book, blog, including Koomey Law graph and pointer to creative commons attribution-noncommercial-noderivative license. Dec. 11, 2011; <http://www.koomey.com/post/14466436072>
- Kumar, A., Baisya, R.J., Shankar, R., and Momaya, K. Diffusion of mobile communications: Application of Bass Diffusion Model to BRIC countries. *Journal of Scientific & Industrial Research* 66 (Apr. 2007), 312–316.
- Kurzweil, R. *The Age of Spiritual Machines*. Penguin Books, New York, 1999.
- Moore, G. Cramping more components onto integrated circuits. *Electronics* 38, 8 (Apr. 1965), 114–117.
- Panth, S., Samadi, K., Du, Y., and Lim, S.K. Design and CAD methodologies for low-power gate-level monolithic 3D ICs. In *Proceedings of the ACM/IEEE International Symposium on Low Power Electronics and Design* (La Jolla, CA, Aug. 11–13). ACM Press, New York, 2014, 171–176; <http://dx.doi.org/10.1145/2627369.2627642>
- Rogers, E. *Diffusion of Innovations*, Fifth Edition. Free Press, New York, 2003.
- Shalf, J. and Leland, R. Computing beyond Moore's Law. *IEEE Computer* 48, 12 (Dec. 2015), 14–23.
- Sutherland, I. The tyranny of the clock. *Commun. ACM* 55, 10 (Oct. 2012), 35–36.
- Thackary, A., Brock, D., and Jones, R. *Moore's Law: The Life of Gordon Moore, Silicon Valley's Quiet Revolutionary*. Basic Books, New York, 2015.
- Ubiquity. Ubiquity Symposium on the Technological Singularity, 2014; <http://ubiquity.acm.org/symposia.cfm>
- Wu, J., Shen, Y.-L., Reinhardt, K., Szu, H., and Dong, B. A nanotechnology enhancement to Moore's Law. *Applied Computational Intelligence and Soft Computing* 2013, Article ID 426962; <http://dx.doi.org/10.1155/2013/426962>

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contributed articles

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Central IT needs to guide functional areas and departments toward effective operational and procurement practices.

BY CECIL ENG HUANG CHUA AND VEDA C. STOREY

Bottom-Up Enterprise Information Systems: Rethinking the Roles of Central IT Departments

CROSS-FUNCTIONAL, ENTERPRISE, AND infrastructure systems integrate information across an organization for use by multiple stakeholders.^{14,22} Development or configuration of these large, multimillion-dollar projects is normally overseen by top management in conjunction with the central information technology (IT) department.²¹ There is, however, an increasing number of such systems arising from functional areas or departments in which users work, with central

IT and top management being challenged to implement controls on these systems only after they go live.¹³

Consider the following examples based on interviews conducted in recent years. Half were with chief information officers (CIOs). The other half were with their end users. Our aim was to understand the factors leading to bottom-up enterprise information systems. The first example is from a mid-size hospital in Auckland, New Zealand, where doctors had contracted with a paging service. In the second, university faculty adopted the Moodle learning-management system instead of their locally supported system.

CIO: "This guy ... who built this thing and hosted it out of a literally a garage somewhere in London, and they said, 'Well, we'd like to trial this.' And he said 'fine.' So they set up a trial using that hosted environment ... they actually implemented it into something like 12 or 16 wards. It was just so successful that after the first month it grew like wildfire."

Another CIO: "Blackboard was the official system ... People said, 'We want to bring the Moodle environment test mode, and it will only be in test mode, and we will see how that goes... so they started using lectures on them, so it became a production environment. But it was under their control sitting somewhere on some server, and they've got an organization functionally dependent on shadow IT."

Bottom-up enterprise information systems are not sanctioned by central IT, the official group within an

» key insights

- Central IT must deal with the emerging reality of bottom-up enterprise information systems.
- Bottom-up enterprise information systems are developed by employees when alternatives are not readily available.
- Central IT and functional areas must work together to understand and maintain effective bottom-up enterprise information systems that support overall organizational strategy.



organization responsible for IT. Nevertheless, they are implemented on an organizationwide or, minimally, a cross-functional basis. They exhibit three key characteristics. First, they are either enterprise-wide, or function spanning, so the technology is used across multiple departments. Second, IT implementations are developed, configured, or procured by end users who do not necessarily have sophisticated technology skills. Third, imple-

mentation decisions are made when top management and central IT exert little formal control and have no official governance over the project.

In this article, we investigate the emergent phenomenon of such bottom-up enterprise information systems to identify causal factors and offer recommendations for how to best manage it. Insights are derived from three sources. First and foremost, the paired CIO and end-user interviews

provide concrete examples of how bottom-up enterprise information systems are emerging and being managed from which some general inferences can be made. Second, our interview data is complemented by the practitioner literature from which we derive a framework for understanding the context of bottom-up enterprise information systems. Finally, the theoretical literature, specifically on distributed leadership, provides insights into how

the phenomenon should be managed. The result is a set of recommendations for rethinking the role of central IT to effectively manage bottom-up enterprise information systems.

Drivers of Bottom-Up Systems

The two types of main drivers of bottom-up enterprise information systems are external and internal:

External. The primary reason bottom-up enterprise information systems are emerging today is changes in technology, especially since the mid-2000s, including:

Simpler/“standardized” application distribution models. Historically, enterprise information systems have been configured and installed by specialized vendors. Such applications are now available in downloadable form. For example, ADempiere (<http://adempire.org>) is an open source enterprise resource planning system; Moodle is an open source learning-management system. Cloud versions of enterprise software are available; for example, SAP Business ByDesign (<http://go.sap.com/product/enterprise-management/business-bydesign.html>) is a cloud-based version of SAP.

Changing IT application cost structure. Historically, new IT applications were expensive capital costs, requiring central IT to secure large budgets in advance.⁶ In contrast, many modern software packages are paid for as ongoing, operational costs; for example, SAP Business ByDesign is accessed through a monthly subscription. Costs are amortized over a longer period,

so functional areas reallocate money from routine budgets to acquire new applications, thereby bypassing financial checks when procuring software.

CIO: “They can reprioritize the definition of what’s an operational expenditure versus a capital expenditure, and, if they have some ‘underspend,’ they can get a developer in and pay just an hourly rate and get some developer time.”

Accessible third-party technical support. One factor impeding the ability of functional areas to procure IT products and support independently has been their lack of IT expertise.¹² However, contemporary applications (such as Microsoft’s Active Directory and TeamViewer) allow monitoring and control of remote computational devices. Functional areas can outsource some IT to a vendor, thereby bypassing both central IT and top management.

User: “... at the moment it’s hosted externally ... it’s an Internet-based system, which means that our staff can access it anywhere, it means ... we can make changes quickly ... Stuff that doesn’t happen through our centralized IT group. Well, it happens, but over a very long period of time.”

Standardization of interfaces. Many enterprise solutions are Web-based, so they work well on most devices. It is thus possible for users to bypass the physical organizational IT infrastructure. Even when organizations block bottom-up enterprise information systems on internal networks, users can still employ personal devices for access.

Changes caused by a bottom-up approach to central IT business processes.

ITIL Process Group	Changes
Service Strategy	Central IT must dedicate more resources to all levels of service strategy: lowest levels focus on functional areas; mid-levels focus on planning and projection; and highest levels focus on negotiation and strategic coordination.
Service Design	Central IT becomes a repository of organizational knowledge and requirements, helping align functional areas’ IT projects with the overall enterprise vision and architecture.
Service Transition	Central IT reminds functional areas to incorporate service transitions into their plans.
Service Operations	Central IT maintains enterprise infrastructure, coordinates across functional areas to ensure operational continuity and quality, and consults with functional areas to facilitate service operations.
Continual Service Improvement	Central IT reminds functional areas to perform CSI, coordinates cross-functional CSI, and advises functional areas on CSI best practices.

Together, these external drivers provide users access to complex, multi-function systems that were previously inaccessible.

Internal drivers. There are two main internal organizational drivers:

Inherent limitations of centrally managed governance. Centrally managed governance systems usually favor large, highly visible projects with quantifiable bottom-line benefits. Smaller, possibly exploratory, projects may be neglected. Such projects may have intangible, difficult-to-quantify benefits. The following quote from a CIO illustrates a bias inherent in many centrally managed IT procurement processes.

CIO: “[Person] said we need more e-learning. I said, absolutely, but fat chance that it’s going to make the priority list based on what we are doing. And he said, look I found this online company; it’s an open source product. All I need is \$20,000 to get started.”

This e-learning case highlights little “objective” basis for top management to support such an endeavor. Convincing top management to take notice may indeed be impossible. However, when projects are successful, they can spread quickly, as in the hospital paging service.

Organizational processes. Some organizational processes are ineffective or dysfunctional, making them difficult or costly to work around;²⁴ alternatively, processes may change frequently in today’s dynamic business environment. Functional departments may thus implement bottom-up enterprise information systems because they do not perceive feasible alternatives as being available.

In one Moodle implementation, a particular university’s rules prevented users from enrolling students who attended “short” courses (such as adult education and executive MBA). These students did not go through the complete university student-enrollment process and were not issued university student-identification cards and numbers, a prerequisite for using the existing learning-management system. Users employed Moodle to enroll and manage these students. Here, the central IT system did not cater to a significant (and highly profitable) sub-segment of the university’s customer