

BRAC UNIVERSITY
Department of Computer Science and Engineering
CSE 260: Digital Logic Design

Examination: **Quiz 1**
Duration: 25 Minutes

Semester: Spring 2025
Full Marks: 15

Answer the following questions. You **MUST** show your workings/calculations where applicable.
Figures in the right margin indicate marks.

Name: <i>Solution</i>	Section: <i>02</i>	ID:
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1. Perform the following conversion: $(\underline{101011110001100})_{\text{Excess-5}} = (?)_7$
Note: You **must** show all the necessary conversions. [4]
2. Subtract $(-36)_{10}$ from 50_{10} using **7-bit 2's complement** system (show the conversion first).
Justify whether there is an **overflow or not**. [5]
3. Divide $(32112)_4$ by $(33)_4$. Find the quotient and remainder.
Note: You **must** show the necessary calculations. [6]

<p><i>1)</i> $(\underline{101011110001100})_{\text{Ex-5}}$</p> <table style="margin-left: auto; margin-right: auto; text-align: center;"> <tr> <td>$\overbrace{0101}$</td> <td>$\overbrace{0111}$</td> <td>$\overbrace{1000}$</td> <td>$\overbrace{1100}$</td> </tr> <tr> <td>5</td> <td>7</td> <td>8</td> <td>12</td> </tr> <tr> <td>-5</td> <td>-5</td> <td>-5</td> <td>-5</td> </tr> <tr> <td style="border-top: 1px solid black;">0</td> <td style="border-top: 1px solid black;">2</td> <td style="border-top: 1px solid black;">3</td> <td style="border-top: 1px solid black;">7</td> </tr> </table> <p>$= (0237)_{10}$</p> <p>$= (237)_{10} = (?)$</p>	$\overbrace{0101}$	$\overbrace{0111}$	$\overbrace{1000}$	$\overbrace{1100}$	5	7	8	12	-5	-5	-5	-5	0	2	3	7	<table style="margin-left: auto; margin-right: auto; text-align: center;"> <tr><td>$\cancel{7} \overline{) 23 \cancel{7}}$</td></tr> <tr><td>$\cancel{7} \overline{) 33 - 6 - 1}$</td></tr> <tr><td>$\cancel{7} \overline{) 4 - 5}$</td></tr> <tr><td>$0 - 4 - 11$</td></tr> </table> <p>$(237)_{10} = (456)_7$</p>	$\cancel{7} \overline{) 23 \cancel{7}}$	$\cancel{7} \overline{) 33 - 6 - 1}$	$\cancel{7} \overline{) 4 - 5}$	$0 - 4 - 11$
$\overbrace{0101}$	$\overbrace{0111}$	$\overbrace{1000}$	$\overbrace{1100}$																		
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$\cancel{7} \overline{) 4 - 5}$																					
$0 - 4 - 11$																					
$\Rightarrow (101011110001100)_{\text{Ex-5}} = (456)_7 \text{ (Ans)}$																					

<p><i>2)</i> $50 - (-36) = 50 + 36$</p> <table style="margin-left: auto; margin-right: auto; text-align: center;"> <tr><td>$2 \overline{) 50}$</td></tr> <tr><td>$2 \overline{) 25 - 0}$</td></tr> <tr><td>$2 \overline{) 12 - 1}$</td></tr> <tr><td>$2 \overline{) 6 - 0}$</td></tr> <tr><td>$2 \overline{) 3 - 0}$</td></tr> <tr><td>$2 \overline{) 1 - 1}$</td></tr> <tr><td>$0 - 1$</td></tr> </table> <p>$\Rightarrow (50)_{10} = (110010)_2$</p> <p>$+ 50 = 0110010$</p>	$2 \overline{) 50}$	$2 \overline{) 25 - 0}$	$2 \overline{) 12 - 1}$	$2 \overline{) 6 - 0}$	$2 \overline{) 3 - 0}$	$2 \overline{) 1 - 1}$	$0 - 1$	<table style="margin-left: auto; margin-right: auto; text-align: center;"> <tr><td>$2 \overline{) 36}$</td></tr> <tr><td>$2 \overline{) 18 - 0 \rightarrow 2}$</td></tr> <tr><td>$2 \overline{) 9 - 0}$</td></tr> <tr><td>$2 \overline{) 4 - 1}$</td></tr> <tr><td>$2 \overline{) 2 - 0}$</td></tr> <tr><td>$2 \overline{) 1 - 0}$</td></tr> <tr><td>$0 - 1 \rightarrow 11$</td></tr> </table> <p>$(36)_{10} = (100100)_2$</p> <p>$+ 36 = 0100100$</p>	$2 \overline{) 36}$	$2 \overline{) 18 - 0 \rightarrow 2}$	$2 \overline{) 9 - 0}$	$2 \overline{) 4 - 1}$	$2 \overline{) 2 - 0}$	$2 \overline{) 1 - 0}$	$0 - 1 \rightarrow 11$	<p style="text-align: center;">$\rightarrow +$</p> <table style="margin-left: auto; margin-right: auto; text-align: center;"> <tr><td>0110010</td></tr> <tr><td>$+ 0100100$</td></tr> <tr><td style="border-top: 1px solid black;">1010110</td></tr> </table> <p style="color: red; font-style: italic;">Here, we added two positive numbers but the answer has negative sign.</p> <p>So, according to this rule, Adding two same signed numbers if answer has different sign, then overflow.</p>	0110010	$+ 0100100$	1010110
$2 \overline{) 50}$																			
$2 \overline{) 25 - 0}$																			
$2 \overline{) 12 - 1}$																			
$2 \overline{) 6 - 0}$																			
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$2 \overline{) 1 - 0}$																			
$0 - 1 \rightarrow 11$																			
0110010																			
$+ 0100100$																			
1010110																			

Yes, we have overflow here.

3)

$$\begin{array}{r}
 \begin{array}{c} \downarrow \downarrow \downarrow \downarrow \\ 33 \end{array} \overline{) 32112} \mid 00331 \\
 \underline{0} \\
 32 \\
 - 0 \\
 \hline
 321 \\
 - 331 \\
 \hline
 301 \\
 - 331 \\
 \hline
 1026 \\
 - 33 \\
 \hline
 03
 \end{array}$$

$$33 \times 0 = 0$$

$$33 \times 1 = 33$$

$$33 \times 2 = 132$$

$$33 \times 3 = 231$$

$$\begin{array}{r}
 1 \\
 33 \quad 4 \mid 6 \mid 1 \\
 \times 2 \\
 \hline
 132
 \end{array}$$

$$\begin{array}{r}
 4 \mid 7 \mid 1 \\
 4 \\
 \hline
 3
 \end{array}$$

$$\begin{array}{r}
 2 \\
 33 \quad 4 \mid 9 \mid 2 \\
 \times 3 \\
 \hline
 231
 \end{array}$$

$$\begin{array}{r}
 4 \mid 11 \mid 2 \\
 8 \\
 \hline
 3
 \end{array}$$

$$\text{Quotient} = (331)_4$$

$$\text{Remainder} = (3)_4$$