

K Map Scenario Based Practice Problems

*For all problems, if you are asked to draw the circuit, you will need to draw the circuit too.

Question 1

In planet Z, there have been two new discoveries of Condition A and Condition B in plants. You have been tasked with creating a system which will detect the chances of development of Conditions A and B in plants. The conditions depend on the following factors:

Inputs (Factors) :

W: High Temperature. (W=1 if the temperature is high, W=0 otherwise)

X: Oxygen Level (X=1 if oxygen level is normal, X=0 otherwise)

Y: Presence of UV Light (Y=1 if UV light is present, Y=0 otherwise)

Z :Humidity (Z= 1 if the humidity is high, Z=0 otherwise)

Outputs: A : Condition A

B : Condition B

1. A plant will develop Condition A if **presence of UV Light** is accompanied by
 - i) **a high temperature with normal oxygen level**
 - or
 - ii) **low humidity.**
2. If **UV Light is absent** then the plant will develop Condition A if there is
 - i) **an abnormal level of oxygen**
 - or
 - ii) **there is high humidity with low temperature**
3. If the **oxygen level is not normal** or **there is high humidity with low temperature** then the plant will develop Condition B.

Devise a truth table for the system above which will detect the presence of the conditions based on the given factors. In your truth table, the input columns should be in the order WXYZ, where W is the MSB and Z is the LSB.

Draw K-map (s) based on the scenario above and derive simplified output (s).

Question 1 Answer

$$A = \sum m(0, 1, 2, 5, 6, 8, 9, 10, 14, 15) = W'Y'Z + X'Y' + YZ' + WXY = Y'(W'Z + X') + Y(WX + Z')$$

$$B = \sum m(0, 1, 2, 3, 5, 7, 8, 9, 10, 11) = X' + W'Z$$

minterm	W	X	Y	Z	A	B
0	0	0	0	0	1	1
1	0	0	0	1	1	1
2	0	0	1	0	1	1
3	0	0	1	1	0	1
4	0	1	0	0	0	0
5	0	1	0	1	1	1
6	0	1	1	0	1	0
7	0	1	1	1	0	1
8	1	0	0	0	1	1
9	1	0	0	1	1	1
10	1	0	1	0	1	1
11	1	0	1	1	0	1
12	1	1	0	0	0	0
13	1	1	0	1	0	0
14	1	1	1	0	1	0
15	1	1	1	1	1	0

Question 2

A new bizarre coffee machine has two LED lights, RED and GREEN which light up based on certain inputs. You are asked to derive the internal circuit of the machine which enables the lights to glow. Depending on the inputs both the lights, any one of the lights or none of the lights may glow.

Inputs (Symptoms) :

W: Water Temperature. (W=1 if the water temperature is high, W=0 otherwise)

X: Amount of coffee beans (X=1 if sufficient amount of coffee beans is present, X=0 otherwise)

Y: Presence of Milk (Y=1 if milk is present, Y=0 otherwise)

Z :Sugar Level (Z= 1 if sugar level is normal, Z=0 otherwise)

Outputs: R : RED LED

G : GREEN LED

1. The RED LED will light up if there is **milk present** and there is
 - i) **an absence of coffee beans**
 - or
 - ii) **normal sugar level with low water temperature.**
2. If there is **no milk** then the RED LED will still glow up if there is
 - i) **normal sugar level.**
 - or
 - ii) **a high water temperature with an adequate amount of coffee.**
3. The GREEN LED will light up if the **sugar level is normal** or **when there is a high water temperature with sufficient amount of coffee beans present.**

Devise a truth table for the system above which will detect the presence of the diseases based on the given symptoms. **In your truth table, the input columns should be in the order WXYZ, where W is the MSB and Z is the LSB.**

Question 2 Answer

$$R = \sum m(1, 2, 3, 5, 7, 9, 10, 11, 12, 13) = W'Z + X'Z + X'Y + WXY'$$

$$= Y(W'Z + X') + Y'(WX + Z) \text{ (condition)}$$

$$G = \sum m(1, 3, 5, 7, 9, 11, 12, 13, 14, 15) = Z + WX$$

minterm	W	X	Y	Z	R	G
0	0	0	0	0	0	0
1	0	0	0	1	1	1
2	0	0	1	0	1	0
3	0	0	1	1	1	1
4	0	1	0	0	0	0
5	0	1	0	1	1	1
6	0	1	1	0	0	0
7	0	1	1	1	1	1
8	1	0	0	0	0	0
9	1	0	0	1	1	1
10	1	0	1	0	1	0
11	1	0	1	1	1	1
12	1	1	0	0	1	1
13	1	1	0	1	1	1
14	1	1	1	0	0	1
15	1	1	1	1	0	1

Question 3

On planet Z, there have been two new outbreaks of Disease X and Disease Y. You have been tasked with creating a system which will detect the presence of Diseases X and Y. A person may have no disease or any one of the diseases or both. The presence of the diseases will depend on the following symptoms:

Inputs (Symptoms) :

- A: Breathing Difficulties. (A=1 if you have breathing difficulties, A=0 otherwise)
- B: Normal Body Temperature (B=1 if you have a normal body temperature, B=0 otherwise)
- C: Fatigue (C=1 if you have fatigue, C=0 otherwise)
- D :Loss of smell (D= 1 if the person has lost his ability of smell, D=0 otherwise)

Outputs: X : Disease X
Y : Disease Y

1. You have Disease X if your **fatigue** is accompanied by
 - i) **breathing difficulties with normal body temperature**
or
 - ii) **no loss of smell.**
2. If you **don't have fatigue** then you will have Disease X if you have
 - i) **an abnormal body temperature**
or
 - ii) **you have loss of smell with no breathing difficulties**
3. If you **don't have a normal body temperature** or **you have lost your sense of smell with no breathing difficulties** then you have Disease Y.

Devise a truth table for the system above which will detect the presence of the diseases based on the given symptoms. **In your truth table, the input columns should be in the order ABCD, where A is the MSB and D is the LSB.**

Draw K-map (s) based on the scenario above and derive simplified output (s).

Question 3 Answer

$$X = \sum m(0,1,2,5,6,8,9,10,14,15) = A'C'D + B'C' + CD' + ABC = C'(A'D + B') + C(AB + D')$$

$$Y = \sum m(0,1,2,3,5,7,8,9,10,11) = B' + A'D$$

minterm	A	B	C	D	X	Y
0	0	0	0	0	1	1
1	0	0	0	1	1	1
2	0	0	1	0	1	1
3	0	0	1	1	0	1
4	0	1	0	0	0	0
5	0	1	0	1	1	1
6	0	1	1	0	1	0
7	0	1	1	1	0	1
8	1	0	0	0	1	1
9	1	0	0	1	1	1
10	1	0	1	0	1	1
11	1	0	1	1	0	1
12	1	1	0	0	0	0
13	1	1	0	1	0	0
14	1	1	1	0	1	0
15	1	1	1	1	1	0

Question 4

On planet Z, there have been two new outbreaks of Disease X and Disease Y. You have been tasked with creating a system which will detect the presence of Diseases X and Y. A person may have no disease or any one of the diseases or both. The presence of the diseases will depend on the following symptoms:

Inputs (Symptoms) :

- A: Normal Breathing. (A=1 if you have normal breathing, A=0 otherwise)
- B: Abnormal Body Temperature (B=1 if you have an abnormal body temperature, B=0 otherwise)
- C: Fatigue (C=1 if you have fatigue, C=0 otherwise)
- D :Loss of smell (D= 1 if the person has lost his ability of smell, D=0 otherwise)

Outputs: X : Disease X

1. You have Disease X if your **fatigue** is accompanied by
 - i) **abnormal breathing with normal body temperature**
 - or
 - ii) **loss of smell.**
2. If you **don't have fatigue** then you will have Disease X if you have
 - i) **an abnormal body temperature**
 - or
 - ii) **you have loss of smell with normal breathing**
3. If you have **fatigue** or **you have an abnormal body temperature with loss of sense of smell** then you have Disease Y.

Devise a truth table for the system above which will detect the presence of the diseases based on the given symptoms. **In your truth table, the input columns should be in the order ABCD, where A is the MSB and D is the LSB.**

Draw K-map (s) based on the scenario above and derive simplified output (s).

Question 4 Answer

$$X = \sum m(2,3,4,5,7,9,11,12,13,15) = AD + CD + BC' + A'B'C$$

$$\text{## } C'(AD+B) + C(A'B'+D) = AC'D + BC' + A'B'C + CD(\text{condition})$$

$$Y = \sum m(2,3,5,6,7,10,11,13,14,15) = C + BD$$

minterm	A	B	C	D	X	Y
0	0	0	0	0	0	0
1	0	0	0	1	0	0
2	0	0	1	0	1	1
3	0	0	1	1	1	1
4	0	1	0	0	1	0
5	0	1	0	1	1	1
6	0	1	1	0	0	1
7	0	1	1	1	1	1
8	1	0	0	0	0	0
9	1	0	0	1	1	0
10	1	0	1	0	0	1
11	1	0	1	1	1	1
12	1	1	0	0	1	0
13	1	1	0	1	1	1
14	1	1	1	0	0	1
15	1	1	1	1	1	1

Question 5

In planet Z, there have been two new discoveries of Condition A and Condition B in plants. You have been tasked with creating a system which will detect the chances of development of Conditions A and B in plants. The conditions depend on the following factors:

Inputs (Symptoms) :

W: Low Temperature. (W=1 if the temperature is Low, W=0 otherwise)

X: Oxygen Level (X=1 if oxygen level is abnormal, X=0 otherwise)

Y: Presence of UV Light (Y=1 if UV light is present, Y=0 otherwise)

Z :Humidity (Z= 1 if the humidity is high, Z=0 otherwise)

Outputs: A : Condition A

B : Condition B

1. A plant will develop Condition A if **presence of UV Light** is accompanied by
 - i) **high temperature with normal oxygen level**
 - or
 - ii) **low humidity.**
2. If **UV Light is absent** then the plant will develop Condition A if there is
 - i) **an abnormal level of oxygen**
 - or
 - ii) **high humidity with low temperature**
3. If there is an **abnormal level of oxygen** or **UV light is present in high humidity** then the plant will develop Condition B.

Devise a truth table for the system above which will detect the presence of the conditions based on the given factors. In your truth table, the input columns should be in the order WXYZ, where W is the MSB and Z is the LSB.

Draw K-map (s) based on the scenario above and derive simplified output (s).

Question 5 Answer

$$A = \sum m(2,3,4,5,6,9,10,12,13,14) = WY'Z + XY' + YZ' + W'X'Y = Y'(WZ + X) + Y(W'X' + Z')$$

$$B = \sum m(3,4,5,6,7,11,12,13,14,15) = X + YZ$$

minterm	W	X	Y	Z	A	B
0	0	0	0	0	0	0
1	0	0	0	1	0	0
2	0	0	1	0	1	0
3	0	0	1	1	1	1
4	0	1	0	0	1	1
5	0	1	0	1	1	1
6	0	1	1	0	1	1
7	0	1	1	1	0	1
8	1	0	0	0	0	0
9	1	0	0	1	1	0
10	1	0	1	0	1	0
11	1	0	1	1	0	1
12	1	1	0	0	1	1
13	1	1	0	1	1	1
14	1	1	1	0	1	1
15	1	1	1	1	0	1

Question No. 6 : Rock Scissors Game

Rock-paper-scissors is a game usually played between two people, in which each player simultaneously forms one of three shapes with an outstretched hand. These shapes are "rock" (a simple fist), "paper" (a flat hand), and "scissors" (a fist with the index and middle fingers together forming a V). The game has only three possible outcomes other than a tie: a player who decides to play rock will beat another player who has chosen scissors ("rock crushes scissors") but will lose to one who has played paper ("paper covers rock"); a play of paper will lose to a play of scissors ("scissors cut paper"). This time we have decided to slightly modify the game with only two options, Rock and Scissor.

Input (4 variables)

$R1 = 1$ indicates Player 1 has chosen **Rock**.

$S1 = 0$ indicates Player 1 has not chosen **Scissor**.

$R2 = 0$ indicates Player 2 has not chosen **Rock**.

$S2 = 1$ indicates Player 2 has chosen **Scissor**.

Output (3 variables)

$P1 = 1$ indicates **Player 1 is winner**

$P2 = 1$ indicates **Player 2 is winner**

$D = 1$ indicates **there is a tie**

We have to consider the following points when designing the game:

- i) If player 1 or player 2 has not chosen anything, there will be **no winner nor tie**.
- ii) A player cannot choose rock and scissor both at a time. This state can be considered as **DON'T CARE**.
 - a) Using the above specification, prepare a truth table for the game.
 - b) Using 4 variable Karnaugh-Map method, derive SOP expressions for all of the three possible results.

Solution:

R1	S1	R2	S2	P1	P2	D	
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	0	0	0	0	2
0	0	1	1	x	x	x	3
0	1	0	0	0	0	0	4
0	1	0	1	0	0	1	5
0	1	1	0	0	1	0	6
0	1	1	1	x	x	x	7
1	0	0	0	0	0	0	8
1	0	0	1	1	0	0	9
1	0	1	0	0	0	1	10
1	0	1	1	x	x	x	11
1	1	0	0	x	x	x	12
1	1	0	1	x	x	x	13
1	1	1	0	x	x	x	14
1	1	1	1	x	x	x	15

	R2!	R2!	R2	R2	
R1!			x		S1!
R1!			x		S1
R1	x	x	x	x	S1
R1		1	x		S1!
	S2!	S2	S2	S2!	

$P1 = R1S2$

	R2!	R2!	R2	R2	
R1!			x		S1!
R1!			x	1	S1
R1	x	x	x	x	S1
R1			x		S1!
	S2!	S2	S2	S2!	

$P2 = R2S1$

	R2!	R2!	R2	R2	
R1!			x		S1!
R1!		1	x		S1
R1	x	x	x	x	S1
R1			x	1	S1!
	S2!	S2	S2	S2!	

$D = S1S2 + R1R2$