

CSE330- Numerical Methods
Quiz 01; Fall'24

Grade

Name: Suhit ID: 1930..... Section: 17

Marks: 15 points

Time: 20 minutes

Instructions: Answer all questions on the space provided below for each.

Question 1: CO2 (3+3+3 points): Given $\beta = 2$, $m = 2$ and $e \in \{-1, 0, 1\}$. Using denormalized form answer the following questions:

a) Compute the Machine Epsilon.

$$= \frac{1}{2} \beta^{-m} = \frac{1}{2} \beta^{-2} = \frac{1}{2} \times 2^{-2} = 2^{-3} = (0.125)_{10}$$

b) Compute the minimum of $|x|$ (non-negative).

$$\text{Denormalised form} = (0.1d_1d_2)_{\beta} \times \beta^e \quad m=2$$

$$= (0.100)_2 \times 2^{-1} = \underbrace{(0.100)_2}_{|x|} \times 2^{-1}$$

c) How many numbers can be represented using this system.

$$0.1d_1d_2; 2^2; \text{exp range} = 3; \text{So, } 2^2 \times 3; \text{total} = \underbrace{12}_{\text{positive}} + \underbrace{12}_{\text{negative}} = 24$$

$$= 12$$

Question 2: CO3 (6 points): Given a system with $\beta = 2$, $m = 3$, What will be the product of $x = \frac{3}{8}$ and $y = \frac{7}{8}$.

$$x \star y = \frac{3}{8} \star \frac{7}{8} = \frac{21}{64} = \frac{1}{64} + \frac{16}{64} + \frac{4}{64} = 2^{-6} + 2^{-2} + 2^{-4}$$

$$= (0.010101)_2$$

$m=3$

$$H.(x \star y) = (0.011)_2$$