

CSE330 Assignment-2 [Spring-2025]

[CO3]

Total Marks: 25

Instructions for submission: [Handwritten submission]

- Write your Name, Student_ID, Section No. in the cover page of the assignment.
 - Mark the answers properly for each corresponding question.
 - Note: All the calculations of CSE330 course must be done with radian mode of calculator.
 - There is no late submission policy.
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1. Consider the following table of data points/nodal points:

Time t (sec)	Velocity (ms ⁻¹) v(t)
2	10
4	20
6	25

a. [4+1 marks] Find an interpolating polynomial of velocity that goes through the above data points by using **the Vandermonde Matrix method**. Also compute an approximate value of acceleration at time, **t = 8 sec**.

b. [4 marks] Find an interpolating polynomial of velocity that goes through the above data points by using **the Lagrange Interpolation Method**.

c. [2 marks] If a **new data point** is added in the above scenario, which method should you use in finding a new interpolating polynomial? Also, what will be the degree of the new polynomial?

2. Read the following and answer accordingly:

a. (4 marks) Consider the nodes $[-\pi/2, 0, \pi/2]$. Find an interpolating polynomial of appropriate degree by using **Newton's divided-difference method** for **$f(x) = x \sin(x)$** .

b. (1 mark) Use the interpolating polynomial to find an approximate value at node $= \pi/3$.

c. (4 marks) Add a new node π to the above nodes and find the interpolating polynomial of appropriate degree.

3. [5 marks] The function $f(x) = e^{3x} - e^{-3x}$ has been interpolated at the nodes at **(-1, 0, 1)** using the Vandermonde matrix method. Evaluate the **upper bound of the interpolation error** for the interval **[-1.5, 1.5]** using **Cauchy's theorem**. Keep your answers upto to 5 significant figures.