

$\{ P_4, P_7 \}$
 C_1 continuous
 spline
 C_1 continuity
 match
 कसरी।

$$Q(t) = (1 - 3t + 3t^2 - t^3) P_1 + (3t - 6t^2 + 3t^3) P_2 + (3t^2 - 3t^3) P_3 + t^3 P_4$$

$$A'(t) = (-3 + 6t - 3t^2) P_1 + (3 - 12t + 9t^2) P_2 + (6t - 9t^2) P_3 + 3t^2 P_4$$

$$B'(t) = (-3 + 6t - 3t^2) P_4 + (3 - 12t + 9t^2) P_5 + (6t - 9t^2) P_6 + 3t^2 P_7$$

$$C'(t) = (-3 + 6t - 3t^2) P_7 + (3 - 12t + 9t^2) P_8 + (6t - 9t^2) P_9 + 3t^2 P_{10}$$

$$A'(1) = (-3 + 6 - 3) P_1 + (3 - 12 + 9) P_2 + (6 - 9) P_3 + 3 P_4$$

$$= -3 P_3 + 3 P_4$$

$$A'(1) = 3 (P_4 - P_3)$$

$$\xrightarrow{P_3 \rightarrow P_4}$$

TOPIC NAME : _____

DAY : _____

TIME : _____ DATE : / /

$$B'(0) = (-3)P_4 + (-3)P_5 + (4-2) = (1)P_4$$

$$= 3(P_5 - P_4)$$

$$3(P_4 - P_3) = 3(P_5 - P_4)$$

$$\Rightarrow \boxed{P_5 = 2P_4 - P_3}$$

$$B'(1) = (-3+6-3)P_4 + (3-12+9)P_5 + (6-9)P_6$$

$$= -3P_6 + 3P_7$$

$$= 3(P_7 - P_6)$$

$$C'(0) = -3P_7 + 3P_8$$

$$= 3(P_8 - P_7)$$

$$3(P_7 - P_6) = 3(P_8 - P_7)$$

$$\therefore \boxed{P_8 = 2P_7 - P_6}$$

$$A''(t) = (6 - 6t)P_1 + (-12 + 18t)P_2 + (6 - 18t)P_3 + 6tP_4$$

$$B''(t) = (6 - 6t)P_4 + (-12 + 18t)P_5 + (6 - 18t)P_6 + 6tP_7$$

$$C''(t) = (6 - 6t)P_7 + (-12 + 18t)P_8 + (6 - 18t)P_9 + 6tP_{10}$$

$$P_5 = 2P_4 - P_3$$

$$P_8 = 2P_7 - P_6$$

$$A''(1) = B''(0)$$

$$\Rightarrow 6P_2 - 12P_3 + 6P_4 = 6P_4 - 12P_5 + 6P_6$$

$$\Rightarrow 6P_2 - 12P_3 + 6P_4 - 6P_4 = -12(2P_4 - P_3) + 6P_6$$

$$\Rightarrow 6P_2 - 12P_3 = -24P_4 + 12P_3 + 6P_6$$

$$\Rightarrow P_6 = \frac{6P_2 - 12P_3 - 12P_3 + 24P_4}{6}$$

$$= \frac{6P_2 - 24P_3 + 24P_4}{6}$$

$$= P_2 - 4P_3 + 4P_4$$

$$P_6 = P_2 + 4(P_4 - P_3)$$

TOPIC NAME: _____

DAY: _____

TIME: _____

DATE: / /

$$B''(1) = C''(0)$$

$$\Rightarrow 6P_5 - 12P_6 + 6P_7 = 6P_7 - 12P_8 + 6P_9$$

$$\Rightarrow 6P_5 - 12P_6 = -12P_8 + 6P_9$$

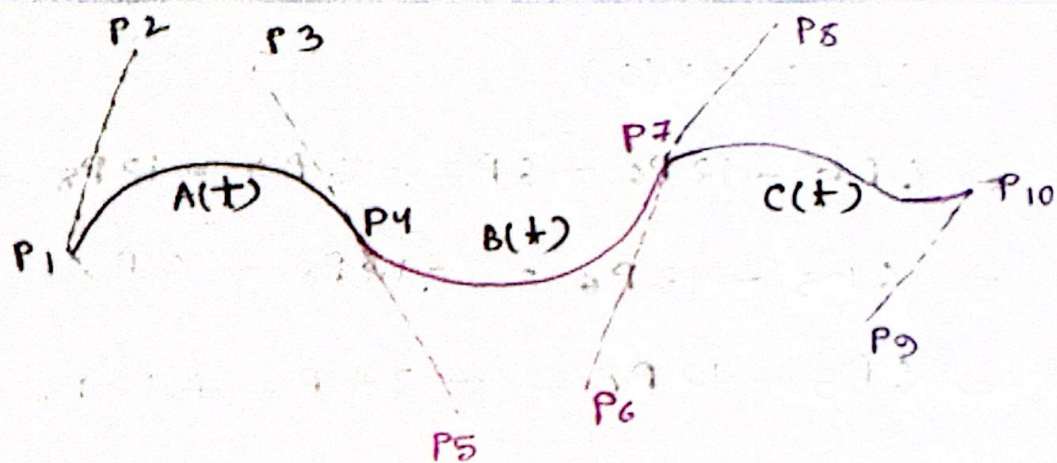
$$\Rightarrow 6P_5 - 12P_6 = -24P_7 + 12P_6 + 6P_9$$

$$\Rightarrow 6P_5 - 12P_6 + 24P_7 - 12P_6 = 6P_9$$

$$\Rightarrow 6P_5 - 24P_6 + 24P_7 = 6P_9$$

$$\Rightarrow P_5 - 4P_6 + 4P_7 = P_9$$

$$\Rightarrow \boxed{P_9 = P_5 + 4(P_7 - P_6)}$$



For C^0 continuity:

$$A(1) = B(0)$$

For C^1 continuity:

$$A'(1) = B'(0)$$

$$P_5 = 2P_4 - P_3$$

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Basically
2nd control
point of
the 2nd curve
needs to be
equal to

Last control
point of
previous
curve

2nd last
control
point of
previous
curve

$$P_8 = 2P_7 - P_6$$

TOPIC NAME: _____

DAY: _____

TIME: _____

DATE: / /

For C^2 continuity:

$$A''(1) = B''(0)$$

$$P_6 = P_2 + A(P_4 - P_3)$$

3rd control point of curve
 2nd control point of previous
 4th control point of previous
 3rd control point of previous

$$P_9 = P_5 + A(P_7 - P_6) = (5, -2)$$

- * $P_1 (0, 0)$
- $P_2 (1, 2)$
- $P_3 (2, 2)$
- $P_4 (3, 0)$
- $P_5 (4, -2)$
- $P_6 (5, -2)$
- $P_7 (6, 0)$
- $P_8 (7, 2)$
- $P_9 (8, 2)$
- $P_{10} (9, 0)$
- A
 B
 C

C^1 continuity

$$P_5 = 2P_4 - P_3$$

$$\Rightarrow (4, -2) = 2(3, 0) - (2, 2)$$

$$= (6, 0) - (2, 2)$$

$$= (4, -2)$$

$A, B \rightarrow C^1$ continuous

$$P_8 = 2P_7 - P_6$$

$$\Rightarrow (7, 2) = 2(6, 0) - (5, -2)$$

$$= (12, 0) + (5, -2) = (7, 2)$$

$B, C \rightarrow C^1$ continuous

 C^2 continuity

$$P_6 = P_2 + 4(P_4 - P_3)$$

$$(5, -2) = (1, 2) + 4((3, 0) - (2, 2))$$

$$= (1, 2) + 4(1, -2)$$

$$= (1, 2) + (4, -8)$$

$$= (5, -6)$$

$$(5, -2) \neq (5, -6)$$

$A, B \rightarrow$ not C^2 continuous

TOPIC NAME : _____

DAY : _____

TIME : _____

DATE : / /

$$P_9 = P_5 + 4(P_7 - P_6)$$

$$\begin{aligned}\Rightarrow (8, 2) &= (1, -2) + 4((6, 0) - (5, -2)) \\ &= (1, -2) + 4(1, 2) \\ &= (1, -2) + (4, 8) \\ &= (8, 6)\end{aligned}$$

$$(8, 2) \neq (8, 6)$$

B, C \rightarrow not C^2 continuous

If I update P_6 as $(5, -6)$

and P_9 as $(8, 6)$, we'll have C^2 continuous for both curve.

Azmari