$\mathbf{Q1}$. For each of the following pairs of integers, write a in the form

$$a = bq + r$$

where q is the quotient and r is the remainder, with $0 \le r < |b|$.

- (i). a = 417, b = 34
- (ii). a = 1052, b = 29
- (iii). a = -121, b = 29
- (iv). a = 2396, b = -11
- (v). a = -121, b = -29

Q2. Using "brute force", i.e., by listing factors, find the gcd of

- (i). 60 and 84
- (ii). 98 and 56

Q3. Using Euclid's algorithm, find the gcd of

- (i). 60 and 84
- (ii). 98 and 56
- (iii). 816 and 612
- (iv). 2064499 and 238067

Q4. Calculate the lcm of

- (i). 60 and 84
- (ii). 98 and 56
- (iii). 816 and 612
- (iv). 2064499 and 238067

Answers:

Q1.

- (i). 417 = 34(12) + 9
- (ii). 1052 = 29(36) + 8
- (iii). -121 = 29(-5) + 24
- (iv). 2396 = -11(-217) + 9
- (v). -121 = -29(5) + 24

Q2.

- (i). 12
- (ii). 14

Q3.

- (i). 12
- (ii). 14
- (iii). 204
- (iv). 751

Q4.

- (i). 420
- (ii). 392
- (iii). 2448
- (iv). 654, 446, 183