

CENTER FOR BIOLOGICAL & COMPUTATIONAL LEARNING (CBCL)



GURLS A LEAST SQUARES-BASED LIBRARY FOR STATE OF THE ART SUPERVISED LEARNING

BASIC DOCUMENTATION

Authors	Affiliation
Andrea Tacchetti	CBCL
Pavan K. Mallapragada	CBCL
Matteo Santoro	CBCL, IIT@MIT Lab
Lorenzo Rosasco	CBCL, IIT@MIT Lab

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CHAPTER 1

Introduction

1.1 Welcome

Gurls – which stands for *Grand Unified Regularized Least Squares* – is a software library for regression and (multiclass) classification based on the Regularized Least Squares (RLS) loss function. The library comprises four main modules. Gurls and BGurls – both implemented in Matlab – are aimed at solving learning problems with small/medium and large-scale datasets respectively. Gurls $^{++}$ and BGurls $^{++}$ are their C^{++} counterparts.

The library takes advantage of some favorable properties of regularized least squares algorithm and is tailored to deal in particular with multi-category/multi-label problems. The package comprises useful routines to perform automatic parameter selection and can handle computations with very large matrices by means of both memory-mapped storage and distributed task execution.

GURLS is distributed under the simplified BSD license. Source code, and binaries can be downloaded from https://github.com/CBCL/GURLS.

The present document describes both the API design and the usage of the GURLS library for machine learning researchers.

1.2 Motivations

The design of GURLS is based upon the following requirements.

Speed Binary learning must be efficient and multi-output learning must scale sub-linearly with respect to the number of classes – both during training and model selection.

Memory It must be possible to work with large datasets non only by relying on online optimization strategies but also on batch methods (either in the primal or the dual space).

Performance We are interested in achieving state of the art results in multiclass problems in particular with tens or hundreds of classes, where the input may have dense features.

The crucial optimisation step in GURLS is implemented through regularised least squares (RLS), because RLS-based estimators have a number of favourable properties. Among others, we mention:

- the whole regularisation path can be computed at essentially the same cost of training a single model;
- both leave-one-out values and errors can be computed in closed form;
- training complexity of multi-class classifiers is independent from the number of classes;
- the regularization parameter is directly linked to the spectral properties of the kernel matrix, and search ranges for the optimal parameter can be automatically set without any input from the user.

Note that such results are classical, and some of them are unique of least squares giving us an important help practice, since they allow for the selection of the best possible model complexity.

In order to be competitive also in the large-scale machine learning scenario, we focused on the problem of dealing with very large data matrices, which may be not even loaded in memory. BGURLS is specifically designed for this purpose, and is a library built around a custom implementation of memory-mapped files. It allows one to learn from extremely large collections of data and provides several tools that help the user to set up the learning pipeline in the most efficient way, and include a distributed manager to perform the key step of matrix-matrix multiplications without loading the whole dataset in memory.

In our work, we put emphasis on designing a compact and easy-to-use API, on performance and on clarity and completeness of documentation. GURLS has minimal external dependencies, and has been deployed and tested successfully on the Linux, Mac and Windows.

1.3 Getting started

1.3.1 Downloading the GURLS package

The Home Page of the GURLS package is at http://cbcl.mit.edu/gurls/, where you will find useful information about the GURLS project, the authors and a link to the research group where the library has been designed and developed, and the link to the GITHUB repository (http://github.com/CBCL/GURLS) from which the source code can be downloaded.

1.3.2 Installing GURLS

GURLS is a pure Matlab library and has no specific dependencies on external libraries, made exception for the stats toolbox (see Subsection 3.3.1). Once the compressed archive has been downloaded on your machine from the GITHUB repository, you need to save it in the desired GURLSROOT. Then open MATLAB and execute:

```
>> run('GURLSROOT/gurls/utils/gurls_install.m');
```

This will add all the important directories to your path. Run savepath if you want the installation to be permanent.

1.3.3 Installing BGURLS

BGURLS is a pure Matlab library and has no specific dependencies on external libraries, made exception for the GURLS library and the stats toolbox (see Subsection 3.3.1). Once the compressed archive has been downloaded on your machine from the GITHUB repository, you need to save it in the desired GURLSROOT. Then open MATLAB and execute:

```
>> run('GURLSROOT/bgurls/utils/bgurls_install.m');
```

This will add all the important directories to your path. Run savepath if you want the installation to be permanent.

1.3.4 Installing GURLS⁺⁺

In the following we assume that the source code of GURLS⁺⁺is located at GURLSROOT.

Installing GURLS⁺⁺on Linux

Below we describe how to build and install Gurls⁺⁺ on Ubuntu (tested on Ubuntu 10.04). For other distributions, the same packages must be installed with the distribution-specific method.

1. Install the cmake build system (www.cmake.org/)

```
$ sudo apt-get install cmake
```

- 2. Install your favourite Blas/Lapack implementation. Currently we support:
 - ATLAS: http://math-atlas.sourceforge.net;
 - AMD's ACML: http://developer.amd.com/libraries/acml;
 - Intel's MKL: http://software.intel.com/en-us/articles/intel-mkl;
 - Netlib's reference implementation: http://www.netlib.org/blas and http://www.netlib.org/lapack/.

As an example, to install Netlib's Blas and Lapack run the following command:

```
$ sudo apt-get install libblas-dev libblas3gf liblapack3gf
```

3. Install Boost's libraries date_time and serialization

```
$ sudo apt-get install libboost-serialization1.40.0 libboost-serialization1.40-dev libboost-date-time1.40.0 libboost-date-time1.40-dev
```

4. To link against some Blas and Lapack implementations you may need a fortran compiler e.g. for Netlib's Blas and Lapack:

```
$ sudo apt-get install gfortran
```

5. Create a build directory (e.g. "build") for GURLS⁺⁺

```
$ cd GURLSROOT
$ mkdir build
```

6. Run cmake into the build directory

```
$ cd build
$ ccmake ...
```

The last command will show the CMake interface, which must be used to set the values of some variables used for building and installing Gurls⁺⁺. See the section **Configuring** Gurls⁺⁺ below for more information on these variables and how to set them to appropriate values.

7. Start GURLS⁺⁺building

```
$ make
```

8. Install Gurls⁺⁺to the path defined at configuration time

```
$ make install
```

Installing GURLS⁺⁺on Windows

Below we describe how to build and install Gurls⁺⁺on Windows with Visual Studio (tested with VS Express 2010 on Windows 7 and with VS Express 2008 on Windows Vista).

- 1. Install the CMake build system downloading the installer from http://cmake.org/cmake/resources/software.html.
- 2. Install your favourite Blas/Lapack implementation. Currently we support:
 - ATLAS: http://math-atlas.sourceforge.net;
 - AMD's ACML: http://developer.amd.com/libraries/acml;
 - Intel's MKL: http://software.intel.com/en-us/articles/intel-mkl.

Under Windows ACML is probably the easiest choice, since they provide the library binaries for free.

3. Install Boost's date_time and serialization libraries following the instructions on Boost's website: http://www.boost.org/doc/libs/1_50_0/more/getting_started/windows.html.

- 4. Create a build directory (e.g. GURLSROOT/build) for GURLS⁺⁺.
- 5. Run the CMake GUI.

You will have to set the source directory to the root directory holding GURLS⁺⁺source code, and the build directory to the directory created at the previous step.

After pressing the configure button, you have to set the values of some variables used for building and installing Gurls⁺⁺. See the section **Configuring** Gurls⁺⁺ below for more information on these variables and how to set them to appropriate values. After having configured the build options, press the generate button to create the solution file.

- 6. Build GURLS⁺⁺by opening and building the solution under Visual Studio.
- 7. Install Gurls⁺⁺by explicitely building the install project included in the solution (it is not automatically built when building the solution).

Configuring GURLS⁺⁺

The configuration step is carried out using CMake.

Using the command-line interface you will be presented with a textual menu, where you can change the values of some variables and configure the building settings accordingly.

- 1. At the beginning no variable is set, and a message EMPTY CACHE is shown.
- 2. Press [c] for 'configure', and CMake will try to determine the correct values for all variables, such as the location of required libraries.
- 3. If CMake does not find some required library, an error message will be displayed. In this case press [e] to exit help and go to the main screen.
- 4. In the main screen you may change a number of variables. Most of them can be left unchanged, but some must be set to appropriate values. The following are the variables whose values should be checked:
 - BLAS_LAPACK_IMPLEMENTATION. Allows user to specify an implementation of the Blas/Lapack routines. Available choices are: ACML, ATLAS, MKL, NETLIB (under linux). Depending on the choice you make, CMake will try to find the libraries in standard locations in the system. Normally this process should run fine, however, in case the libraries have been installed in some non-standard directory, you may have to manually specify their location.
 - USE_BINARY_ARCHIVES. If set to ON, all data structures in GURLS are stored in binary (rather than text) files, saving storage space and time.

• BUILD_DEMO and BUILD_TEST. These two options enable the building of the demo and test programs. You may need to enable the latter if you are interested in expanding GURLS⁺⁺. If so, the directory for BUILD_TEST has to coincide with the directory that will be used to perform tests (see Section 4.5 for more details).

- CMAKE_INSTALL_PREFIX. This is the path where the library will be installed to.
- 5. Once all variables have been set, press [c] again, and CMake will check the settings. As in step (3), if something is wrong an error message will be displayed and you will have to go back to the main screen to tweak the configuration.
- 6. When the settings are correct, the option to 'generate' the files required for the actual build will appear. Press [g]. CMake will generate the files and exit.

After the build files (e.g. the Makefile under Linux) have been generated, you can proceed as explained above.

The same procedure outlined above is used when using the GUI of CMake, e.g. under Windows or Mac.

1.3.5 Installing BGURLS⁺⁺

In the following we assume that the source code of BGURLS⁺⁺ is located at \$ BGURLSROOT.

Installing BGURLS⁺⁺on Linux

Below we describe how to build and install BGURLS⁺⁺ on Ubuntu (tested on Ubuntu 12.04). For other distributions, the same packages must be installed with the distribution-specific method.

1. Install the cmake build system (www.cmake.org/)

```
$ sudo apt-get install cmake
```

- 2. Install your favourite Blas/Lapack implementation. Currently we support:
 - ATLAS: http://math-atlas.sourceforge.net;
 - AMD's ACML: http://developer.amd.com/libraries/acml;
 - Intel's MKL: http://software.intel.com/en-us/articles/intel-mkl;
 - Netlib's reference implementation: http://www.netlib.org/blas and http://www.netlib.org/lapack/.

As an example, to install Netlib's Blas and Lapack run the following command:

```
$ sudo apt-get install libblas-dev libblas3gf liblapack3gf
```

3. Install Boost's libraries date_time and serialization

```
$ sudo apt-get install libboost-serialization1.46.1 libboost-serialization1.46-dev libboost-date-time1.46.1 libboost-date-time1.46-dev
```

4. Install an MPI implementation (e.g. OpenMPI)

```
$ sudo apt-get install libopenmpi-dev openmpi-bin openmpi-doc
```

- 5. Build libNetCDF C and C⁺⁺libraries. Download "The netCDF C library and utilities" and "The netCDF legacy and netCDF-4 C⁺⁺libraries" from the official netCDF website (http://www.unidata.ucar.edu/downloads/netcdf/index.jsp) and build them. Building BGURLS⁺⁺using the libnetCDF packages provided by Ubuntu generates compiler errors.
- 6. To link against some Blas and Lapack implementations you may need a fortran compiler e.g. for Netlib's Blas and Lapack:

```
$ sudo apt-get install gfortran
```

7. Create a build directory (e.g. "build") for BGURLS⁺⁺

```
$ cd BGURLSROOT
$ mkdir build
```

8. Run cmake into the build directory

```
$ cd build
$ ccmake ..
```

The last command will show the CMake interface, which must be used to set the values of some variables used for building and installing BGURLS⁺⁺. See the section **Configuring** BGURLS⁺⁺ below for more information on these variables and how to set them to appropriate values.

9. Start BGURLS⁺⁺building

```
$ make
```

10. Install BGURLS⁺⁺to the path defined at configuration time

```
$ make install
```

Installing BGURLS⁺⁺**on Windows**

Below we describe how to build and install BGURLS⁺⁺ on Windows with Visual Studio (tested with VS Express 2010 on Windows 7 and with VS Express 2008 on Windows Vista).

- 1. Install the CMake build system downloading the installer from http://cmake.org/cmake/resources/software.html.
- 2. Install your favourite Blas/Lapack implementation. Currently we support:
 - ATLAS: http://math-atlas.sourceforge.net;
 - AMD's ACML: http://developer.amd.com/libraries/acml;
 - Intel's MKL: http://software.intel.com/en-us/articles/intel-mkl.

Under Windows ACML is probably the easiest choice, since they provide the library binaries for free.

- 3. Install Boost's date_time and serialization libraries following the instructions on Boost's website: http://www.boost.org/doc/libs/1_50_0/more/getting_started/windows.html.
- 4. Install your favorite MPI implementation. E.g. MPICH2 (http://www.mpich.org) provides precompiled binaries.
- 5. Install libNetCDF C and C⁺⁺libraries. Download "The netCDF C library and utilities" and "The netCDF legacy and netCDF-4 C⁺⁺libraries" from the official netCDF website (http://www.unidata.ucar.edu/downloads/netcdf/index.jsp) and build them. Alternatively you may try the precompiled binaries from http://www.unidata.ucar.edu/software/netcdf/win_netcdf/.
- 6. Create a build directory (e.g. BGURLSROOT/build) for BGURLS⁺⁺.
- 7. Run the CMake GUI.
 - You will have to set the source directory to the root directory holding BGURLS⁺⁺source code, and the build directory to the directory created at the previous step.
 - After pressing the configure button, you have to set the values of some variables used for building and installing BGURLS⁺⁺. See the section **Configuring** BGURLS⁺⁺ below for more information on these variables and how to set them to appropriate values. After having configured the build options, press the generate button to create the solution file.
- 8. Build BGURLS⁺⁺by opening and building the solution under Visual Studio.
- 9. Install BGURLS⁺⁺by explicitely building the install project included in the solution (it is not automatically built when building the solution).

Configuring BGURLS⁺⁺

The configuration step is carried out using CMake.

Using the command-line interface you will be presented with a textual menu, where you can change the values of some variables and configure the building settings accordingly.

- 1. At the beginning no variable is set, and a message EMPTY CACHE is shown.
- 2. Press [c] for 'configure', and CMake will try to determine the correct values for all variables, such as the location of required libraries.
- 3. If CMake does not find some required library, an error message will be displayed. In this case press [e] to exit help and go to the main screen.
- 4. In the main screen you may change a number of variables. Most of them can be left unchanged, but some must be set to appropriate values. The following are the variables whose values should be checked:
 - GURLSROOT. Directory containing GURLS⁺⁺code.
 - BLAS_LAPACK_IMPLEMENTATION. Allows user to specify an implementation of the Blas/Lapack routines. Available choices are: ACML, ATLAS, MKL, NETLIB (under linux). Depending on the choice you make, CMake will try to find the libraries in standard locations in the system. Normally this process should run fine, however, in case the libraries have been installed in some non-standard directory, you may have to manually specify their location.
 - USE_BINARY_ARCHIVES. If set to ON, all data structures in BGURLS are stored in binary (rather than text) files, saving storage space and time.
 - BUILD_DEMO and BUILD_TEST. These two options enable the building of the demo and test programs. You may need to enable the latter if you are interested in expanding BGURLS⁺⁺. If so, the directory for BUILD_TEST has to coincide with the directory that will be used to perform tests (see Section 4.5 for more details).
 - CMAKE_INSTALL_PREFIX. This is the path where the library will be installed to.
- 5. Once all variables have been set, press [c] again, and CMake will check the settings. As in step (3), if something is wrong an error message will be displayed and you will have to go back to the main screen to tweak the configuration.
- 6. When the settings are correct, the option to 'generate' the files required for the actual build will appear. Press [g]. CMake will generate the files and exit.

After the build files (e.g. the Makefile under Linux) have been generated, you can proceed as explained above.

The same procedure outlined above is used when using the GUI of CMake, e.g. under Windows or Mac.

1.3.6 Hello World in GURLS

Have a look, and run gurls_helloworld.m in the 'demo' subdirectory. Below we describe the demo in details. We first have to load the training data

```
>> load('data/quickanddirty_traindata;')
and train the classifier
>> [opt] = gurls_train(Xtr,ytr);
now we load the test data
>> load('data/quickanddirty_testdata');
then we predict the labels for the test set and asses prediction accuracy
>> [yhat,acc] = gurls_test(Xte,yte,opt);
```

1.3.7 Hello World in GURLS⁺⁺

Have a look, and run helloworld.cpp in the 'demo' subdirectory. Below we describe the salient parts of demo in details.

First we have to load the training data

```
Xtr = readFile<T>("../data/Xtr.txt");
ytr = readFile<T>("../data/ytr_onecolumn.txt");
and the test data

Xte = readFile<T>("../data/Xte.txt");
yte = readFile<T>("../data/yte_onecolumn.txt");
then we train the classifer

GurlsOptionsList* opt = gurls_train(*Xtr, *ytr);
finally we predict the labels for the test set and asses prediction accuracy
gurls_test(*Xte, *yte, *opt);
```

1.3.8 License

GURLS is distributed under the BSD license. This means that it is free for both academic and commercial use.

If you are going to use GURLS in your scientific work, please cite the library, the main website and the paper

```
Tacchetti, A., P. Mallapragada, M. Santoro, and L. Rosasco Gurls: a Toolbox for Large Scale Multiclass Learning, presented at Workshop: "Big Learning: Algorithms, Systems, and Tools for Learning at Scale" at NIPS 2011, December 16-17 2011, Sierra Nevada, Spain.
```

CHAPTER 2

User's Guide

In supervised learning, the building blocks of a learning experiment are its phases or *processes* (typically the training process and the testing process), that can be run on different data sets (typically the train and test set). What characterizes GURLS is the idea that processes within the same experiment share a common (ordered) sequence of *tasks* which we call the learning *pipeline*. Each GURLS process differs from the others on how each task is performed (e.g. compute or load previously computed results) and on the data used as input.

As both GURLS and GURLS++ are similarly designed, in the following we start describing GURLS design and usage, and later explain what changes in the C++ implementation. Then we described some additional functionalities of the package, precisely the normalization and visualization commands. In the remainder of the chapter, a number of commonly used experiments will be described.

2.1 GURLS design

GURLS (GURLS++) basically consists of a set of tasks, each one belonging to a predefined category, and of a method called GURLS *Core* (the gurls routine in Matlab, and the gurls class in C++) that is responsible for processing the task pipeline. An additional "options structure", often referred to as *OPT*, is used to store all configuration parameters needed to customize the tasks behaviour. Tasks receive configuration parameters from the options structure in readonly mode and, after terminating, their results are appended to the structure by the GURLS Core in order to make them available to the subsequent tasks. This allows the user to easily skip the execution of some tasks in a pipeline, by simply inserting the desired results directly into the options structure. All tasks belonging to the same category can be interchanged with each other, so that the user can easily choose how each task shall be carried out. A schema of the design and execution of a GURLS process is shown in Fig.2.1.

2. User's Guide 2.2. The first example

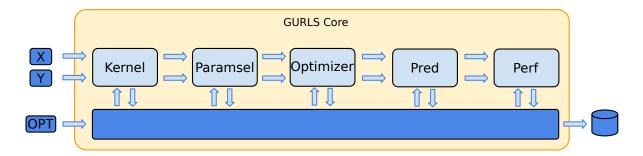


Figure 2.1: GURLS process.

2.2 The first example

The gurls command runs the learning pipeline and is the main function the user would directly call. It accepts exaclty four arguments:

- 1. the input data, stored in a $N \times D$ matrix, where N is the number of samples, D is the number of variables.
- 2. The data encoded labels stored in a $N \times T$ matrix, where T is the number of outputs. For (multi-class) classification, labels (+1,-1) must be in the One-Vs-All format.
- 3. An options' structure.
- 4. A job-id number.

Each time the data need to be changed (e.g. going from training process to testing process) gurls needs to be called again.

The options' structure is built through the defopt function with default fields and values. The three main fields in the options' structure are:

- opt.name: defines a name for a given experiment.
- opt.seq: specifies the (ordered) sequence of tasks, i.e. the pipeline, to be executed.
- opt.process: specifies what to do with each task. It has to be a cell array, where each cell specify the executions code for each job, i.e. gurls call. In particular here are the codes:
 - -0 = Ignore
 - **-** 1 = Compute
 - -2 = Compute and save
 - 3 = Load from file
 - 4 = Explicitly delete

Now, let's suppose we want to run the training process on a dataset (Xtr, ytr) and then test on a different dataset (Xte, yte). We are interested in the precision-recall performance measure as well as the average classification accuracy. In order to train a linear classifier using a leave one out cross-validation approach, we just need the following lines of code:

The meaning of the above code fragment is the following:

- For the training data: calculate the regularization parameter λ minimizing classification accuracy via Leave-One-Out cross-validation and save the result, solve RLS for a linear classifier in the primal space and save the solution. Ignore the rest.
- For the test data set, load the used λ (this is important if you want to save this value for further reference), load the classifier. Predict the output on the test-set and save it. Evaluate the two aforementioned performance measures and save them.

Note that the field opt.name is implicitly specified by the defopt function which assigns to it its only input argument. Fields opt.seq and opt.process have to be explicitly assigned.

2.3 Further examples

The gurls command executes an ordered sequence of tasks, the *pipeline*, specified in the field seq of the options' structure as

```
{' < CATEGORY1>: < TASK1>';' < CATEGORY2>: < TASK2>; ...}
```

These tasks can be combined in order to build different train-test pipelines. A list of the currently implemented GURLS tasks organized by category, is summarized in Table 2.1. Type

```
help <CATEGORY> <TASK>
```

(ex. help paramsel_hoprimal) for further reference on each task. The most popular learning pipelines are outlined in the following.

task category	description	available tasks
split	Splits data into one or more pair of	ho
spiit	training and validation sets	
	performs selection of the regularization parameter λ and, if using Gaussian kernel, also of the kernel parameter σ	fixlambda
		loocvprimal
		loocvdual
		hoprimal
		hodual
		siglam
paramsel		siglamho
		bfprimal
		bfdual
		calibratesgd
		hoprimalr
		hodualr
		horandfeats
		chisquared
	huilds the symmetric kernel matrix to be	linear
kernel	builds the symmetric kernel matrix to be used for training	load
		randfeats
		rbf
	solves RLS optimization problem	primal
		dual
		auto
rls		pegasos
		primalr
		dualr
		randfeats
predkernel	builds the train-test kernel matrix	traintest
_	predicts the labels	primal
pred		dual
		randfeats
	assess prediction performance	macroavg
perf		precrec
		rmse
		maxscore
conf	computes a confidence for the highest scoring class	gap
		boltzmangap
		boltzman

Table 2.1: List of GURLS tasks organized by category.

2.3.1 Linear classifier, primal case, hold-out cv

```
name = 'ExampleExperiment';
opt = defopt(name);
opt.seq = {'split:ho','paramsel:hoprimal','rls:primal',...
   'pred:primal','perf:macroavg'};
opt.process{1} = [2,2,2,0,0];
opt.process{2} = [3,3,3,2,2];
gurls(Xtr, ytr, opt,1)
gurls(Xte, yte, opt,2)
```

Here hold-out cross validation requires the training test to be split in one pair of train and validation sets. Splitting is performed in the first task, split, with choice ho.

2.3.2 Linear regression, primal case, hold-out cv

Here GURLS is used for regression. Note that the objective function is explicitly set to <code>@perf_rmse</code>, i.e. root mean square error, whereas in the first example <code>opt.hoperf</code> is set to its default <code>@perf_macroavg</code> which evaluates the average classification accuracy per class. The same code can be used for multiple output regression.

2.3.3 Linear classifier, dual case, leave one out cv

```
name = 'ExampleExperiment';
opt = defopt(name);
opt.seq = {'kernel:linear', 'paramsel:loocvdual', 'rls:dual', ...
    'pred:dual', 'perf:macroavg''};
opt.process{1} = [2,2,2,0,0];
opt.process{2} = [3,3,3,2,2];
gurls(Xtr, ytr, opt,1)
gurls(Xte, yte, opt,2)
```

Here the dual formulation requires the kernel matrix, which is built through the task linear belonging to the category kernel. Note that the train-test kernel matrix is not build as, with

linear kernel, prediction is implicitly performed in the primal formulation.

2.3.4 Gaussian Kernel, dual case, leave one out cv

```
name = 'ExampleExperiment';
opt = defopt(name);
opt.seq = {'paramsel:siglam', 'kernel:rbf', 'rls:dual', ...
  'predkernel:traintest', 'pred:dual', 'perf:macroavg'};
opt.process{1} = [2,2,2,0,0,0];
opt.process{2} = [3,3,3,2,2,2];
gurls(Xtr, ytr, opt,1)
gurls(Xte, yte, opt,2)
```

Here parameter selection for gaussian kernel requires selection of both the regularization parameter λ and the kernel parameter σ , and is performed selecting the task siglam for the category paramsel. Once the value for kernel parameter σ has been chosen, the gaussian kernel is built through the kernel task with option rbf.

2.3.5 Random features RLS, hold-out cv

```
name = 'ExampleExperiment';
opt = defopt(name);
opt.seq = {'split:ho','paramsel:horandfeats','kernel:randfeats','rls:randfeat
opt.process{1} = [2,2,2,2,0,0];
opt.process{2} = [3,3,3,3,2,2];
gurls(Xtr, ytr, opt,1)
gurls(Xte, yte, opt,2)
```

Computes a classifier for the primal formulation of RLS using the Random Features approach proposed by [35]. In this approach the primal formulation is used in a new space built through random projections of the input data.

2.3.6 Stocastic gradient descent

Here the optimization is carried out using a stochastic gradient descent algorithm, namely Pegasos [44].

2.4 Customizing the options' structure

The options structure passed as third input to gurls is built by function defopt with a set of default fields and values. Some of these fields can be manually customized by adding the line

```
opt.<FIELD> = <VALUE>;
```

before calling gurls, and after having built opt with defopt. In the example of Subsection 2.3.2, we have seen how field hoperf can be changed in order to deal with regression problems. Below we list the most important fields that can be customized

- nlambda (100): number of values for the regularization parameter
- nsigma (25): number of values for the kernel parameter.
- nholdouts (1): number of data splits to be used for hold-out cross validation.
- hoproportion (0.2): proportion between training and validation set in parameter selection
- hoperf (function @perf_macroavg): objective function to be used for parameter selection.
- epochs (4): number of passes over the training set for stocastic gradient descent
- subsize (50): training set size used for parameter selection when using stocastic gradient descent.
- singlelambda (function @mean): function for obtaining one value for the regularization parameter, given the parameter choice for each class in multiclass classification (for each output in multiple output regression).

As an example, in order to perform parameter selection on 5 different hold-out splits of the training set, with validation/training proportion set to 0.4, and with 20 and 10 values for the regularization and kernel parameter respectively, one has to run the following lines of code

```
name = 'ExampleExperiment';
opt = defopt(name);
opt.seq = {'split:ho', 'paramsel:siglamho', 'kernel:rbf', ...
   'rls:dual','predkernel:traintest', 'pred:dual', 'perf:macroavg'};
opt.process{1} = [2,2,2,2,0,0,0];
opt.process{2} = [3,3,3,3,2,2,2];
opt.nlambda = 20;
opt.nlambda = 20;
opt.nsigma = 10;
opt.hoproportion = 0.4;
opt.nholdouts = 5;
gurls(Xtr, ytr, opt,1)
gurls(Xte, yte, opt,2)
```

2.5 Examples in GURLS++

In C++ the counterpart of the gurls function is the GURLS class, with its only method run, whereas function defopt has its equivalent in the class GurlsOptionsList. In the 'demo' directory you will find GURLSloocvprimal.cpp, which implements exactly the first example described in Section 2.2. In the following we report it for completeness.

```
#include <iostream>
#include "gurls.h"
#include "exceptions.h"
#include "gmat2d.h"
#include "options.h"
#include "optlist.h"
using namespace gurls;
using namespace std;
typedef double T;
int main(int argc, char *argv[])
   string xtr_file, xte_file, ytr_file, yte_file;
// check that all inputs are given
   if(argc<4)
       std::cout << "========"<< std::endl
       << " Wrong parameters number ("<<argc <<")." << std::endl
       << " Provide a valid path for training, test and output files"
       << "using the following syntax:" << std::endl
       << " \n\n\t " << argv[0] << " xtr xte ytr yte" << std::endl
       << std::endl << std::endl;
       return 0;
// get file names from input
   xtr_file = argv[1];
   xte_file = argv[2];
   ytr_file = argv[3];
   yte_file = argv[4];
   try
   {
       gMat2D<T> *Xtr, *Xte, *ytr, *yte;
       // load data from file
```

```
Xtr.readCSV(xtr_file);
   Xte.readCSV(xte_file);
    ytr.readCSV(ytr_file);
    yte.readCSV(yte_file);
    // specify the task sequence
    OptTaskSequence *seq = new OptTaskSequence();
    *seq << "paramsel:loocvprimal" << "optimizer:rlsprimal";
    *seq<< "pred:primal" << "perf:macroavg" << "perf:precrec";
    GurlsOptionsList * process = new GurlsOptionsList("processes", false);
    // defines instructions for training process
    OptProcess* process1 = new OptProcess();
    *process1 << GURLS::computeNsave << GURLS::computeNsave;
    *process1 << GURLS::ignore << GURLS::ignore;
   process->addOpt("one", process1);
    // defines instructions for testing process
    OptProcess* process2 = new OptProcess();
    *process2 << GURLS::load << GURLS::load << GURLS::computeNsave;
    *process2 << GURLS::computeNsave << GURLS::computeNsave;
    process->addOpt("two", process2);
    // build an options' list
    GurlsOptionsList* opt = new GurlsOptionsList("{\sc Gurls}looprimal", true);
    opt->addOpt("seq", seq);
    opt->addOpt("processes", process);
    GURLS G;
    string jobId0("one");
    string jobId1("two");
    // run gurls for training
    G.run(Xtr, ytr, *opt, jobId0);
    // run gurls for testing
    G.run(Xte, yte, *opt, jobId1);
catch (gException& e)
   cout << e.getMessage() << endl;</pre>
   return EXIT_FAILURE;
```

```
return EXIT_SUCCESS;
}
```

In order to run the other examples you just have to substitute the code fragment for the task pipeline

```
*seq << "paramsel:loocvprimal" << "optimizer:rlsprimal";
  *seq << "pred:primal" << "perf:macroavg" << "perf:precrec";

and for the sequence of instructions

*process1 << GURLS::computeNsave << GURLS::computeNsave;
  *process1 << GURLS::ignore << GURLS::ignore << GURLS::ignore;
process->addOpt("one", process1);

and

*process2 << GURLS::load << GURLS::load << GURLS::computeNsave;
  *process2 << GURLS::computeNsave << GURLS::computeNsave;
process->addOpt("two", process2);
```

with the desired task pipeline and instructions sequence. For example, for the case 'Gaussian Kernel, dual case, hold-out cv' the code for defining the task pipeline must be

```
*seq << "split:ho"<<"paramsel:siglamho" <<"kernel:rbf";
*seq<< "optimizer:rlsdual" << "pred:dual" << "predkernel:traintest";
*seq <<"perf:macroavg";</pre>
```

the code fragment specifying the sequence of instructions for the training process must be

```
*process1 << GURLS::computeNsave << GURLS::computeNsave;

*process1 << GURLS::computeNsave << GURLS::ignore;

*process1 << GURLS::ignore << GURLS::ignore;
```

and the code fragment specifying the sequence of instructions for the testing process must be

```
*process2 << GURLS::load << GURLS::load << GURLS::load << GURLS::load;
*process2 << GURLS:: computeNsave << GURLS:: computeNsave;
*process2 << GURLS:: computeNsave;
```

2.6 Normalization functions

The norm set of functions allow to normalize the data. This is a preprocessing step, therefore it has not implemented as a GURLS task, and has to be called explicitly before running the pipeline. There are two possible ways to call these functions, that we describe in the following. In the first example we separately normalize train and test data.

```
[Xtr] = norm_12(Xtr,ytr,opt);
[Xte] = norm_12(Xte,yte,opt);
```

In the following example the training set is first normalized and the column-wise means and covariances are saved to file. Then the test data are normalized according to the stats computed with the training set.

```
[Xtr] = norm_zscore(Xtr, ytr, opt);
[Xte] = norm_testzscore(Xte, yte, opt);
```

In GURLS++ normalization is implemented through the classes Norm, NormZScore and NormTestZScore. We refer to the doxygen documentation of each class for further reference.

2.7 Results visualization (only for GURLS)

You can visualize the results of one or more GURLS pipelines using the summary_* functions. Below we show the usage of these set of functions for two sets of experiments (i.e. GURLS pipelines) each one run 5 times.

First we have to run the experiments. nRuns contains the number of runs for each experiment, and filestr contains the names of the experiments.

```
nRuns = \{5, 5\};
filestr = {'hoprimal'; 'hodual'};
for i = 1:nRuns\{1\};
  opt = defopt(filestr{1} '_' num2str(i)];
  opt.seq = {'split:ho','paramsel:hoprimal','rls:primal',...
   'pred:primal','perf:macroavg','perf:precrec'};
  opt.process\{1\} = [2,2,2,0,0,0];
  opt.process\{2\} = [3,3,3,2,2,2];
  gurls (Xtr, ytr, opt, 1)
  gurls (Xte, yte, opt, 2)
end
for i = 1:nRuns\{2\};
  opt = defopt(filestr{2} '_' num2str(i)];
  opt.seq = {'split:ho', 'kernel:linear', 'paramsel:hodual', ...
  'rls:dual', 'pred:dual', 'perf:macroavg', 'perf:precrec'};
  opt.process\{1\} = [2,2,2,2,0,0,0];
  opt.process\{2\} = [3,3,3,3,2,2,2];
  gurls (Xtr, ytr, opt, 1)
  gurls (Xte, yte, opt, 2)
end
```

In order to visualize the results we have to specify in fields which fields of opt are to be displayed (as many plots as the elements of fields will be generated)

```
>> fields = {'perf.ap','perf.acc'};
we can generate "per-class" plots with the following command:
>> summary_plot (filestr, fields, nRuns)
and "global" plots with:
>> summary_overall_plot (filestr, fields, nRuns)
this generates "global" table:
>> summary_table (filestr, fields, nRuns)
This plots times taken by each step of the pipeline for performance reference:
>> plot_times (filestr, nRuns)
```

2.8 Learning from large datasets

Two modules in Gurls have been specifically designed to deal with the so-called *big learning* scenario. We consider to be big those data that cannot fully reside in RAM without any memory mapping techniques – such as swapping. Conversely data that can fully reside in RAM are considered to be small/medium. Learning with small/medium data can be carried out via Gurls or Gurls⁺⁺. Learning with big data can be carried out with the dedicate modules BGurls or BGurls⁺⁺, under the conditions described in the following. Without the ambition to develop a good solution for all the infinte possible variants of big learning, we decided to focus specifically on those situations where one seeks a linear model on a large set of (possibly non linear) features. A more accurate specification of what "large" means in Gurls is directly related to the number d of features: we require it must be possible to store a $d \times d$ matrix in memory. In practice, this roughly means we can train models with up-to 25k features on machines with 8Gb of RAM, and up-to 50k features on machines with 36Gb of RAM. It is important to remark we do not require the data matrix itself to be stored in memory. Indeed, in BGURLS it is possible to manage an arbitrarily large set of training examples.

Both BGURLS and BGURLS⁺⁺ include all the design patterns described for GURLS, and have been complemented with additional big data and distributed computation capabilities. Big data support is obtained using a data structure called *bigarray*, which allows to handle data matrices as large as a machine's available space on hard drive instead of its RAM: we store the entire dataset on disk and load only small chunks in memory when required. Due to programming language constraints, there are some differences between the Matlab and C⁺⁺implementations. In Figure 2.8 we depicted the different scenarios where the different packages can be applied.

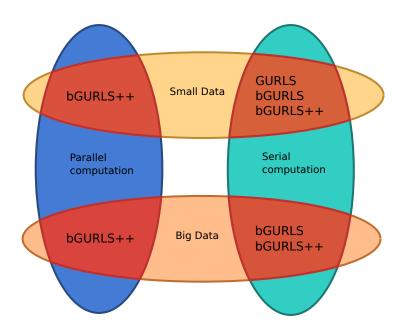


Figure 2.2: GURLS scenarios.

2.8.1 BGURLS

BGURLS relies on a simple interface – developed ad-hoc and called *Gurls Distributed Manager* (GDM) – to distribute matrix-matrix multiplications, thus allowing users to perform the important task of kernel matrix computation on a distributed network of computing nodes. After this step, the subsequent tasks behave as in GURLS (cfr. Fig. 2.3).

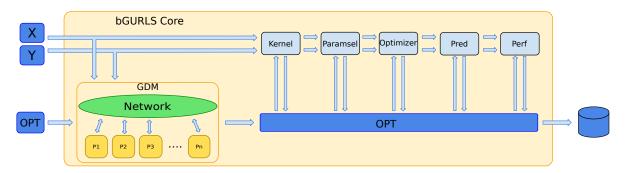


Figure 2.3: BGURLS design.

The BGURLS Core is identified with the bgurs1 command, which behaves as gurls. As gurls it accepts exactly four arguments:

- 1. the bigarray of the input data.
- 2. the bigarray of the labels vector.
- 3. An options' structure.
- 4. A job-id number.

The options' structure is built through the bigdefopt function with default fields and values. Most of the main fields in the options' structure are the same as in GURLS, however bgurls requires the options' structure to have the additional field files, which must be a structure with fields:

- Xva_filename: the prefix of the files that constitute the bigarray of the input data used for validation
- yva_filename: the prefix of the files that constitute the bigarray of the labels vector used for validation
- pred_filename: the prefix of the files that constitute the bigarray of the predicted labels for the test set
- XtX_filename: the name of the files where pre-computed matrix X'X is stored
- ullet Xty_filename: the name of the files where pre-computed matrix Xt'y is stored
- XvatXva_filename: the name of the files where pre-computed matrix $X_{va}'X_{va}$ is stored
- Xvatyva_filename: the name of the files where pre-computed matrix $X'_{va}y_{va}$ is stored

BGURLS example

Let us consider the demo bigdemoA.m in the demo directory to better understand the usage of BGURLS. The demo computes a linear classifier with the regularization parameter chosen via hold-out validation, and then evaluate the prediction accuracy on a test set. The data set used in the demo is the bio data set used in [26], which is saved in the demo directory as a .zip file, 'bio_unique.zip', containing two files:

- 'X.csv': containing the input $n \times d$ data matrix, where n is the number of samples (24,942) and d is the number of variables (68)
- 'Y.csv': containing the input $n \times 1$ label vector

Note that the bio data is not properly a big data set, as it could reside in memory, however it is large enough to make it reasonable to use BGURLS.

In the following we examine the salient part of the demo in details. First unzip the data file

```
unzip('bio_unique.zip','bio_unique')
and set the name of the data files
filenameX = 'bio_unique/X.csv'; %nxd input data matrix
filenameY = 'bio_unique/y.csv'; %nxl or 1xn labels vector
```

Now set the size of the blocks for the bigarrays (matrices of size blocksize× d must fit into memory):

```
blocksize = 1000;
```

the fraction of total samples to be used for testing:

```
test_hoproportion = .2;
```

the fraction of training samples to be used for validation:

```
va_hoproportion = .2;
```

and the directory where all processed data is going to be stored:

```
dpath = 'bio_data_processed';
```

Now set the prefix of the files that will constitute the bigarrays

```
mkdir(dpath)
files.Xtrain_filename = fullfile(dpath, 'bigarrays/Xtrain');
files.ytrain_filename = fullfile(dpath, 'bigarrays/ytrain');
files.Xtest_filename = fullfile(dpath, 'bigarrays/Xtest');
files.ytest_filename = fullfile(dpath, 'bigarrays/ytes');
files.Xva_filename = fullfile(dpath, 'bigarrays/Xva');
files.yva_filename = fullfile(dpath, 'bigarrays/yva');
```

and the name of the files where pre-computed matrices will be stored

```
files.XtX_filename = fullfile(dpath, 'XtX.mat');
files.Xty_filename = fullfile(dpath, 'Xty.mat');
files.XvatXva_filename = fullfile(dpath, 'XvatXva.mat');
files.Xvatyva_filename = fullfile(dpath, 'Xvatyva.mat');
```

We are now ready to prepare the data for BGURLS. The following line of command reads files filenameX and filenameY blockwise – thus avoiding to load all file at the same time—and stores them in the bigarray format, after having split the data into train, validation and test set

```
bigTrainTestPrepare(filenameX, filenameY, files, blocksize,...
va_hoproportion, test_hoproportion)
```

Bigarrays are now stored in the file names specified in the structure files. We can now precompute matrices that will be recursively used in the training phase, and store them in the file names specified in the structure files

```
bigMatricesBuild(files)
```

The data set is now prepared for running the learning pipeline with the bgurls command. This phase behaves almost completely as in GURLS. The only differences are that:

• we need not to load the data into memory, but simply "load" the bigarray, that is load the information necessary to access the data blockwise.

• we have to specify in the opt structure the path where the already computed matrix multiplications, and bigarrays for validation data are stored.

Let us first define the option structure as in GURLS

```
name = fullfile(wpath,'gurls');
opt = bigdefopt(name);
opt.seq = {'paramsel:dhoprimal','rls:dprimal','pred:primal','perf:macroavg'};
opt.process{1} = [2,2,0,0];
opt.process{2} = [3,3,2,2];
```

Note that no task is defined for the split category, as data has already been split in the preprocessing phase and bigarrays for validation were built. In the following fragment of code we add to the options' structure the information relative to the already computed matrix multiplications and to the validation bigarrays

```
opt.files = files;
opt.files = rmfield(opt.files, {'Xtrain_filename';'ytrain_filename';...
'Xtest_filename';'ytest_filename'}); %not used by bgurls
opt.files.pred_filename = fullfile(dpath, 'bigarrays/pred');
```

Note that we have also defined where the predicted labels shall be stored as bigarray.

Now we have to "load" bigarrays for training

```
X = bigarray.Obj(files.Xtrain_filename);
y = bigarray.Obj(files.ytrain_filename);
X.Transpose(true);
y.Transpose(true);
and run bgurls on the training set
bgurls(X,y,opt,1)
```

In order to run the testing process, we first have to "load" bigarrays variables for test data

```
X = bigarray.Obj(files.Xtest_filename);
y = bigarray.Obj(files.ytest_filename);
X.Transpose(true);
y.Transpose(true);
```

and then we can finally run bgurls on the test set

```
bgurls(X,y,opt,2);
```

Now you should have a mat file named gurls.mat in your path. This file contains all the information about your experiment. If you want to see the mean accuracy, for example, load the file in your workspace and type

```
>> mean(opt.perf.acc)
```

If you are interested in visualizing or printing stats and facts about your experiment, check the documentation about the summarizing functions in the gurls package.

Dealing with other data formats

Other two demos can be found in the 'demo' directory. The three demos differ in the format of the input data, as we tried to provide examples for the most common data formats. The data set used in bigdemoB is again the bio data set, though in a slightly different format as it is already split into train and test data. The bigTrainPrepare and bigTestPrepare take care of preparing the train and test set separately.

The data set used in <code>bigdemoC</code> is the ImageNet data set, which is automatically downloaded from <code>http://bratwurst.mit.edu/sbow.tar</code>, when running the demo. This data set is stored in 1000 .mat files where the i-th file contains the variable <code>x</code> which is a $d \times n_i$ input data matrix for the n_i samples of class i. The <code>bigTrainTestPrepare_manyfiles</code> takes care of preparing the bigarrays for the ImageNet data format. Note that, while the bio data is not properly a big data set, the ImageNet occupies about 1G of RAM and can thus be called a big data set.

In order to run BGURLS on other data formats, one can simply use bigdemoA after having substituted the line

```
bigTrainTestPrepare(filenameX, filenameY, files, blocksize,...
va hoproportion, test hoproportion)
```

with a suitable fragment of code. The remainder of the data preparation, that is the computation and storage of the relevant matrices, can be left unchanged.

2.8.2 BGURLS⁺⁺

BGURLS⁺⁺ (currently in active development) offers more interesting features because it is based on the MPI libraries. Therefore, it allows for a full distribution within every single task of the pipeline. All the processes read the input data from a shared filesystem over the network and then start executing the same pipeline. During execution, each process' task communicates with the corresponding ones running over the other processes. Every process maintains his local copy of the options. Once the same task is completed by all processes, the local copies of the options are synchronized. This advanced architecture, which is shown in Fig. 2.4, allows for the creation of hybrid pipelines comprising serial one-process-based tasks from Gurls⁺⁺.

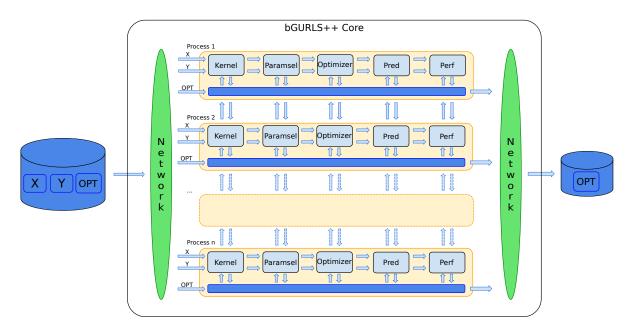


Figure 2.4: BGURLS⁺⁺ design.

CHAPTER 3

MATLAB DEVELOPER'S GUIDE

3.1 Package Organization

The GURLS toolbox contains two user functions gurls and defopt, and a number of supporting functions and additional functionalities which the developer needs to know about. These functions can be divided as:

task functions tasks are the elements of the learning pipeline, for each task several choices are available (see Table 2.1).

utility functions functions called by the task functions.

quickanddirty functions pair of simplified calls of a train-test GURLS pipeline.

normalization functions set of functions for normalizing the data.

summary functions set of functions that help in visualizing the results.

3.2 The gurls function

The gurls function

```
function [opt] = gurls (X, y, opt, jobid)
```

is, beyond defopt, the only function the user would directly call. It executes an ordered sequence of tasks. For each task several choices are available (see Table 2.1). We recall that the choice for each task has to be specified in the field seq of the input options' structure as

```
{<TASK1>:<TASK1_CHOICE>'; <TASK2>:<TASK2_CHOICE>';...}
```

Within the gurls function, each task is executed by calling the function corresponding to the task choice specified in the options' structure as {'<TASK1>:<TASK1_CHOICE>';...}. After the gurls function has executed the task, the returned variable is stored in the field of the options' structure named after the task. After all tasks have been executed, it removes the fields of options'structure that must not be saved, as specified in the option process of the input options'structure.

3.3 Gurls tasks

The gurls command executes an ordered sequence of tasks, specified in the option seq of the input options' structure. The available tasks and task choices are listed in Table 2.1. Each task choice is implemented as a function <TASK>_<TASK_CHOICE>.m, e.g. paramsel_hoprimal.m. The functions that implement different choices of the same task are all saved in the same directory, named after the task (e.g. directory perf contains the files perf_macroavg, perf_precrec, and perf_rmse) and containing also the tasks' utility functions.

All task functions have the same input-outpt structure as they take three inputs:

X: input data matrix

y: labels matrix

OPT: options' structire

and return only one output.

3.3.1 Description of the available tasks choices

split Splits data into traing and validation sets

splits data into one pair of training and validation sets

ho Splits data into one (default) or more pairs of training and validation sets

paramsel Performs parameter selection

fixlambda Sets the regularization parameter to the value set in OPT

loocvprimal Performs parameter selection when the primal formulation of RLS is used. The leave-one-out approach is used.

loocvdual Performs parameter selection when the dual formulation of RLS is used. The leave-one-out approach is used.

hoprimal Performs parameter selection when the primal formulation of RLS is used. The hold-out approach is used.

hodual Performs parameter selection when the dual formulation of RLS is used. The hold-out approach is used.

siglam Performs parameter selection when the dual formulation of RLS is used. The leave-one-out approach is used. It selects both the regularization parameter lambda and the kernel parameter sigma (requires the stats toolbox).

siglamho Performs parameter selection when the dual formulation of RLS is used (requires the stats toolbox). The hold-out approach is used. It selects both the regularization parameter lambda and the kernel parameter sigma.

bfprimal Performs parameter selection when the primal formulation of RLS is used. The hold-out approach is used in a brute force way, i.e. the RLS problem is solved from scratch for each value of the regularizer.

bfdual Performs parameter selection when the dual formulation of RLS is used. The hold-out approach is used in a brute force way, i.e. the RLS problem is solved from scratch for each value of the regularizer.

calibratesgd Performs parameter selection when one wants to solve the problem using pegasos as rls task.

kernel Computes the symmetric Kernel matrix

linear Computes the Kernel matrix for a linear model.

rbf Computes the kernel matrix for a Gaussian kernel.

chisquared Computes the Kernel matrix for chi-squared kernel.

load Loads the kernel matrix from disk.

rls Solves RLS optimization problem

primal Computes a classifier for the primal formulation of RLS.

dual Computes a classifier for the dual formulation of RLS.

auto Computes a RLS classifier, with automatic selection of primal/dual procedure.

pegasos Computes a classifier for the primal formulation of RLS. The optimization is carried out using a stochastic gradient descent algorithm.

predkernel Computes the Kernel matrix for prediction

traintest Computes the kernel matrix between the training points and the test points.

pred Predicts the labels

primal Computes the predictions of the linear classifier stored computed with the primal formulation of RLS, on the samples passed in the X matrix.

dual Computes the predictions of the classifier computed with the dual formulation of RLS, on the samples passed in the X matrix.

perf Assesses prediction performance

macroavg Computes the average classification accuracy per class.

precrec Computes the average precision per class

rmse Computes the root mean squared error for the predictions, taken as the Frobenius norm of the distance matrix between the predicted labels specified in the field pred of opt and the true labels y

conf Computes a confidence for the highest scoring class

- **maxscore** Computes a confidence estimation for the predicted class (i.e. highest scoring class). The highest score is considered
- **gap** Computes a confidence estimation for the predicted class (i.e. highest scoring class). The difference between the highest scoring class and the second highest scoring class is considered.
- **boltzman** Computes the probability of belonging to the highest scoring class. The scores are converted in probabilities using the Boltzman distribution.
- **boltzmangap** Computes a confidence estimation for the predicted class (i.e. highest scoring class). The scores are converted in probabilities using the Boltzman distribution and the difference between the highest scoring class and the second highest scoring class is used as an estimate.

3.4 defopt function

The defopt function:

```
function opt = defopt(expname)
```

builds a defualt options' structure. The options' structure, given in input to gurls, and passed to the task functions, contains all the information relative to the learning pipeline and to the tasks of the pipeline that have already been executed. The defopt function assignes default values to the following fields (in parenthesis the default values):

Experiment options:

- name (expname): experiment identifier.
- savefile (expname.mat) name of the file where results will be saved.

Data options:

- nholdouts (1): number of data splits to be used for hold-out cross validation.
- hoproportion (0.2): proportion between training and validation set in parameter selection.
- nlambda (100): number of values for the regularization parameter.

• nsigma (25): number of values for the kernel parameter.

General algorithm options:

- kernel (structure with field type set to 'rbf'): kernel for dual formulation.
- singlelambda (function @mean): function for obtaining one value for the regularization parameter, given the selected parameter value for each class in multiclass classification (for each output in multiple output regression).
- smallnumber (1e-8): sets the lower limit for the values of the regularization parameter.
- hoperf (function @perf_macroavg): objective function to be used for parameter selection.

Pegasos options:

- epochs (4): number of passes over the training set for stocastic gradient descent.
- subsize (50): training set size used for parameter selection when using stocastic gradient descent.
- calibfile ('foo'): name of the file used by paramsel_calibratesgd to save temporary results in parameter selection for pegasos.

Version info:

- version (1.0): GURLS version.

The options' structure saved by gurls contains both the above default values and some additional fields: the field times, where computing times for each task are saved, and the fields corresponding to the tasks which corresponding instruction code has been set to 2 (=CSV), in at least one job.

3.5 Other supporting functions

In addition to the two user functions gurls and defopt and the tasks functions, the GURLS toolbox comprises a number of supporting functions.

3.5.1 Installation functions

gurls_install Adds all the important directories to your path.

gurls_root Returns the directory where the calling M-files is saved

3.5.2 Tasks utility functions

GInverseDiagonal Utility function for the loocvdual choice of paramsel task.

rls_eigen Returns the RLS optimizer given the data singular value decomposition. It is called by the paramsel and rls tasks.

precrec_driver Utility function for the precrec choice of the perf task.

distance Computes the Euclidean squared distance matrix. It is used to compute the kernel in the paramesel, kernel and predkernel tasks.

paramsel_lambdaguesses Returns a geometric series of values for the regularization parameter. It is a utility function for the paramsel task.

tygert_svd Computes randomized singular value decomposition. It is called by the primalr and dualr options for both paramesel and rls tasks.

rls_pegasos_driver Utility function for the pegasos choice of rls task. Computes a single pass for pegasos algorithm, performing the stochastic gradient descent over all training samples once.

rls_primal_driver Utility function for the primal choice of rls task.

3.5.3 enums functions

ign Returns the instruction code for 'IGNORE' in a GURLS process sequence

cpt Returns the instruction code for 'COMPUTE' in a GURLS process sequence

csv Returns the instruction code for 'COMPUTE AND SAVE' in a GURLS process sequence

ldf Returns the instruction code for 'LOAD FROM FILE' in a GURLS process sequence

del Returns the instruction code for 'EXPLICITLY DELETE' in a GURLS process sequence

3.6 Designing and Implementing a new functionality

Thanks to its great modularity you can extend the GURLS package by adding new choices for the already available tasks. You can add a new task choice, say <NEWTASKCHOICE>, for task <TASK>, by implementing the function <TASK>_<NEWTASKCHOICE>.m (to be saved in the <TASK> folder) with the following structure

```
function [out] = <TASK>_<NEWTASKCHOICE>(X, y, opt)
\%<TASK>_<NEWTASKCHOICE>(X,Y,OPT)
\%Computes ....
\%INPUTS:
\%-X: input data matrix
```

```
\%-y: labels matrix
\%-OPT: structure of options with the following fields (and subfields):
\ 응
      fields that need to be set through previous gurls tasks:
\ 응
       - ... (set by the ...* routine)
\ 응
      fields with default values set through the defopt function:
\ 응
       - ...
\ 응
     For more information on standard OPT fields
\ 응
see also defopt
\ 응
\% OUTPUT: ...
\% new code
\% ...
\% ...
end
```

Note that in the above scheme, all the information relative to a field <TASK> previously saved in the input OPT is lost. In order to maintain such information – as in the perf_* routines – the old OPT field must be copied in a new struct, which can then be partially modified by adding or substituting some of its fields.

CHAPTER 4

C++ DEVELOPER'S GUIDE

4.1 Package Organization

The GURLS++ toolbox comprises two main classes, GURLS and GurlsOptionsList, and a number of supporting classes and additional functionalities which the developer needs to know about. These functions can be divided as:

task classes tasks are the elements of the learning pipeline, for each task several subclasses are available (see Table 2.1).

utilities functions called by the task classes.

quickanddirty classes pair of simplified calls of a train-test GURLS pipeline.

normalization classes set of classes for normalizing the data.

In the following we describe the user's classes GURLS and GurlsOptionList and the set of tasks classes. For all other classes we refer to the doxygen documentation.

4.2 The GURLS class

The GURLS class has only one method, run, which executes an ordered sequence of tasks. For each task several choices are available (see Table 2.1). We recall that the choice for each task has to be specified in the field seq of the input options' structure, say opt, as

```
OptTaskSequence *seq = new OptTaskSequence();
seq->addTask("<CATEGORY1>:<TASK1>");
...
seq->addTask("<CATEGORYn>:<TASKn>");
opt->addOpt("seq", &seq);
```

4. C++ developer's Guide 4.3. Gurls tasks

The run method executes each task of the sequence. After all tasks have been executed, it removes the fields of the options'structure corresponding to tasks that must not be saved, as specified in the option process of the input options'structure.

4.3 Gurls tasks

The run method of the GURLS class executes an ordered sequence of tasks. For the list of possible task choices we refer to the Matlab developer's guide (precisely Section 3.3) Each task is implemented as a class, with its sub-classes being listed in Table 4.1 and with the only difference that classes and subclasses in C++ are defined in Camel Case.

All the task classes have the same input-outpt structure as they take three inputs:

X: input data matrix

y: labels matrix

OPT: options' structire

and have only one method, namely execute, that returns a GurlsOptionList.

task	Class	subclasses	
split	Split	Но	
paramsel	ParamSelection	LoocvDual	LoocvPrimal
		HoDual	HoPrimal
		SiglamHo	Siglam
		FixLambda	CalibrateSGD
		BfDual	BfPrimal
		HoPrimalr	HoDualr
kernel	Kernel	ChisquaredKernel	LinearKernel
		RBFKernel	
rls	Optimizer	RLSPrimal	RLSDual
		RLSAuto	RLSPegasos
		RLSPrimalr	RLSDualr
predkernel	PredKernel	TrainTest	
pred	Prediction	PredPrimal	PredDual
perf	Performance	MacroAvg	PrecisionRecall
		Rmse	
conf	Confidence	ConfMaxScore	ConfGap
		ConfBoltzmanGap	ConfBoltzman

Table 4.1: List of GURLS++ task classes and subclasses.

4.4 The GurlsOptionList class

The options' structure given in input to the GURLS class, and passed to the task functions, contains all the information relative to the learning pipeline and to the tasks of the pipeline that have already been executed. All options must be of one of the following OptTypes:

- OptNumber
- OptNumberList
- OptList
- OptString
- OptStringList
- OptMatrix
- OptFunction
- OptTaskSequence
- OptProcess

The GurlsOptionList class builds a default options' structure assigning default values to the following fields (in parenthesis the default values):

Experiment options:

- name (OptString (ExpName) where ExpName is the string given in input to GurlsOptionList): experiment identifier.
- savefile (OptString (ExpName.txt): name of the file where results will be saved.

Data options:

- nholdouts (OptNumber (1)): number of data splits to be used for hold-out cross validation
- hoproportion (OptNumber (0.2)): proportion between training and validation set in parameter selection.
- nlambda (OptNumber (100)): number of values for the regularization parameter.
- nsigma (OptNumber (25)): number of values for the kernel parameter.

General algorithm options:

- singlelambda (OptFunction ("median")): function for obtaining one value for the regularization parameter, given the selected parameter value for each class in multiclass classification (for each output in multiple output regression).
- smallnumber (OptNumber (1e-8)): sets the lower limit for the values of the regularization parameter.
- hoperf (macroavg): objective function to be used for parameter selection.

Pegasos options:

- epochs (OptNumber (4)): number of passes over the training set for stocastic gradient descent.
- subsize (OptNumber (50)): training set size used for parameter selection when using stocastic gradient descent.
- calibfile (OptString("foo")): name of the file used by paramsel_calibratesgd to save temporary results in parameter selection for pegasos.

Version info:

- version (OptString("1.0")): GURLS version.

The options' structure saved by the run method of the GURLS class contains both the above default values and some additional fields: the field times, where computing times for each task are saved, and the fields corresponding to the tasks which corresponding instruction code has been set to 2 (=CSV), in at least one job.

4. C++ developer's Guide 4.5. Testing

4.5 Testing

Testing routines and scripts are available to test wether GURLS and GURLS++ results coincide. This is usefull if you want to modify the existing GURLS++ routines.

4.5.1 Setting the Test directory

Chose a directory where to save the GURLS results, for comparison with GURLS++ results. Let's call this directory <TEST_DIR>. This has to coincide with the variable GURLS_DATA_DIR settable when the Cmake configuring option BUILD_TEST is on. Now add to <TEST_DIR> the files 'Xtr.txt' and 'ytr.txt', that must contain the input and output data respectively.

4.5.2 Generate GURLS results

Launch Matlab and execute the following commands

```
>> datadir = <TEST_DIR>
>> testall
```

This will execute a series of GURLS tasks on the data stored in the <TEST_DIR> directory.

4.5.3 Generate GURLS++ results and perform comparisons

Launch tests in GURLS++ with the following command on Unix

```
$ ./testall
```

and with the following command for Windows

```
$ testall.exe
```

4.6 Designing and Implementing a new functionality

Thanks to its great modularity you can extend the GURLS++ package by adding new tasks for the already available categories. You can add a new task, say <NEWTASK>, for task category <CATEGORY>, by adding the following two lines of code

```
}else if(id == "<NEWTASK>") {
    return new <NEWSUBCLASS><T>;
```

right before the following fragment of code:

```
} else
    throw BadPredictionCreation(id);
```

in the definition of the the class, say <CLASS>, corresponding to <CATEGORY>, and by creating the subclass <NEWSUBCLASS> of <CLASS>. The new subclass must be defined in the following way:

```
#ifndef _GURLS_<NEWSUBCLASSFILE>_H_
#define _GURLS_<NEWSUBCLASSFILE>_H_
#include <cstdio>
#include <cstring>
#include <iostream>
#include <cmath>
#include <algorithm>
#include <set>
#include "options.h"
#include "optlist.h"
#include "gmat2d.h"
#include "gvec.h"
#include "gmath.h"
// HERE INCLUDE THE HEADER WHERE THE TASK CLASS IS DEFINED
#include // other required classes
namespace gurls {
/**
   \star \brief <NEWSUBCLASS> is the subclass of <CLASS> that implements ...
   */
template <typename T>
class <NEWSUBCLASS>: public <CLASS><T>{
public:
    /**
     * \param X input data matrix
     * \param Y labels matrix
     * \param opt options with the following:
       - ...
     * \return ret a GurlsOptionsList with the following fields:
     * - ...
     */
    void execute(const gMat2D<T>& X, const gMat2D<T>& Y,
        GurlsOptionsList& opt);
};
template <typename T>
GurlsOptionsList* <NEWSUBCLASS><T>::execute(const gMat2D<T>& X,
     const gMat2D<T>& /*Y*/, const GurlsOptionsList &/*opt*/) throw(gException)
```

```
{
GurlsOptionsList* ret = new GurlsOptionsList("<CLASS>");

/*
  new code here
  ...
  */
return ret
}
}
#endif // _{\sc Gurls}_<NEWSUBCLASSFILE>_H_
```

Note that in the above scheme, all the information relative to a field <CLASS> previously saved in the input opt is lost. In order to maintain such information – as in the Performance class – the old OPT field must be copied in a new GurksOptionList, which can then be partially modified by adding or substituting some of its fields.

CHAPTER 5

EXPERIMENTS

We focus our experimental analysis on the assessment of GURLS' performance both in terms of accuracy and time. Indeed, we believe it is fair to question whether or not a least square algorithm – classically thought of as an approach to regression problems – can perform well in a classification setting. From a theoretical point of view, the use of a least squares estimator is justified since it provides a plug-in estimator: i.e. least squares estimate conditional probabilities that can be used for classification. From an empirical point of view, there is evidence in the literature that a least squares estimator can perform remarkably well in a variety of tasks.

In our experiments we considered 5 popular data sets, briefly described in Table5.1(a). We set up different pipelines with different optimization routines available in Gurls, and compared the performance to SVM, for which we used the python modular interface to LIBSVM [7]. Automatic selection of the optimal regularization parameter is implemented identically in all experiments: (i) split the data; (3) define a set of regularization parameter on a regular grid; (3) perform hold-out validation. The variance of the Gaussian kernel has been fixed by looking at the statistics of the pairwise distances among training examples. The prediction accuracy of Gurls and Gurls⁺⁺ is identical – as expected – but the latter module is significantly faster. The prediction accuracy of standard RLS-based methods is in many cases higher than SVM. However the computing performance seems to favor SVM. By exploiting the wide range of op-

	# of	# of	# of
data set	samples	classes	variables
optdigit	3800	10	64
landast	4400	6	36
pendigit	7400	10	16
letter	10000	26	16
isolet	6200	26	600

Table 5.1: Data sets description

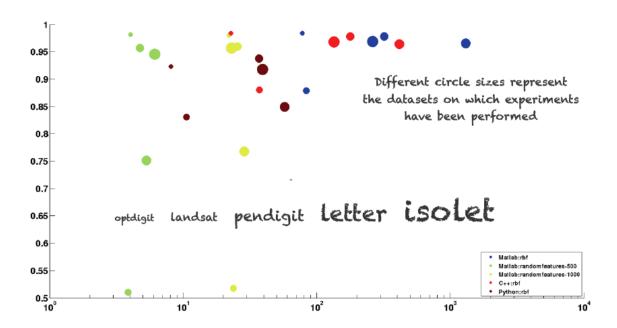


Figure 5.1: Experiments.

timization procedures handled in our library, we further run the experiments with the random features approximation [35] implemented in GURLS. As show in Figure 5(b), with a relatively small number of random features namely 500, the performance of such method is comparable to that of SVM at much lower computational cost in the majority of the tested data sets.

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