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\\\\frac { 1 } { n }$$成立;(Ⅱ)设$$a \_ { n } = 1 + \\\\frac { 1 } { 2 } + \\\\cdots + \\\\frac { 1 } { n } - \\\\ln n \\\\left( n = 1 , 2 , \\\\right.$$…),证明数列$$\\\\left\\\\{ a \_ { n } \\\\right\\\\}$$收敛","pos\_list":[[{"x":140,"y":687},{"x":1319,"y":684},{"x":1320,"y":870},{"x":141,"y":872}]],"content\_list":[{"type":1,"prob":96,"string":"(I)证明:对任意的正整数","option":"","pos":[{"x":142,"y":702},{"x":591,"y":702},{"x":591,"y":752},{"x":142,"y":752}]},{"type":1,"prob":98,"string":"n","option":"","pos":[{"x":591,"y":718},{"x":605,"y":718},{"x":605,"y":741},{"x":591,"y":741}]},{"type":1,"prob":99,"string":",都有","option":"","pos":[{"x":606,"y":702},{"x":695,"y":702},{"x":695,"y":752},{"x":606,"y":752}]},{"type":2,"prob":99,"string":"$$\\\\frac { 1 } { n + 1 } < \\\\ln \\\\left( 1 + \\\\frac { 1 } { n } \\\\right) < \\\\frac { 1 } { n 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