

**WIA2005 Algorithm Design & Analysis**  
**Semester 2, 2016/17**  
**Tutorial 6**

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1. What are the minimum and maximum numbers of elements in a heap of height  $h$ ?
2. Is the array with values [23, 17, 14, 6, 13, 10, 1, 5, 7, 12] a max-heap? What is the  $A.length$  and  $A.heap-size$  for this array?
3. Illustrate the operation of MAX-HEAPIFY on the array  $A = [27, 17, 3, 16, 13, 10, 1, 5, 7, 12, 4, 8, 9, 0]$ .
4. Write pseudocode for the procedure MIN-HEAPIFY( $A, i$ ), which performs the corresponding manipulation on a min-heap.
5. Write an efficient MAX-HEAPIFY that uses an iterative control construct (a loop) instead of recursion.
6. Illustrate the operation of BUILD-MAX-HEAP on the array  $A = [5, 3, 17, 10, 84, 19, 6, 22, 9]$ .
7. Illustrate the operation of HEAPSORT on the array  $A = [5, 13, 2, 25, 7, 17, 20, 8, 4]$ .
8. Illustrate the operation of MAX-HEAP-INSERT( $A, 10$ ) on the heap  $A = [15, 13, 9, 5, 12, 8, 7, 4, 0, 6, 2, 1]$ .