

# Tutorial for Week 6 - Answers

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2. All of the following are solved by the pigeon-hole principle. Therefore the set  $A$  must have a cardinality  $\geq k|B| + 1$  to satisfy the question.

(a)  $A$  is the set of rolls and  $B$  is the set of pairs of numbers:

$$\{(1;1);(2;2);(3;3);(4;4);(5;5);(6;6)\};$$

such that the statement is satisfied.  $|B| = 6$ , therefore  $|A| = |B| + 1 = 7$  rolls.

- (b) Two die can give any combination between 2 and 12. Therefore  $|B| = 11$ . The number of rolls required is  $|A|$ , as  $|A| = |B| + 1$ ,  $|A| = 11 + 1 = 12$  rolls.
- (c) This is similar to the last question but  $k$  is increased from 1 to 2, as there are now three matches required. This gives  $k = n - 1 = 3 - 1 = 2$ . As the number of rolls required is  $|A|$  and  $|A| = k|B| + 1$ ,  $|A| = 2 \times 11 + 1 = 23$ .