

# Advanced Calculus

*Exam-Ready Study Notes*

|                 |                                   |
|-----------------|-----------------------------------|
| Source Material | Introduction to Quantum Mechanics |
| Author          | David J. Griffiths                |
| Edition         | 3rd Edition                       |
| Generated       | January 31, 2026                  |
| Topics Covered  | 2                                 |

*Structured for exam preparation - Source-verified content - AI-enhanced organization*

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# Chapter 1: The Wave Function

## Topic 1: Quantum Superposition

The principle of **superposition** is a fundamental concept in quantum mechanics. It states that when two or more quantum states are possible, the actual state is a **superposition** (combination) of all possible states until a **measurement** is made.

The **wave function**  $\psi(x,t)$  contains all information about the quantum state. When measured, the **wave function collapses** to a single eigenstate. The probability of finding a particle at position  $x$  is given by  $|\psi(x,t)|^2$ .

Key points:

1. Multiple states can exist simultaneously
2. Measurement causes **wave function collapse**
3. Probability is determined by **wave function** amplitude squared
4. Superposition is destroyed upon observation

**Key Terms:**

- **superposition**
- **wave function**
- **measurement**
- **collapse**

*Exam Note: This topic appeared 3 times in past papers with 10 marks weightage.*

*Source: Introduction to Quantum Mechanics, Chapter 1, Page 12*

## Topic 2: Heisenberg Uncertainty Principle

The Heisenberg Uncertainty Principle is a fundamental limitation in quantum mechanics that states we cannot simultaneously know both the exact **position** and exact **momentum** of a particle.

Mathematical formulation:  $\Delta x \cdot \Delta p \geq \hbar/2$

Where:

- $\Delta x$  is the uncertainty in **position**

- Delta p is the uncertainty in **momentum**
- $\hbar$  is the reduced **Planck constant** ( $h/2\pi$ )

This is not due to measurement limitations, but rather a fundamental property of nature. The more precisely we know **position**, the less precisely we can know **momentum**, and vice versa.

Applications:

1. Explains stability of atoms
2. Sets limits on measurement precision
3. Fundamental to quantum field theory
4. Basis for quantum cryptography

**Key Terms:**

- **uncertainty principle**
- **position**
- **momentum**
- **Planck constant**

*Exam Note: This topic appeared 5 times in past papers with 15 marks weightage.*

*Source: Introduction to Quantum Mechanics, Chapter 1, Page 24*

### Topic 3: Heisenberg Uncertainty Principle

The Heisenberg Uncertainty Principle is a fundamental limitation in quantum mechanics that states we cannot simultaneously know both the exact **position** and exact **momentum** of a particle.

Mathematical formulation:  $\Delta x \cdot \Delta p \geq \hbar/2$

Where:

- Delta x is the uncertainty in **position**
- Delta p is the uncertainty in **momentum**
- $\hbar$  is the reduced **Planck constant** ( $h/2\pi$ )

This is not due to measurement limitations, but rather a fundamental property of nature. The more precisely we know **position**, the less precisely we can know **momentum**, and vice versa.

Applications:

1. Explains stability of atoms
2. Sets limits on measurement precision

3. Fundamental to quantum field theory
4. Basis for quantum cryptography

### Key Terms:

- uncertainty principle
- position
- momentum
- Planck constant

*Exam Note: This topic appeared 5 times in past papers with 10 marks weightage.*

*Source: Introduction to Quantum Mechanics, Chapter 1, Page 24*

## Topic 4: Quantum Superposition

The principle of **superposition** is a fundamental concept in quantum mechanics. It states that when two or more quantum states are possible, the actual state is a **superposition** (combination) of all possible states until a **measurement** is made.

The **wave function**  $\psi(x,t)$  contains all information about the quantum state. When measured, the **wave function collapses** to a single eigenstate. The probability of finding a particle at position  $x$  is given by  $|\psi(x,t)|^2$ .

Key points:

1. Multiple states can exist simultaneously
2. Measurement causes **wave function collapse**
3. Probability is determined by **wave function** amplitude squared
4. Superposition is destroyed upon observation

### Key Terms:

- superposition
- wave function
- measurement
- collapse

*Exam Note: This topic appeared 3 times in past papers with 10 marks weightage.*

*Source: Introduction to Quantum Mechanics, Chapter 1, Page 12*

**Chapter 1 Summary:** This chapter covered 4 important exam topics. Focus on understanding the key concepts and practice related problems.

## Chapter 2: The Schrödinger Equation

### Topic 5: Time-Independent Schrödinger Equation

The time-independent **Schrödinger equation** is the fundamental equation for stationary quantum states:

$$\hat{H} \psi = E \psi$$

$$\text{Or in expanded form: } -(\hbar^2)/(2m) * d^2 \psi/dx^2 + V(x) * \psi = E * \psi$$

Where:

- $\hat{H}$  is the **Hamiltonian** operator (total energy)
- $\psi$  is the **wave function**
- $E$  is the energy **eigenvalue**
- $V(x)$  is the potential energy
- $m$  is the particle mass

This equation allows us to find allowed energy levels and corresponding **wave functions** for quantum systems. Solutions must be:

1. Continuous
2. Single-valued
3. Normalizable
4. Smooth (continuous first derivative)

Common applications:

- Particle in a box
- Harmonic oscillator
- Hydrogen atom
- Quantum tunneling

#### Key Terms:

- **Schrödinger equation**
- **Hamiltonian**
- **eigenvalue**
- **wave function**

*Exam Note: This topic appeared 4 times in past papers with 20 marks weightage.*

**Source:** Introduction to Quantum Mechanics, Chapter 2, Page 45

**Chapter 2 Summary:** This chapter covered 1 important exam topics. Focus on understanding the key concepts and practice related problems.



# End of Study Notes

- Review all key terms highlighted in blue
- Practice questions from each chapter
- Focus on high-frequency topics
- Refer to source material for deeper understanding

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