$$\sum_{d|n} \mu(d) = [n == 1]$$

$$\mu(m) = \begin{cases} (-1)^r & m = p_1 p_2 \dots p_r \\ 0 & p^2 | n \end{cases}$$