

Graphs Cheatsheet

Topic Overview

Graphs in Java represent relationships as nodes and edges, used for network and path problems. This cheatsheet covers graph-based techniques.

Prerequisites

Trees

List of Subtopics

- Adjacency Matrix
- Adjacency List
- BFS (Breadth-First Search)
- DFS (Depth-First Search)
- Dijkstra's Algorithm
- Bellman-Ford Algorithm
- Kruskal's Algorithm
- Prim's Algorithm
- Topological Sort
- Detect Cycle

Key Concepts Explained

- **Adjacency Matrix:** 2D array representing edges, space-intensive.
- **Adjacency List:** Array of lists, space-efficient for sparse graphs.
- **Dijkstra's Algorithm:** Finds shortest paths in weighted graphs.

Approaches to Solve Problems with Step-by-Step Algorithms

- **Adjacency Matrix:**
 - **Algorithm:**
 1. Create a $V \times V$ matrix, initialize with infinity.
 2. Set 1 or weight for edges, 0 for no edge.
 3. Access edge with $\text{matrix}[u][v]$.
 - **Context:** $O(V^2)$ space, $O(1)$ edge check.
- **Adjacency List:**
 - **Algorithm:**
 1. Use array of lists, each index for a vertex.
 2. Add edges to the list of the source vertex.
 3. Traverse list for neighbors.
 - **Context:** $O(V+E)$ space, $O(\text{degree})$ edge check.
- **BFS (Breadth-First Search):**
 - **Algorithm:**
 1. Use a queue, enqueue start node.
 2. Dequeue, process, enqueue unvisited neighbors.
 3. Mark visited, repeat until queue is empty.
 - **Context:** $O(V+E)$ time, $O(V)$ space.
- **DFS (Depth-First Search):**
 - **Algorithm:**
 1. Use a stack or recursion, start with root.
 2. Visit node, recurse on unvisited neighbors.
 3. Backtrack when no unvisited neighbors.
 - **Context:** $O(V+E)$ time, $O(V)$ space.
- **Dijkstra's Algorithm:**
 - **Algorithm:**
 1. Use min heap for distances, initialize to infinity.
 2. Start from source, update distances to neighbors.
 3. Repeat until all nodes processed.
 - **Context:** $O((V+E) \log V)$ time, $O(V)$ space.
- **Bellman-Ford Algorithm:**
 - **Algorithm:**

1. Initialize distances to infinity, source to 0.
 2. Relax all edges $V-1$ times.
 3. Check for negative cycles with extra relaxation.
- **Context:** $O(VE)$ time, $O(V)$ space.
- **Kruskal's Algorithm:**
 - **Algorithm:**
 1. Sort edges by weight.
 2. Use union-find to add edges without cycles.
 - **Context:** $O(E \log E)$ time, $O(V)$ space.
 - **Prim's Algorithm:**
 - **Algorithm:**
 1. Use min heap for edges, start with any node.
 2. Add minimum edge to unvisited node, update heap.
 - **Context:** $O((V+E) \log V)$ time, $O(V)$ space.
 - **Topological Sort:**
 - **Algorithm:**
 1. Use DFS, store finish times in a stack.
 2. Pop stack to get topological order.
 - **Context:** $O(V+E)$ time, $O(V)$ space.
 - **Detect Cycle:**
 - **Algorithm:**
 1. Use DFS with visited and recursion stack.
 2. If node in recursion stack, cycle exists.
 - **Context:** $O(V+E)$ time, $O(V)$ space.

Common LeetCode Problems with Approaches

- **Clone Graph (133):** Use DFS or BFS with a map for cloning.
- **Network Delay Time (743):** Use Dijkstra's for shortest paths.
- **Number of Islands (200):** Use DFS or BFS for counting.
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- **Course Schedule (207):** Use topological sort for prerequisites.

Time & Space Complexities

- BFS/DFS: $O(V+E)$
- Dijkstra's: $O((V+E) \log V)$
- Space: $O(V)$ or $O(V+E)$

Important Tips & Tricks

- Use adjacency lists for sparse graphs.
- Optimize Dijkstra's with binary heap.
- Handle disconnected components in DFS/BFS.
- Use union-find for cycle detection in MST.
- Preprocess weights for efficiency.