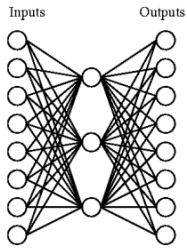


# Artificial Neural Networks (ANNs)

Biologically inspired computational model:

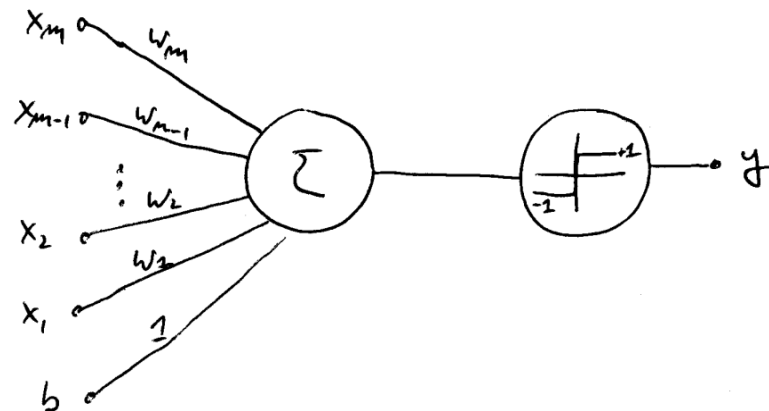
- (1) Simple computational units (neurons).
- (2) Highly interconnected - connectionist view
- (3) Vast parallel computation, consider:
  - Human brain has  $\sim 10^{11}$  neurons
  - Slow computational units, switching time  $\sim 10^{-3}$  sec (compared to the computer  $> 10^{-10}$  sec)
  - Yet, you can recognize a face in  $\sim 10^{-1}$  sec
  - This implies only about 100 sequential, computational neuron steps - this seems too low for something as complicated as recognizing a face
  - Parallel processing



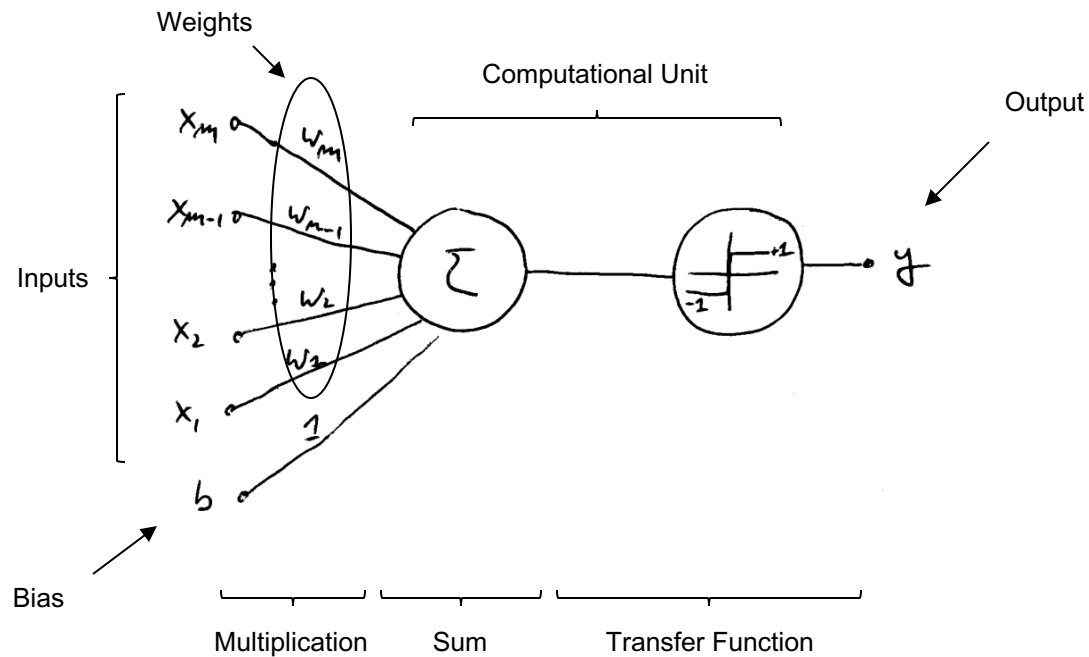
ANNs are naturally parallel - each neuron is a self-contained computational unit that depends only on its inputs.

# The Perceptron

- A simple, single layered neural “network” - only has a single neuron.
- However, even this simple neural network is already powerful enough to perform classification tasks.



# The Architecture



Transfer Function:

$$\text{sgn}(k) = \begin{cases} +1 & \text{if } k \geq 0 \\ -1 & \text{otherwise} \end{cases}$$

Perceptron Computation: 
$$y = \text{sgn}\left(b + \sum_{i=1}^m w_i x_i\right)$$

Note:  $y \in \{+1, -1\}$

Binary Classification

# Computation

A perceptron computes the value,

$$y = \text{sgn}\left(b + \sum_{i=1}^m w_i x_i\right)$$

Ignoring the activation function  $\text{sgn}$  and setting  $m = 1$ , we obtain,

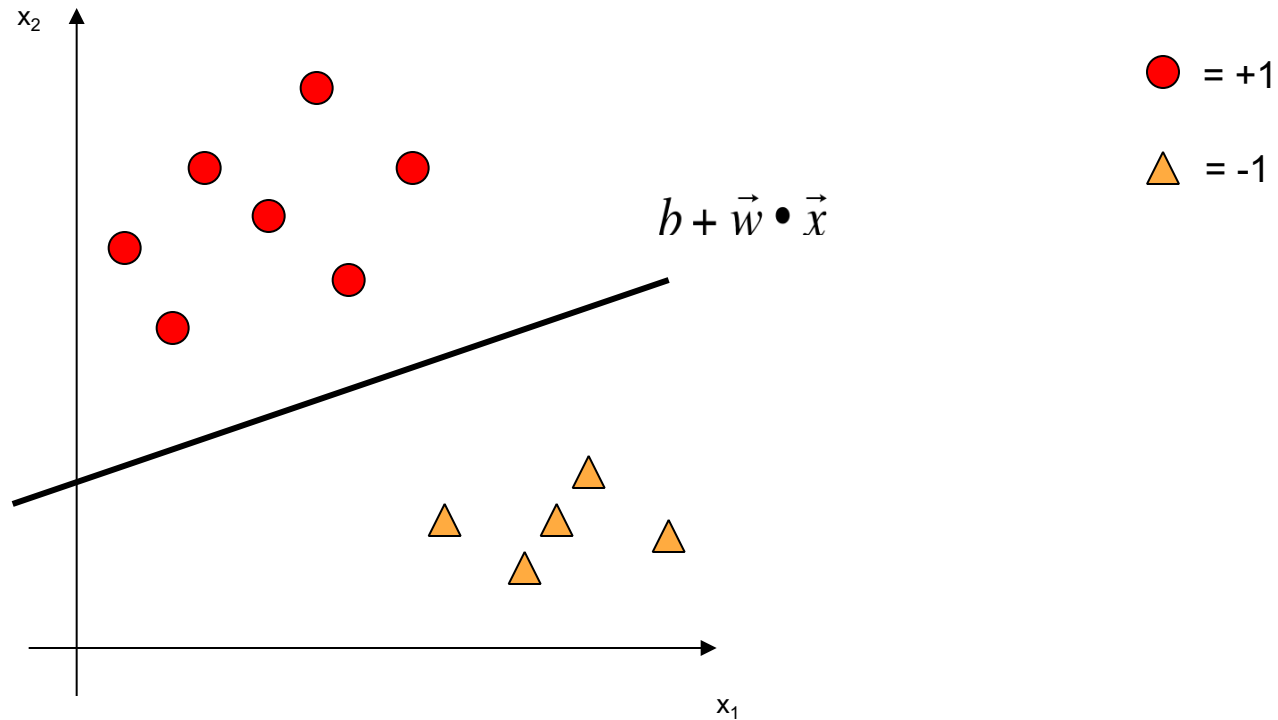
$$y' = b + w_1 x_1$$

But this is the equation of a line with slope  $w$  and offset  $b$ .

Observation: For the general case the perceptron computes a hyperplane in order to accomplish its classification task,

$$y' = b + \sum_{i=1}^m w_i x_i = b + \vec{w} \cdot \vec{x}$$

# Classification



In order for the hyperplane to become a classifier we need to find  $b$  and  $w \Rightarrow$  learning!

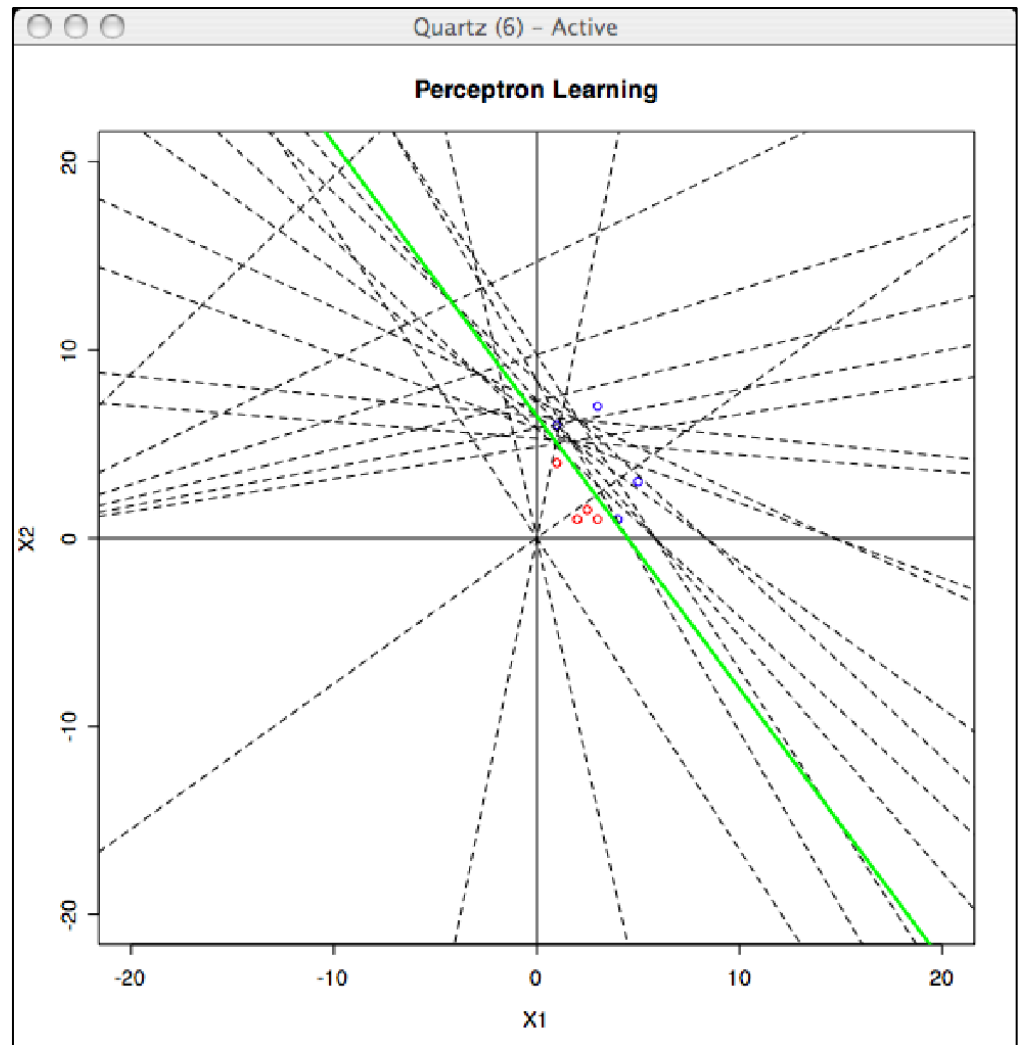
# Learning Algorithm

```
Let  $D = \{(\bar{x}_1, y_1), (\bar{x}_2, y_2), \dots, (\bar{x}_n, y_n)\} \subset H \times \{-1, +1\}$   
 $\bar{w} \leftarrow \bar{0}$   
 $b \leftarrow 0$   
 $R \leftarrow \max_{1 \leq i \leq n} |\bar{x}_i|$   
 $\eta \leftarrow 0 < \eta < 1$   
repeat  
  for  $i = 1$  to  $n$   
    if  $\text{sign}(\bar{w} \bullet \bar{x}_i + b) \neq y_i$  then  
       $\bar{w} \leftarrow \bar{w} + \eta y_i \bar{x}_i$   
       $b \leftarrow b + \eta y_i R^2$   
    end if  
  end for  
until no mistakes made in the for-loop  
return  $(\bar{w}, b)$ 
```

Note: learning is very different here compared to decision trees...here we have many passes over the data until the perceptron converges on a solution.

# Demo

R perceptron demo



# Observations

- The learned information is represented as weights and the bias  $\Rightarrow$  sub-symbolic learning
- In order to apply this learned information we need a neural network structure
- The learned information is not directly accessible to us  $\Rightarrow$  non-transparent model