

→ Sparse coding:

- Similar to vocabulary  $\longleftrightarrow$  doc, represents doc by sparse vectors.

$$\vec{x}_i = \vec{w}^T \vec{z}_i$$

$\downarrow$   
 $d \times 1$

$\downarrow$   
 $d \times d$   
 $\uparrow$   
 dictionary

$\downarrow$   
 $d \times 1$   
 $\longleftarrow$   
sparse vector

- Unsupervised learning can't produce error to be minimized.

One way is to assume a probabilistic model to fit data into, ie: RBM, then use ML to train

Another way is Autoencoder.

- Think about PCA:

Input:  $X$

Prediction:  $Z = W^T X$

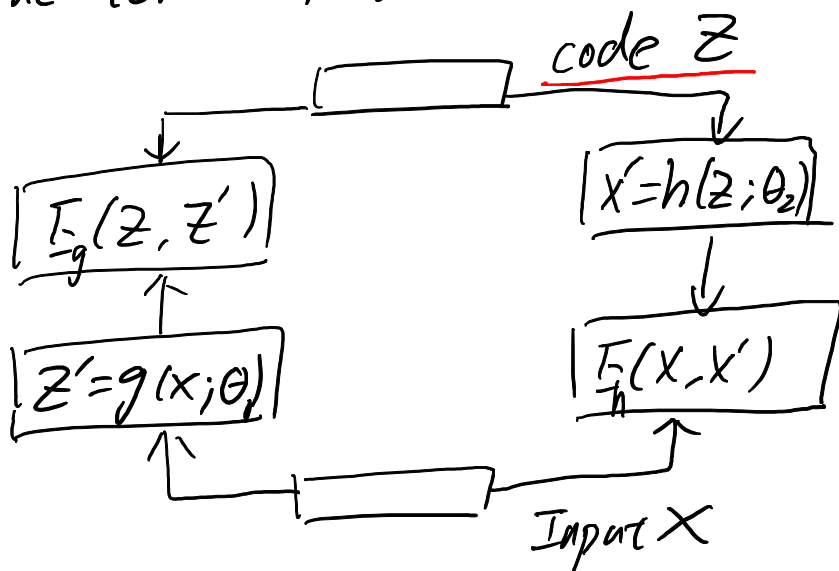
Restore input from  $Z$ :  $X' = WZ$

Error:  $\sum_{i=1}^n \|x_i - WW^T x_i\|^2 \longleftarrow$  Reconstruction error

- Reconstruction of prediction should be either low dimension or in sparse high-dimension
- Other unsupervised: EM

→ Auto encoder

- Bottleneck vs overcomplete code.
- One common arch



$$\theta_1 = \vec{c}, b_c$$

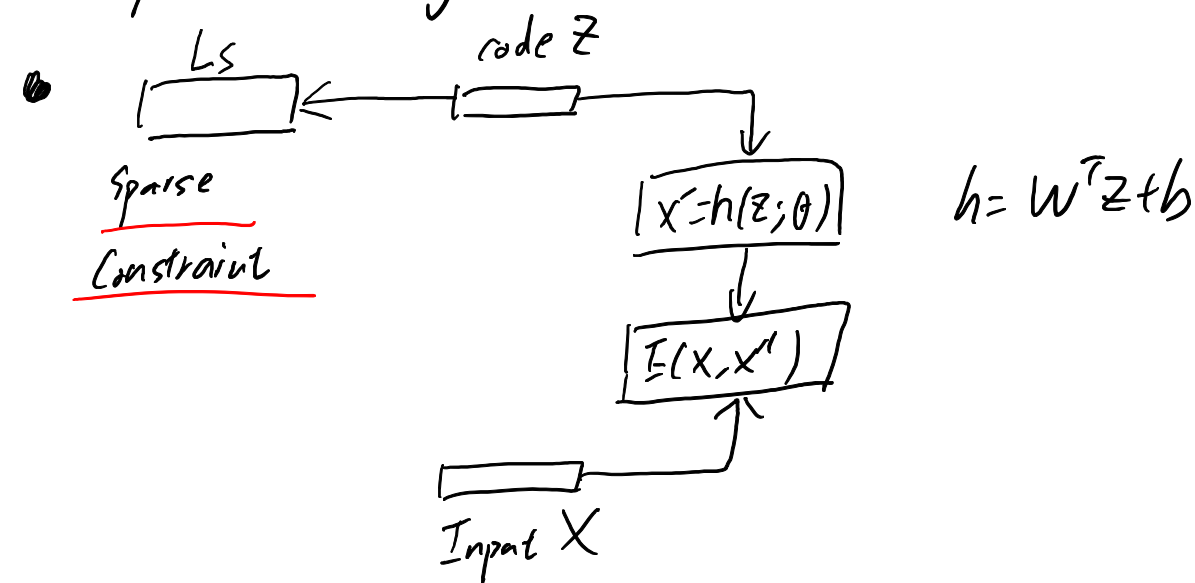
$$\theta_2 = \vec{D}, b_D$$

- Loss function =  $\alpha \cdot$  encoding energy + decode energy

PCA doesn't have encoding energy

- The learning process is similar to EM algo
- Backprop needs gradients of  $h()$ ,  $E_g$  and  $E_h$
- Two backprops needed due to there r two networks

## → Sparse coding



- Loss function  $= \|x - x'\|_2^2 + \lambda L_s(z)$
- Not really an autoencoder, but popular before 2009
- Limitation: exploding  $W$

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- Sparse autoencoder
  - Stacked sparse autoencoder