


L12

EC500/K

Binary units



$W_{ij} \leftarrow W_{ij} - \epsilon \nabla W_{ij}$
 $p(h_j=1 | \vec{v}) = \sigma(w_j^T \vec{v} + b_j)$
 $p(v_i=1 | \vec{h}) = \sigma(h^T w_i + a_i)$

Energy Function

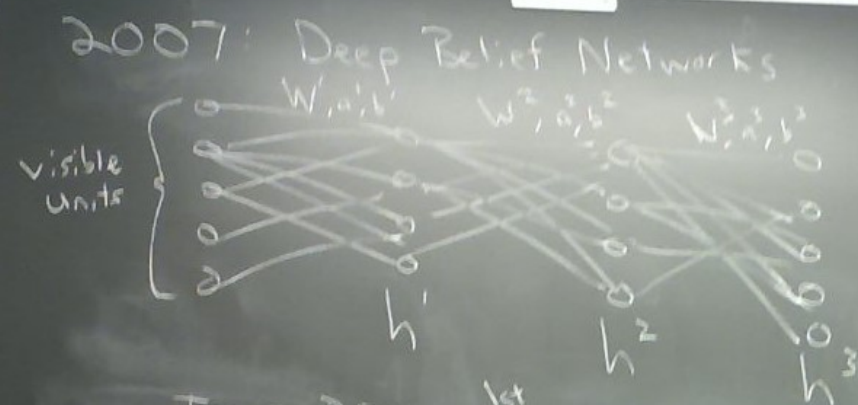
$$E(\vec{v}, \vec{h}) = -\vec{a}^T \vec{v} - \vec{b}^T \vec{h} - \vec{v}^T W \vec{h}$$

$$P(\vec{v}, \vec{h}) = \frac{1}{Z} e^{-E(\vec{v}, \vec{h})}$$

$$Z = \sum_{\vec{v}, \vec{h}} e^{-E(\vec{v}, \vec{h})}$$

$p(h_j=1 | \vec{v}) = \frac{e^{\vec{v}^T w_j + b_j}}{\sum_{k=1}^K e^{\vec{v}^T w_k + b_k}}$

2007: Deep Belief Networks



visible units
 h^1
 h^2
 h^3

Train RBM on 1st layer.
 Fix parameters.
 Sample values of h^1 for all training data.
 Train RBM on 2nd layer.
 Etc...

Greedy layer-wise pretraining

Real-valued visible units and binary hidden units

$$E(\vec{v}, \vec{h}) = \sum_{i=1}^d \frac{(v_i - a_i)^2}{2\sigma_i^2} - \sum_{j=1}^k b_j h_j - \sum_{ij} \frac{v_i}{\sigma_i} h_j w_{ij}$$

$$P(v|h) \sim \text{Gaussian}$$