

Homework 3 Report - Image Sentiment Classification

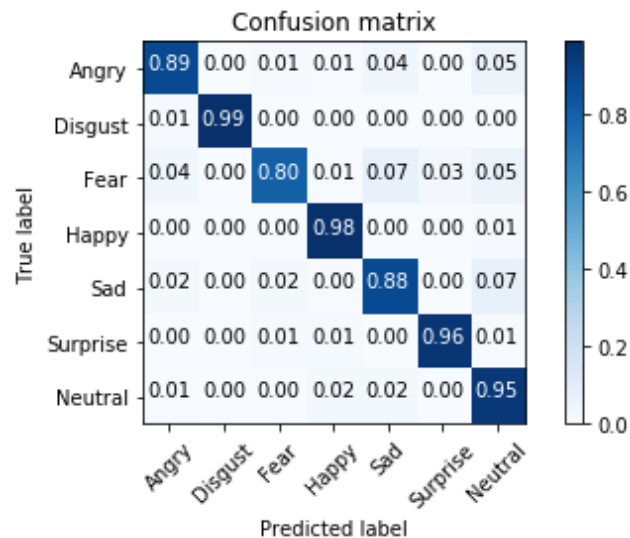
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- (1%) 請說明你實作的 CNN model，其模型架構、訓練過程和準確率為何？
- (1%) 承上題，請用與上述 CNN 接近的參數量，實做簡單的 DNN model，其模型架構、訓練過程和準確率為何？試與上題結果做比較，並說明你觀察到了什麼？

模型	CNN	DNN
架構	<pre> Layer (type) Output Shape Param # ===== conv2d_1 (Conv2D) (None, 48, 48, 64) 640 batch_normalization_1 (Batch Normalization) (None, 48, 48, 64) 256 leaky_re_lu_1 (LeakyReLU) (None, 48, 48, 64) 0 conv2d_2 (Conv2D) (None, 48, 48, 64) 36928 batch_normalization_2 (Batch Normalization) (None, 48, 48, 64) 256 leaky_re_lu_2 (LeakyReLU) (None, 48, 48, 64) 0 conv2d_3 (Conv2D) (None, 48, 48, 64) 36928 batch_normalization_3 (Batch Normalization) (None, 48, 48, 64) 256 leaky_re_lu_3 (LeakyReLU) (None, 48, 48, 64) 0 max_pooling2d_1 (MaxPooling2D) (None, 24, 24, 64) 0 dropout_1 (Dropout) (None, 24, 24, 64) 0 conv2d_4 (Conv2D) (None, 24, 24, 128) 73856 batch_normalization_4 (Batch Normalization) (None, 24, 24, 128) 512 leaky_re_lu_4 (LeakyReLU) (None, 24, 24, 128) 0 conv2d_5 (Conv2D) (None, 24, 24, 128) 147584 batch_normalization_5 (Batch Normalization) (None, 24, 24, 128) 512 leaky_re_lu_5 (LeakyReLU) (None, 24, 24, 128) 0 max_pooling2d_2 (MaxPooling2D) (None, 12, 12, 128) 0 dropout_2 (Dropout) (None, 12, 12, 128) 0 conv2d_6 (Conv2D) (None, 12, 12, 256) 295168 batch_normalization_6 (Batch Normalization) (None, 12, 12, 256) 1024 leaky_re_lu_6 (LeakyReLU) (None, 12, 12, 256) 0 conv2d_7 (Conv2D) (None, 12, 12, 256) 590080 batch_normalization_7 (Batch Normalization) (None, 12, 12, 256) 1024 leaky_re_lu_7 (LeakyReLU) (None, 12, 12, 256) 0 max_pooling2d_3 (MaxPooling2D) (None, 6, 6, 256) 0 dropout_3 (Dropout) (None, 6, 6, 256) 0 Flatten_1 (Flatten) (None, 9216) 0 dense_1 (Dense) (None, 512) 4719104 batch_normalization_8 (Batch Normalization) (None, 512) 2048 leaky_re_lu_8 (LeakyReLU) (None, 512) 0 dropout_4 (Dropout) (None, 512) 0 dense_2 (Dense) (None, 256) 131328 batch_normalization_9 (Batch Normalization) (None, 256) 1024 leaky_re_lu_9 (LeakyReLU) (None, 256) 0 dropout_5 (Dropout) (None, 256) 0 dense_3 (Dense) (None, 7) 1799 Total params: 6,040,327 Trainable params: 6,036,871 Non-trainable params: 3,456 </pre>	<pre> Layer (type) Output Shape Param # ===== Flatten_1 (Flatten) (None, 2304) 0 dense_1 (Dense) (None, 1024) 2360320 leaky_re_lu_1 (LeakyReLU) (None, 1024) 0 dense_2 (Dense) (None, 1024) 1049600 leaky_re_lu_2 (LeakyReLU) (None, 1024) 0 dense_3 (Dense) (None, 1024) 1049600 leaky_re_lu_3 (LeakyReLU) (None, 1024) 0 dense_4 (Dense) (None, 512) 524800 leaky_re_lu_4 (LeakyReLU) (None, 512) 0 dense_5 (Dense) (None, 512) 262560 leaky_re_lu_5 (LeakyReLU) (None, 512) 0 dense_6 (Dense) (None, 512) 262560 leaky_re_lu_6 (LeakyReLU) (None, 512) 0 dense_7 (Dense) (None, 512) 262560 leaky_re_lu_7 (LeakyReLU) (None, 512) 0 dense_8 (Dense) (None, 256) 131328 leaky_re_lu_8 (LeakyReLU) (None, 256) 0 dense_9 (Dense) (None, 256) 65792 leaky_re_lu_9 (LeakyReLU) (None, 256) 0 dense_10 (Dense) (None, 128) 32896 leaky_re_lu_10 (LeakyReLU) (None, 128) 0 dense_11 (Dense) (None, 128) 16512 leaky_re_lu_11 (LeakyReLU) (None, 128) 0 dense_12 (Dense) (None, 64) 8256 leaky_re_lu_12 (LeakyReLU) (None, 64) 0 dense_13 (Dense) (None, 64) 4160 leaky_re_lu_13 (LeakyReLU) (None, 64) 0 dense_14 (Dense) (None, 32) 2080 leaky_re_lu_14 (LeakyReLU) (None, 32) 0 dense_15 (Dense) (None, 32) 1056 leaky_re_lu_15 (LeakyReLU) (None, 32) 0 dense_16 (Dense) (None, 32) 1056 leaky_re_lu_16 (LeakyReLU) (None, 32) 0 dense_17 (Dense) (None, 16) 528 leaky_re_lu_17 (LeakyReLU) (None, 16) 0 dense_18 (Dense) (None, 16) 272 leaky_re_lu_18 (LeakyReLU) (None, 16) 0 dense_19 (Dense) (None, 16) 272 leaky_re_lu_19 (LeakyReLU) (None, 16) 0 dense_20 (Dense) (None, 8) 136 leaky_re_lu_20 (LeakyReLU) (None, 8) 0 dense_21 (Dense) (None, 8) 72 leaky_re_lu_21 (LeakyReLU) (None, 8) 0 dense_22 (Dense) (None, 8) 72 leaky_re_lu_22 (LeakyReLU) (None, 8) 0 dense_23 (Dense) (None, 7) 63 Total params: 6,036,839 Trainable params: 6,036,839 Non-trainable params: 0 </pre>
訓練過程 (橫:epoch; 縱:val acc)		
準確率	69%	14%

CNN 說明& 比較 結果	<p>我的 CNN 架構採用類似 VGG16 多層卷積層後才連接池化層的方式，共疊了三個大層後再接兩層 Fully Connected，並以 Softmax 輸出。統一使用 LeakyReLU(alpha=0.3)當 activation function、Dropout=0.3，並加入 BatchNormalization 改善。</p> <p>使用相同參數量的 DNN 模型很顯然會在前幾個 epoch 便嚴重 overfit 了。雖然本來使用 fully connected 就會很容易 overfit，但是相同數量的參數下 CNN 還有相當漂亮的結果，因此可以得知使用圖片的特性來訓練一個模型在處理影響辨識上相當重要。</p>
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3. (1%) 觀察答錯的圖片中，哪些 class 彼此間容易用混？並說明你觀察到了什麼？ [繪出 confusion matrix 分析]



容易搞混的 class:

- (1) Fear ↔ Sad, Neutral, Angry
- (2) Sad ↔ Neutral
- (3) Angry ↔ Sad, Neutral

Neutral(中性)的 label 針對自己的預測準確率很高，但其他的 label(Fear, Sad, Angry)卻很容易預測到 Neutral 上。在所有的 label 中，Fear 的準確率最低，Disgust 跟 Happy 的準確率最高。

4. (1.5%, each 0.5%)CNN time/space complexity:

For a. b. Given a CNN model as

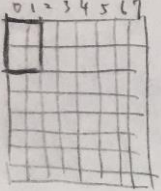
```
model = Sequential()
model.add(Conv2D(filters=6,
                  strides=(3, 3),
                  padding = "valid",
                  kernel_size=(2,2),
                  input_shape=(8,8,5),
                  activation='relu'))
model.add(Conv2D(filters=4,
                  strides=(2, 2),
                  padding = "valid",
                  kernel_size=(2,2),
                  activation='relu'))
```

And for the c. given the parameter as:

kernel size = (k, k) ; channel size = c ; input shape of each layer = (n, n) ;

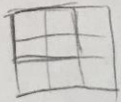
padding = p ; strides = (s, s) ;

- How many parameters are there in each layer (Hint: you may consider whether the number of parameter is related with)
- How many multiplications/additions are needed for a forward pass (each layer).
- What is the time complexity of convolutional neural networks? (note: you must use big-O upper bound, and there are l (lower case of L) layer, you can use C_l , C_{l-1} as l th and $l-1$ th layer)

4. a. 

\therefore total in layer A: $6 \times (5 \times 2 + 1)$
 $= 126 \neq$

\Rightarrow output $3 \times 3 \times 5$

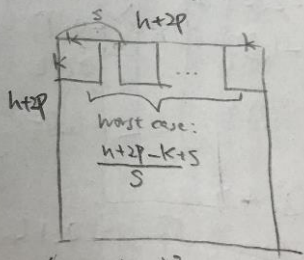


\therefore total in layer B: $4 \times (6 \times 2 + 1) = 100 \neq$

b. layer A: $6 \times (5 \times 2 \times 3 \times 3) = 1080$ (multiplication)
 $6 \times (3 \times 3) \times (5 \times 2 \times 2 - 1) = 1026$ (addition)

layer B: $4 \times (6 \times 2 \times 1 \times 1) = 96$ (multiplication)
 $4 \times (1 \times 1) \times (6 \times 2 \times 2 - 1) = 92$ (addition)

c. kernel size: (k, k)
channel size = C
input shape of each layer = (n, n)
padding = p
strides: (s, s)



Multiplication: $C_i \times C_{i-1} \times k \times k \times \left(\frac{n+2p-k+s}{s}\right)^2$ (Bis 0)

Addition: $C_i \times \left(\frac{n+2p-k+s}{s}\right)^2 \times [C_{i-1} \times k \times k - 1]$ (Bis 0)

$\Rightarrow \sum_{i=1}^l O\left(C_i \times \left(\frac{n+2p-k+s}{s}\right)^2 [2C_{i-1}k^2 - 1]\right)$

5. (1.5%, each 0.5%) PCA practice: Problem statement: Given 10 samples in 3D space.

(1,2,3), (4,8,5), (3,12,9), (1,8,5), (5,14,2), (7,4,1), (9,8,9), (3,8,1), (11,5,6), (10,11,7)

(1) What are the principal axes?

(2) Compute the principal components for each sample.

(3) Reconstruction error if reduced to 2D. (Calculate the L2-norm)

Covariance matrix

$$\begin{bmatrix} 12.04 & 0.5 & 3.28 \\ 0.5 & 12.2 & 2.9 \\ 3.28 & 2.9 & 8.16 \end{bmatrix}$$

a. principle axes:

$$\lambda_1 = 15.2974434$$

$$\lambda_2 = 11.63052369$$

$$\lambda_3 = 5.47203291$$

$$\begin{bmatrix} -0.6165747 \\ -0.58881629 \\ -0.52259379 \end{bmatrix}$$

$$\begin{bmatrix} -0.67817891 \\ 0.73431013 \\ -0.02728563 \end{bmatrix}$$

$$\begin{bmatrix} 0.31875541 \\ 0.33258926 \\ -0.75214385 \end{bmatrix}$$

b.

$$\begin{bmatrix} -2.25 \\ -1.37 \\ 7.19 \end{bmatrix}, \begin{bmatrix} -0.73 \\ 0.94 \\ 0.75 \end{bmatrix}, \begin{bmatrix} -2.19 \\ 4.45 \\ -2.07 \end{bmatrix}, \begin{bmatrix} -1.93 \\ 2.98 \\ 2.61 \end{bmatrix}, \begin{bmatrix} 4.25 \\ 4.75 \\ -1.82 \end{bmatrix},$$

$$\begin{bmatrix} 2.53 \\ -3.92 \\ 3.35 \end{bmatrix}, \begin{bmatrix} -2.14 \\ -2.56 \\ -4.41 \end{bmatrix}, \begin{bmatrix} 2.28 \\ 1.77 \\ 3.47 \end{bmatrix}, \begin{bmatrix} 0.20 \\ -6.03 \\ -2.31 \end{bmatrix}, \begin{bmatrix} 0.98 \\ -0.98 \\ -5.75 \end{bmatrix}$$

c.

2.25, 0.73, 3.19, 1.93, 4.25, 2.53, 2.14, 2.28,

0.20, 0.98