## 13 TRIBHUVAN UNIVERSITY INSTITUTE OF ENGINEERING

## Examination Control Division

2073 Magh

| Exam.       | 。New Sad Sea (                 |            |        |  |
|-------------|--------------------------------|------------|--------|--|
| Level       | BE                             | Full Marks | 80     |  |
| Programme   | BEL, BEX, BCT.<br>B. Agri, BGE | Pass Marks | 32     |  |
| Year / Part | П/Ц .                          | Time       | 3 hrs. |  |

## Subject: - Numerical Method (SH553)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- √ Attempt All questions.
- ✓ The figures in the margin indicate <u>Full Marks</u>.
- √ Assume suitable data if necessary.



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- 1. Discuss the importance of Numerical Methods in Science and Engineering
- 2. Find a real root of  $\cos x + e^x 5 = 0$  accurate to 4 decimal places using the Secant Method. [6]
- 3. Write pseudo-code to find a real root of a non-linear equation using the Bisection Method. [6]
- 4. Compute the inverse of following matrix using the Gauss-Jordan Method.





- 5. Write algorithm for computing the dominant Eigen value and corresponding vector of a square matrix using the Power method.
- 6. Fit the following set of data to a curve of the form  $y = ab^x$ .

| x | 1.0 | 1.5 | 2.0 | 2.5 | 3.0 | 3.5 | 4.0 |
|---|-----|-----|-----|-----|-----|-----|-----|
| y | 8.2 | 5.2 | 3.1 | 2.5 | 1.7 | 1.6 | 1.4 |

7. Estimate y(4.5) from the following data using Natural Cubic Spline Interpolation technique.

|     |   |    |    | · · · |     |   |   |
|-----|---|----|----|-------|-----|---|---|
| . 1 | T | T  | 3  | 0     | 7   | 5 | F |
|     | y | 10 | 12 | 11    | 13- | 9 | - |

- 8. Derive the formula to evaluate y'(x) and y''(x) from Newton's Forward Interpolation formula.
- 9. Evaluate  $\int_{0}^{1.4} (\sin x^3 + \cos x^2) dx$  using Gaussian 3-point formula.



[4]

- Solve  $y' = \sin x + \cos y$  subject to initial condition y(0) = 2 in the range 0(0.5)2 using the Runge-Kutta second order method. [6]
- Write a program in C/C++/FORTRAN to solve a second order ordinary differential equation [6] (initial value problem) using the Runge-Kutta fourth order method.
- 12. Solve the elliptic equation  $u_{xx} + u_{yy} = 0$  for the square mesh with boundary values as shown in the figure below. [10]

