

| Exam.       | New Back (2066 & Later Batch) |            |        |
|-------------|-------------------------------|------------|--------|
| Level       | BE                            | Full Marks | 80     |
| Programme   | BEL, BEX,<br>BCT, B.Agric.    | Pass Marks | 32     |
| Year / Part | II / II                       | Time       | 3 hrs. |

Subject: - Numerical Method (SH553)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

[14]



1. Discuss the importance of Numerical Methods in the field of Science and Engineering. [4]
2. Write pseudo-code for finding a real root of a non-linear equation using False Position Method. [6]
3. Find a real root of the following equation, correct to three decimals, using the Fixed Point iteration method. [6]

$$\sin x + 3x - 2 = 0$$

4. Solve the following systems of linear equations using the Gauss-Seidal iteration method. [8]

$$x_1 + 3x_2 - x_3 + 7x_4 = 19$$

$$2x_1 + 8x_2 + x_3 - x_4 = 17$$

$$3x_1 + x_2 + 9x_3 - x_4 = 15$$

$$9x_1 - x_2 - x_3 + 2x_4 = 13$$

5. Find the largest Eigen value and corresponding vector of the following matrix using power method. [8]

$$\begin{bmatrix} 2 & 5 & 1 \\ 5 & -2 & 3 \\ 1 & 3 & 10 \end{bmatrix}$$

6. Compute the value of y(3) and y(7) from the following data using Newton's interpolation formula. [8]

|   |     |     |     |     |     |     |
|---|-----|-----|-----|-----|-----|-----|
| x | 2   | 4   | 6   | 8   | 10  | 12  |
| y | 5.1 | 4.2 | 3.1 | 3.5 | 6.2 | 7.3 |

7. Fit the following data to the curve  $y = \log_e(ax+b)$ . [8]

|   |     |     |     |     |     |     |     |
|---|-----|-----|-----|-----|-----|-----|-----|
| x | 0   | 1   | 2   | 3   | 4   | 5   | 6   |
| y | 0.9 | 1.0 | 1.5 | 1.9 | 2.1 | 2.4 | 2.5 |

8. Evaluate the following, using simpson's 1/3 rule. (take  $h = 0.2$ )  $\int_0^2 \frac{4e^x}{1+x^3} dx$  [5]

9. Evaluate  $\int_2^3 \frac{\cos 2x}{1+\sin x} dx$  using Gauss quadrature three-point formula. [5]



10. Solve the following boundary value problem using finite difference method. [8]

$$y'' = e^x + 2y' - y; \quad y(0) = 1.5; \quad y(2) = 2.5$$

11. Explain the technique of solving an initial value problem using Euler's method. [4]

12. Find the value of  $u(x,y)$  satisfying the Laplace equation  $\nabla^2 u = 0$ , at the pivotal points of the square region with boundary conditions as shown below. [10]

