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SEQUENCE AND SERIES

EE23BTECH11011- Batchu Ishitha*

- Q: (i). For the wave on the string $y(x,t) = 0.06\sin(\frac{2\pi x}{3})\cos(120\pi t)$, do all the points on the string oscillate with the same (a)frequency, (b)phase, (c)amplitude? Explain your answers.
 - (ii). What is the amplitude of a point 0.375m away from one end?

Solution:

- (i). For the wave on the string, l = 1.5m and $\lambda = 3m$. So, it is clear that $l = \lambda/2$ and for a string clamped at both ends,
- it is possible only when both ends behave as nodes and there is only one antinode in between i.e., whole string is vibrating in one segment only.
- (a). Yes, all the string particles, except nodes, vibrate with the same frequency v = 60 Hz and the frequency of nodes is zero.
- (b). All the particles in the wire lie in one segment; thus, they all have the same phase. Except for the nodes.
- (c). Amplitude varies from particle to particle. At antinode, amplitude = 2A = 0.06 m. It gradually falls on going towards nodes and at nodes, it is zero.
 - (ii).given the equation of wave; $y(x,t) = 0.06 \sin(\frac{2\pi x}{3}) \cos(120\pi t)$, x=0.375m

$$amplitude = 0.06sin(\frac{2\pi(0.375)}{3})\tag{1}$$

$$=0.06\sin(\frac{\pi}{4})\tag{2}$$

$$= 0.042m.$$
 (3)