1

SEQUENCE AND SERIES

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Q: Find the sum to n terms of the series whose n^{th} term is given by $(2n-1)^2$? **Solution:**

	Variable	Description	Value
ĺ	x(n)	n th term of sequence	$(2n+1)^2 u(n)$
		TABLE 0	
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Sum of n terms of AP is given by

$$y(n) = x(n) * u(n) \tag{1}$$

$$x(n) = (2n+1)^2 u(n)$$
 (2)

$$u(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} \frac{1}{(1-z^{-1})} \quad |z| > 1$$
 (3)

$$nu(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} \frac{z^{-1}}{(1-z^{-1})^2} \quad |z| > 1 \tag{4}$$

$$n^2 u(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} \frac{z^{-1}(1+z^{-1})}{(1-z^{-1})^3} \quad |z| > 1$$
 (5)

$$\implies X(z) = \frac{4z^{-1}(1+z^{-1})}{(1-z^{-1})^3} + \frac{1}{(1-z^{-1})} + \frac{4z^{-1}}{(1-z^{-1})^2} \quad |z| > 1$$
 (6)

$$Y(z) = X(z)U(z) \tag{7}$$

$$= \left(\frac{4z^{-1}(z^{-1}+1)}{(1-z^{-1})^3} + \frac{1}{(1-z^{-1})} + \frac{4z^{-1}}{(1-z^{-1})^2}\right) \left(\frac{1}{1-z^{-1}}\right)$$
(8)

$$= \frac{1+9z^{-1}}{(1-z^{-1})} + \frac{25z^{-2}}{(1-z^{-1})^2} + \frac{24z^{-3}}{(1-z^{-1})^3} + \frac{8z^{-4}}{(1-z^{-1})^4} \quad |z| > 1$$
 (9)

On solving, we get

$$y(n) = \left(\frac{4n^3 + 12n^2 + 11n + 3}{3}\right)u(n) \tag{10}$$

... Sum of *n* terms of the series whose n^{th} term is given by $(2n+1)^2$ is $\frac{4n^3+12n^2+11n+3}{3}$.

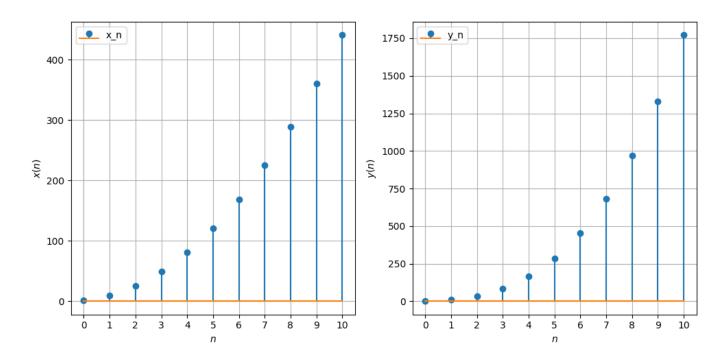


Fig. 0.