Multi-output Bus Travel Time Prediction Using Convolutional LSTM Neural Network

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Abstract

This paper presents a multi-output, multi-time-step, deep neural network for bus travel time prediction using Convolutional and Long short-term memory (LSTM) layers. The method is evaluated and compared to other popular approaches for link travel time prediction.

Keywords: Bus Travel Time Prediction, Intelligent Transport Systems, Convolutional Neural Network (CNN), Long short-term memory (LSTM)

1. Introduction

Public transport authorities has long found that GPS trajectory data from already deployed *Automatic Vehicle Location*-systems (AVL) can be used in *Intelligent Transport Systems* (ITS) [1]. Examples include real-time traffic information for passengers, e.g. departure boards, where studies has shown that reliable real-time information at bus stops has a statistical significant dampening effect on the perceived waiting time [2].

Besides real-time passenger information, robust arrival- and departure time predictions are necessary for operating more sophisticated ITS applications successfully, e.g. demand-adaptive transit systems, and *connection insurance* between different public transport services. Arrival/departure time prediction is commonly approached as a specialization of travel time prediction, where the predicted travel time is simply accumulated downstream the route to yield the arrival/departure time predictions at each stop point of the rest of the current journey. Besides the link travel time, estimations of dwell time (i.e. when a bus is holding at a stop point) are accumulated downstream.

Producing precise bus travel time predictions in areas with little external influence, e.g. rural areas, can be solved to a large extent with historical averaging or simple regression methods [3, 4]. The problem becomes much more complex in urban areas where congestion, events, road-works, weather, etc. highly influences the traffic flow and passenger demand.

In this paper we presents a multi-output, multi-time-step deep neural network for bus travel time prediction using *Convolutional* and *Long short-term memory* (LSTM) [5, 6] layers. The goal of this work is to produce precise short-term predictions (e.g. 0–3 hours) for link travel time, specifically for bus traffic in urban areas. The method is evaluated and compared to other popular approaches for link travel time prediction. The paper is structured in the following manner: In the next related work and literature is reviewed. Section 2 introduces Convolutional LSTM neural networks in general and in Section 3 we present the proposed multi-output model in more details, including e.g. network topology, etc. Section 4 introduces the dataset which the model has been evaluated on and results are presented and discussed in Section 5. Finally we conclude on the work in Section 6.

1.1. Literature review

Early approaches presents historical averaging models [7, 8], and linear regression [9]. Recent research presents this type of model only for comparison purpose, and the models are in all cases outperformed by the compared models [10, 11]. Kalman-filters, which by its capabilities of maintaining state between predictions, has shown interest from several studies, either as an independent model [12, 10] or in combination with other models [13, 14].

Both the different regression style models and the Kalman-filter models still has limited options for capturing fluctuations in travel and dwell time in a metropolitan bus system, since they to a large extent still is averaging and smoothing their response. E.g., the Kalman-filter's state is only directly accessible for the leading time step, and thus not capable of finding long-distance patterns spanning over several links and/or over several time steps. This is substantiated by [15] and [16] that finds artificial neural networks (ANN) outperforms Kalman-filter models.

The computational challenges of pure ANN approaches i.a. has sparked the interest for studying composite or hybrid models. [13] uses a two-stage approach by combining offline ANN-models, with an adaptable/online Kalman-filter to yield a dynamic model. The model is not actually learning in the long term, but is able to adapt to temporal variations in the current travel time on a journey.

Some recent research recognizes that several routes can benefit from each other's predictions if they share some partial route segment, e.g. [17, 18, 14], however none of these approaches consider cross temporal correlations between different route segments, and only uses a small window for correlation with upstream links (e.g. max. 3 links).

[19] proposes to use LSTM model for general highway travel time prediction, and do predict multiple steps ahead, but only for a single link at a time, i.e. cross link (spacial) correlations are lost.

2. Convolutional LSTM neural networks

A Long short-term memory (LSTM) neural network is a special type of Recurrent Neural Network (RNN) which has proven robust for capturing long-distance dependencies [5, 6]. The important feature of a LSTM network is its capability to persist cell state, c_t, from previous observations across sequences of input (e.g. time), but also eliminate information which is considered unimportant. To allow this mechanism the persistence of information is controlled by three gates: *input gate*, *forget gate*, and *output gate*. Each gate yields a state value at time t, respectively i_t, f_t, and o_t, along with the cell output, h_t, cf. Equation (1).

$$
\begin{aligned}
i_t &= \sigma\left(W_{xi}x_t + W_{hi}h_{t-1} + W_{ci}c_{t-1} + b_i\right)\\
f_t &= \sigma\left(W_{xf}x_t + W_{hf}h_{t-1} + W_{cf}c_{t-1} + b_f\right)\\
c_t &= f_t c_{t-1} + i_t \tanh\left(W_{xc}x_t + W_{hc}h_{t-1} + b_c\right)\\
o_t &= \sigma\left(W_{xo}x_t + W_{ho}h_{t-1} + W_{co}c_t + b_o\right)\\
h_t &= o_t \tanh\left(c_t\right)
\end{aligned}
\tag{1}
$$

Figure 1 illustrates the inner structure of a LSTM cell with peephole as proposed by [20]. Is has especially grown popular for predicting time series using methods evolved from [21], where fixed-length windows of time-series are generated and feed into a LSTM network. Multiple LSTMs can be stacked such more complex patterns of sequential information (e.g. temporal patterns) can be learned.

Convolutional Neural Networks (CNN) on the other hand has been widely used for capturing spacial relationships, e.g. importance of neighboring pixels in an image. As opposed to fully connected layers, where each unit, i, in the

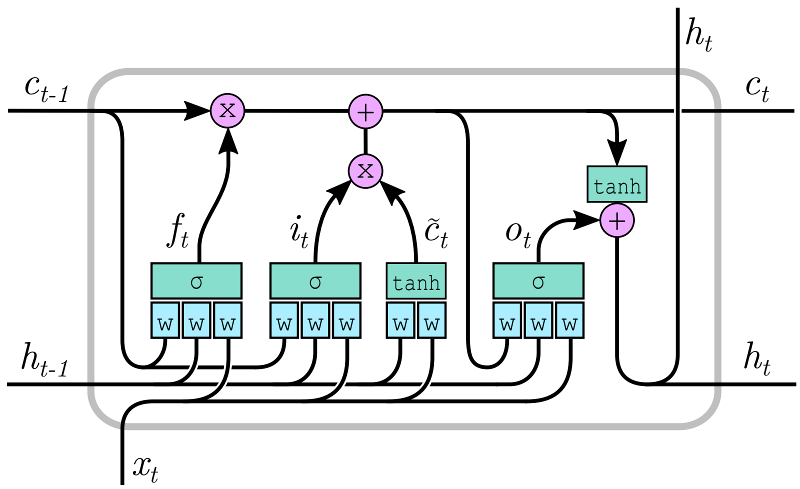

Figure 1: Structure of LSTM cell with peephole.

layer, has a dedicated weight, w_{ij}, for all input, x_j, convolutional units are only locally connected and reuses the same weights for producing several outputs. Instead of considering the entire input-vector, only a fixed sized window, or *convolution*, around each input is considered. The weights are therefore referred to as the *filters* or *kernels* of the layer. Figure 2 illustrates a single convolutional filter of size 3 being applied to 1-dimensional data.

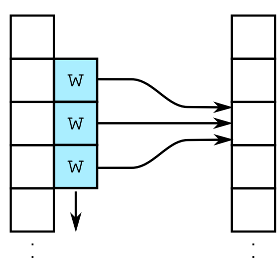

Figure 2: Application of Convolutional filter onto 1D data.

Special care needs to be taken on the boundaries, i.e. where the convolutional filter will exceed the input. A popular approach to avoid the size of the output decreases is to pad the input, e.g. with zeros. This ensures that the output shape of each convolutional unit will always be identical to the input shape, which is often desirable. One of the key benefits of convolutional networks is that the number of weights that needs to be learned is greatly reduced compared to fully connected networks, and that learned patterns transfers across space. I.e. the convolutional filters become feature detectors, that in our case can detect spacial patterns across links, e.g. congestion forming, etc.

[22] introduced the novel combination of Convolutional and LSTM layers into a single structure, the *Convolutional LSTM*, or simply *ConvLSTM*. Specifically the method applies convolutional filters in the input-to-state and state-to-state transitions the LSTM cf. Equation (2), where $*$ denotes the convolution operator.

$$\begin{aligned} i_t &= \sigma\left(W_{xi} * x_t + W_{hi} * h_{t-1} + W_{ci} c_{t-1} + b_i\right) \\ f_t &= \sigma\left(W_{xf} * x_t + W_{hf} * h_{t-1} + W_{cf} c_{t-1} + b_f\right) \\ c_t &= f_t c_{t-1} + i_t \tanh\left(W_{xc} * x_t + W_{hc} * h_{t-1} + b_c\right) \\ o_t &= \sigma\left(W_{xo} * x_t + W_{ho} * h_{t-1} + W_{co} c_t + b_o\right) \\ h_t &= o_t \tanh\left(c_t\right) \end{aligned} \tag{2}$$

3. Multi-output model

Input data is arranged in N samples, each with w time steps $t-w+1,\ldots,t$, and each time step with k link travel times $e_1,\ldots,e_k$ cf. Figure 3. Likewise is the output arranged with predictions of j time steps ahead, $t+1,\ldots,t+j$. Thus the input is a 4D-tensor with shape $(N, w, k, 1)$, and the output a 4D-tensor with shape $(N, j, k, 1)$. It is emphasized that each prediction consists of travel time predictions for all links for the next j time steps, i.e. multi-output, multi-time-step prediction.

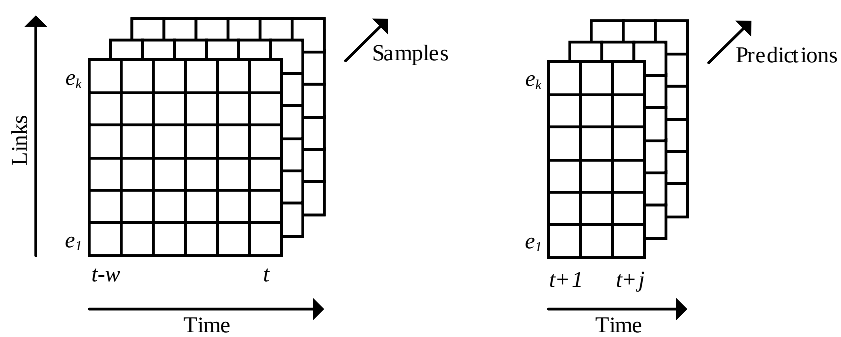

Figure 3: Shapes of the input and output data.

Obviously the travel time varies throughout the time of the day, and the day of the week due to *recurring congestion*. In order to reduce the need for the network to learn this recurring variation, data is normalized to focus on deviations from the normal and expected pattern. Travel times are centered with the mean for each link, at teh time of day, and day of week, $\bar{x}_{l,dow,tod}$, and scaled with the standard for each link, σ_l, cf. Equation (3).

$$\frac{x - \bar{x}_{l,dow,tod}}{\sigma_l} \tag{3}$$

3.1. Network topology and training

Figure 4 shows the overall network topology, where blue boxes illustrates *input-to-state* convolutions and yellow *state-to-state* convolutions. The network uses an encoder/decoder technique that to a large extent follows [22], where the encoder-block consists of two *ConvLSTM* layers. The result is feed into a decoder, or prediction block, also consisting of two *ConvLSTM* layers. The architecture allows unequal w and k, e.g. predict the next 3 time steps based on a window size of 10.

Thus convolutional filters are applied to each input, at each time step to the respective LSTM-cell, and also between LSTM-cells in the state-transition. Since the time steps are one-dimensional (link travel times across links), the filters are also one-dimensional. In total the 4 layers of Convolutional LSTMs are arranged with filter sizes of 5×1 for both *input-to-state* and *state-to-state* filters.

To avoid over-fitting doing training *Dropout* [23] is performed between the *ConvLSTM* layers, and *Batch Normalization* [24] are also performed before each *ConvLSTM* layers to ensure reasonable input for activations. The dropout factor is adjusted to respectively 20%, 10% and 10%.

The network is trained using the *RMSprop*-algorithm [25].

4. Experiments

For evaluation the method is applied to a dataset from Copenhagen's public transport authority. The dataset consists of 814,710 travel time observations for the "4A" bus line in the period January 1 to May 31 2017. The data points were collected using the real-time AVL-system installed in all vehicles of the line. The geography of the route is shown in Figure 5. As the line circles central Copenhagen, it is potentially highly sensitive to

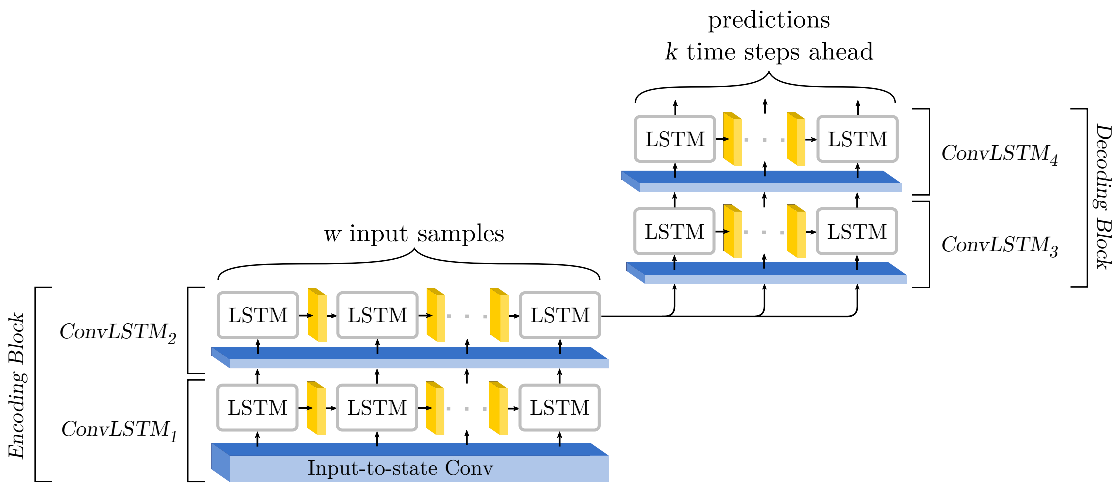

Figure 4: Convolutional LSTM network topology.

congestion to/from the city as it intersects with several large corridors along its route.

TODO: How much used for training, how much for testing?

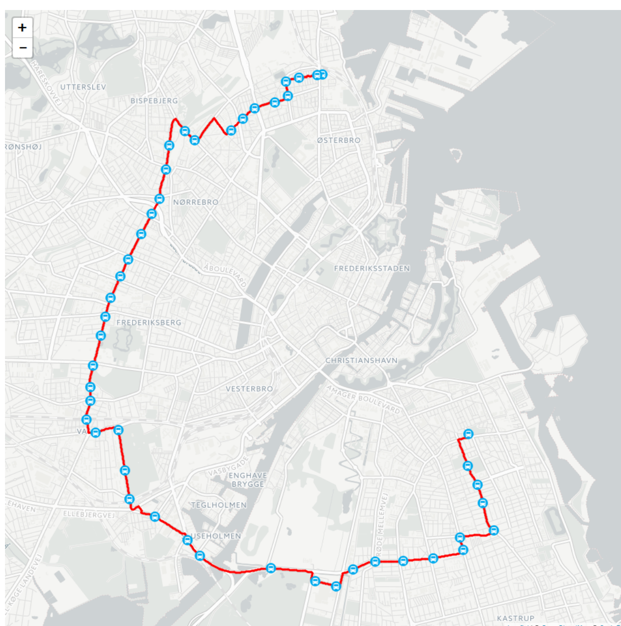

Figure 5: Geography of the 4A bus line in Copenhagen.

4.1. Data preprocessing

Since the travel time measurement contains several extreme outliers due to measurement faults, these were labeled and dropped using the *absolute deviation around the median* (MAD) cf. [26]. Data is aggregated into 15-minute time steps and normalized cf. Section 3.

The implementation of the proposed model was done in Python using Keras [27].

4.2. Evaluation

In order to evaluate the presented model and comparisons, the following measures is used: *mean absolute error* (MAE), *root mean square error* (RMSE), and *mean absolute percentage error* (MAPE) cf. Equations (4) to (6), where X_i is the true travel time for sample i and $\widehat{X}_i$ is the predicted travel time.

$$\mathrm{MAE}(X, \widehat{X}) = \frac{\sum_{i=1}^{n} \left| X_i - \widehat{X}_i \right|}{n} \tag{4}$$

$$\mathrm{RMSE}(X, \widehat{X}) = \sqrt{\frac{\sum_{i=1}^{n} \left(X_i - \widehat{X}_i \right)^2}{n}} \tag{5}$$

$$\mathrm{MAPE}(X, \widehat{X}) = \frac{1}{n} \sum_{i=1}^{n} \left| \frac{X_i - \widehat{X}_i}{X_i} \right| \tag{6}$$

5. Results and discussion

The model is trained on the prepared data using a sliding window approach to simulate real-world conditions where real-time travel time measurements arrives as a continuously data stream. Figure 6 shows the evolution of training and validation loss for each epoch for such a window, where the loss is the MAE if the individual links.

Table 1 shows the results of the presented method and compares to two other methods: 1) a nave historical average model, i.e. equivalent of just prediction the normalized value, $\bar{x}_{l,dow,tod}$ and 2) a pure LSTM model as proposed by [19]. Predictions are accumulated downstream on journey level to simulate for use in real-time bus arrival/departure time prediction.

TODO: Needs to be updated ...

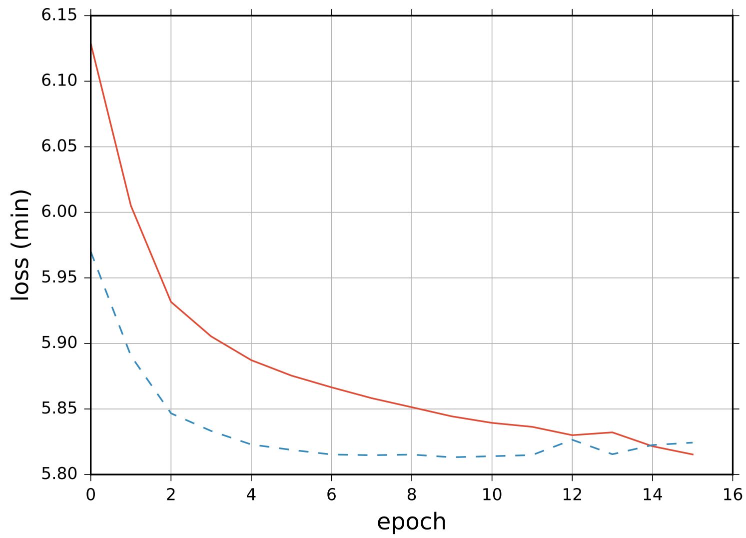

Figure 6: Training and validation loss evolution.

From the table it is found that the Convolutional LSTM performs better than the compared methods. Although the advantage might seem small it is emphasized that evaluation measurements are averaging their response, and thus the increased accuracy can be much higher on individual journeys, especially if they experienced very irregular travel times.

Table 1: Results of the presented and other popular models

Model	Time ahead	MAE (min)	RMSE (min)	MAPE (%)
Historical average		4.90	6.32	7.38 %
Pure LSTM	t + 1 (15 min)	3.71	3.71	5.87 %
Pure LSTM	t + 2 (30 min)	4.31	5.63	6.63 %
Pure LSTM	t + 3 (45 min)	4.97	6.41	7.52 %
Convolutional LSTM	t + 1 (15 min)	2.96	3.94	5.10 %
Convolutional LSTM	t + 2 (30 min)	3.04	4.08	5.21 %
Convolutional LSTM	t + 3 (45 min)	3.17	4.24	5.37 %

5.1. Future work

For the prediction accuracy to be increased further it is proposed to apply ensemble/multi-model approaches. In this case the presented model can be included and used as a sub-model for the ensemble. Further research should be invested in the more rare, but highly impacting deviations, e.g. traffic incidents, extreme weather conditions, etc.

6. Conclusion

This paper has presented a multi-output, multi-time-step deep neural network for bus travel time prediction using Convolutional and Long short-term memory (LSTM) layers. Results shown the presented network outperforms other popular and recent methods.

Future research opportunities include using the model a part of a multi-model ensemble, and focus in the more rare, but highly impacting deviations.

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