

ENGG1003 - Friday Week 1

Algorithms and Pseudocode

Brenton Schulz

University of Newcastle

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Algorithms

- ▶ Informally, an *algorithm* is a series of steps which accomplishes a task
- ▶ More accurately, the steps (instructions) must:
 - ▶ Have a strict order
 - ▶ Be unambiguous
 - ▶ Be executable
- ▶ “Executable” means that the *target platform* is capable of performing that task.
 - ▶ eg: An industrial welding robot can execute “move welding tip 1 cm left”. A mobile phone can’t.

Algorithms

- ▶ An algorithm exists purely as an abstract concept until it is communicated
- ▶ We will use:
 - ▶ *Pseudocode* to communicate algorithms to ourself's and other people
 - ▶ The languages C and MATLAB to communicate algorithms to computers
- ▶ Pseudocode *can* be very formal, but as engineers we will only use formal rules if required
 - ▶ eg: When documenting algorithms for other people
 - ▶ Your own “working out” can be anything that helps *you*

Algorithm Example 1

Example 1: Algorithm given to mum to start my car (2015 Tarago)

Result: The vehicle's engine is idling

Initialisation: stand next to the vehicle, key fob in hand

1. Depress the unlock button on the key fob, car will beep twice
2. Place key fob in your pocket
3. Enter the vehicle, sit in the driver's seat
4. Ensure that the gear selector has P engaged
5. Depress the brake pedal
6. Observe that the green LED is lit on the engine start button
7. Press the engine start button
8. If engine is not idling

▶ Call me

Example Discussion

- ▶ Algorithms typically need to feel over-explained
 - ▶ Computers are *really stupid*; get in the habit of over-thinking everything
- ▶ The algorithm contained *flow control* in the form of an “if” statement
 - ▶ The final step (“call me”) was *conditional* on the car not starting
- ▶ We will discuss logical statements later, but first...

Algorithm Example 2

A wife asks her husband, a programmer, “Could you please go shopping for me and buy one carton of milk, and if they have eggs, get 6?”

A short time later the husband comes back with 6 cartons of milk and his wife asks, “Why did you buy 6 cartons of milk?”

He replies, “They had eggs.”

Algorithm Example 2a

Lets make this more realistic.

A wife asks her robot helper, “Could you please go shopping for me and buy one carton of milk, and if they have eggs, get 6?”

The robot replies: “Unknown instruction: ‘get 6’. ”

Conditions

- ▶ Computers don't understand “maybe”
- ▶ A *condition* must be absolutely **true** or **false**
- ▶ Human examples:
 - ▶ I am within the boundary of the Callaghan campus
 - ▶ I am alive
 - ▶ My net worth is below AU\$100M
- ▶ Computer examples:
 - ▶ i is less than 184
 - ▶ x plus y is not equal to zero
 - ▶ Input data has been given to the program
 - ▶ A division by zero occurred

Algorithm Example 3 - Quadratic Root Finding

From high school you should know that the equation

$$ax^2 + bx + c = 0 \quad (1)$$

has solutions given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad (2)$$

lets write an algorithm which only deals with real numbers.

Algorithm Example 3 - Quadratic Root Finding

Input: Real numbers a , b , and c

Output: Three numbers:

1. The number of solutions, N
2. One of the roots, x_1
3. The other root, x_2

Behaviour:

- ▶ If N is 2 then x_1 and x_2 are different real numbers
- ▶ If N is 1 then x_1 is the unique solution and x_2 is undefined
- ▶ If N is 0 then x_1 and x_2 are undefined

Algorithm Example 3 - Quadratic Root Finding

```
BEGIN
   $D = b^2 - 4ac$ 
  IF  $D < 0$ 
     $N = 0$ 
  ELSE IF  $D = 0$ 
     $N = 1$ 
     $x_1 = \frac{-b}{2a}$ 
  ELSE IF  $D > 0$ 
     $N = 2$ 
     $x_1 = \frac{-b + \sqrt{D}}{2a}$ 
     $x_2 = \frac{-b - \sqrt{D}}{2a}$ 
  ENDIF
END
```

- ▶ Reasonably formal pseudocode
- ▶ The IF ... ELSE IF flow control construct forces exclusive execution of only *one* block
- ▶ The first condition that is true causes execution of that block
- ▶ Subsequent blocks ignored
- ▶ Contains 3 *conditions*

Boolean Algebra Basics

- ▶ What if we want more complicated conditions?
Boolean algebra is needed!
- ▶ Boolean algebra (or Boolean logic) is a field of mathematics which evaluates combinations of *logical variables* as either true or false
- ▶ Boolean *variables* can only take the values **true** (or 1) or **false** (or 0)
- ▶ Boolean algebra defines three *operators*:
 - ▶ OR
 - ▶ AND
 - ▶ NOT

Boolean Algebra Basics

- ▶ Boolean variables can be allocated any symbols (just like in “normal” algebra)
 - ▶ Typically get uppercase letters
 - ▶ eg: $X = A \text{ OR } B$
- ▶ Various symbols can be used for OR/AND/NOT, we will only use the words here
 - ▶ Write them in capitals to remove ambiguity
 - ▶ C and MATLAB have their own symbols for Boolean algebra
 - ▶ Other courses (eg: ELE17100) will use different symbols again

Boolean Operators

- ▶ An *operand* is a value on which a mathematical operation takes place
 - ▶ eg: In “1 + 2” the 1 and 2 are operands and + is the operator
- ▶ OR - Evaluates true if either operand is true
 - ▶ $X = A \text{ OR } B$
 - ▶ X is true if A or B is true
- ▶ AND- Evaluates true only when *both* operands are true
 - ▶ $X = A \text{ AND } B$
 - ▶ X is true only if both A and B is true

Boolean Operators

- ▶ Observe that OR and AND are *binary* operators
 - ▶ They operate on two operands
 - ▶ From latin “bini” meaning “two together”
- ▶ The NOT operator is *unitary*
 - ▶ ie: it only operates on *one* operand
 - ▶ NB: The operand could be a single variable or complex expression
- ▶ NOT performs a logical inversion
 - ▶ NOT true = false
 - ▶ NOT false = true

Boolean Condition Examples

- ▶ My car needs a service if, since the last service, (more than 6 months has past) OR (more than 15000km have been traveled)
- ▶ You will pass this course if (you score 40% or more in the final exam) AND (the weighted sum of all assessments is more than 50%)
- ▶ A computer program repeats an algorithm if (there is still data to process) AND (errors have not been encountered) AND (NOT (the user has terminated the program))

Algorithm Example 4 - Boolean Conditions

Problem: How can trigonometric functions be calculated by a computer?

One Solution: Series expansion! (Seen in MATH11xx).

The function $\cos(x)$ can be evaluated with arithmetic as:

$$\cos(x) = \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k}}{(2k)!} = \frac{-x^2}{2!} + \frac{x^4}{4!} + \frac{-x^6}{6!} + \frac{x^8}{8!} \dots \quad (3)$$

Evaluation of this series needs two things:

1. The *loop* flow control concept
2. Some kind of *stop condition*

Algorithm Example 4 - Boolean Conditions

- ▶ Computers can't count to infinity, we need to know when to stop
- ▶ Computers have limited precision, around 10^{-16} is typical
- ▶ Observe that as k increases in Equation 4 the denominator increases *really fast* ($4!=24$, $10!=3628800$)
- ▶ This implies that the value of $\frac{(-1)^k x^{2k}}{(2k)!}$ tends to drop as k increases
- ▶ Therefore, we can add terms until they are “too small”
- ▶ A maximum value of k can also be specified for safety

$$\cos(x) = \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k}}{(2k)!} \quad (4)$$

Loops

- ▶ A *loop* causes an algorithm to execute a given block of instruction multiple times
- ▶ Loops typically require an *exit condition*
 - ▶ Without an exit condition they are called *infinite loops*
 - ▶ Yes, these have a purpose
- ▶ Multiple types of loops
 - ▶ WHILE *condition*...ENDWHILE
 - ▶ DO...WHILE *condition*
 - ▶ FOR *counter* FROM 1 TO *something*

Algorithm Example 4 - Boolean Conditions

```
BEGIN
  tmp = 1
  k = 0
  WHILE (k<10) AND (tmp>1e-6)
     $tmp = \frac{(-1)^k x^{2k}}{(2k)!}$ 
    x = x + tmp
    k = k + 1
  ENDWHILE
END
```

- ▶ The *while* loop repeats a block of steps until the *condition* becomes false.
- ▶ We loops until 10 *iterations* have occurred OR a precision limit is reached

C listing template

```
1 #include <stdio.h>
2 int main() {
3     printf("Custom listing template\n");
4 }
```

```
#include <stdio.h>
int main() {
    printf("default C style\n");
}
```

Columns Template

right side

left side

```
brenton@brenton-Lenovo-ideapad-5205-14IKB: /usr/share/hunspell
brenton@brenton-Lenovo-ideapad-5205-14IKB: /usr/share/hunspell 80x24
[99315.136504] usb 1-7: reset full-speed USB device number 3 using xhci_hcd
[99315.221506] ata1: SATA link up 6.0 Gbps (SStatus 133 SControl 300)
[99315.276562] usb 1-5: reset high-speed USB device number 2 using xhci_hcd
[99315.523947] OOM killer enabled.
[99315.523949] Restarting tasks ... done.
[99315.529326] PM: suspend exit
[99316.774373] [drm] RC6 on
[99320.358150] ata1.00: qc timeout (cmd 0xec)
[99320.358172] ata1.00: failed to IDENTIFY (I/O error, err_mask=0x4)
[99320.358178] ata1.00: reset failed (errno=-5)
[99320.678561] ata1: SATA link up 6.0 Gbps (SStatus 133 SControl 300)
[99320.673416] ata1.00: configured for UDMA/133
[99320.845235] IPv6: ADDRCONF(NETDEV_UP): wlp2s0: link is not ready
[99321.595422] IPv6: ADDRCONF(NETDEV_UP): wlp2s0: link is not ready
[99321.644706] IPv6: ADDRCONF(NETDEV_UP): wlp2s0: link is not ready
[99326.549930] wlp2s0: authenticate with 40:9b:cd:28:a3:90
[99326.588140] wlp2s0: send auth to 40:9b:cd:28:a3:90 (try 1/3)
[99326.589777] wlp2s0: authenticated
[99326.591943] wlp2s0: associate with 40:9b:cd:28:a3:90 (try 1/3)
[99326.595543] wlp2s0: RX AssocResp from 40:9b:cd:28:a3:90 (capab=0x431 status=0
aid=1)
[99326.598023] wlp2s0: associated
[99326.605174] IPv6: ADDRCONF(NETDEV_CHANGE): wlp2s0: link becomes ready
brenton@brenton-Lenovo-ideapad-5205-14IKB: /usr/share/hunspell [1]
```