ENGG1003 - Friday Week 1

Algorithms and Pseudocode

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Algorithms

- Informally, an algorithm is a series of steps which accomplishes a task
- More accurately, the steps (instructions) must:
 - Have a strict order
 - Be unambiguous
 - Be executable
- "Executable" means that the target platform is capable of performing that task.
 - eg: An industrial welding robot can execute "move welding tip 1 cm left". A mobile phone can't.



Algorithms

- An algorithm exists purely as an abstract concept until it is communicated
- We will use:
 - Pseudocode to communicate algorithms to ourselves and other people
 - The languages C and MATLAB to communicate algorithms to computers
- Pseudocode can be very formal, but as engineers we will only use formal rules if required
 - eg: When documenting algorithms for other people
 - ► Your own "working out" can be anything that helps you

Algorithm Example 1

Example 1: Algorithm given to mum to start my car (2015 Tarago)

Result: The vehicle's engine is idling

Initialisation: stand next to the vehicle, key fob in hand

- 1. Depress the unlock button on the key fob, car will beep twice
- 2. Place key fob in your pocket
- 3. Enter the vehicle, sit in the driver's seat
- 4. Ensure that the gear selector has P engaged
- 5. Depress the brake pedal
- 6. Observe that the green LED is lit on the engine start button
- 7. Press the engine start button
- 8. If engine is not idling
 - Call me



Example Discussion

- Algorithms typically need to feel over-explained
 - Computers are really stupid; get in the habit of over-thinking everything
- ► The algorithm contained flow control in the form of an "if" statement
 - ► The final step ("call me") was conditional on the car not starting
- We will discuss logical statements later, but first...



Algorithm Example 2

A wife asks her husband, a programmer, "Could you please go shopping for me and buy one carton of milk, and if they have eggs, get 6?"

A short time later the husband comes back with 6 cartons of milk and his wife asks, "Why did you buy 6 cartons of milk?"

He replies, "They had eggs."



Algorithm Example 2a

Lets make this more realistic.

A wife asks her robot helper, "Could you please go shopping for me and buy one carton of milk, and if they have eggs, get 6?"

The robot replies: "Unknown instruction: 'get 6'."

Conditions

- Computers don't understand "maybe"
- A condition must be absolutely true or false
- Human examples:
 - I am within the boundary of the Callaghan campus
 - ► I am alive
 - My net worth is below AU\$100M
- Computer examples:
 - ▶ i is less than 184
 - x plus y is not equal to zero
 - Input data has been given to the program
 - A division by zero occurred



Algorithm Example 3 - Quadratic Root Finding

From high school you should know that the equation

$$ax^2 + bx + c = 0 \tag{1}$$

has solutions given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \tag{2}$$

lets write an algorithm which only deals with real numbers.

Algorithm Example 3 - Quadratic Root Finding

Input: Real numbers a, b, and c

Output: Three numbers:

- 1. The number of solutions, N
- 2. One of the roots, x_1
- 3. The other root, x_2

Behaviour:

- ▶ If N is 2 then x_1 and x_2 are different real numbers
- ▶ If N is 1 then x_1 is the unique solution and x_2 is undefined
- ▶ If N is 0 then x_1 and x_2 are undefined



Algorithm Example 3 - Quadratic Root Finding

BEGIN $D = b^2 - 4ac$ IF D < 0M = 0ELSE IF D = 0N=1 $x_1 = \frac{-b}{2a}$ ELSE IF D > 0N=2 $x_1 = \frac{-b + \sqrt{D}}{2a}$ $x_2 = \frac{-b - \sqrt{D}}{2a}$ ENDIF END

- Reasonably formal pseudocode
- The IF ... ELSE IF flow control construct forces exclusive execution of only one block
- ► The first condition that is true causes execution of that block
- Subsequent blocks ignored
- Contains 3 conditions



Boolean Algebra Basics

- What if we want more complicated conditions? Boolean algebra is needed!
- Boolean algebra (or Boolean logic) is a field of mathematics which evaluates combinations of logical variables as either true or false
- ▶ Boolean variables can only take the values true (or 1) or false (or 0)
- Boolean algebra defines three operators:
 - OR
 - AND
 - NOT



Boolean Algebra Basics

- Boolean variables can be allocated any symbols (just like in "normal" algebra)
 - Typically get upper-case letters
 - ightharpoonup eg: X = A OR B
- Various symbols can be used for OR/AND/NOT, we will only use the words here
 - Write them in capitals to remove ambiguity
 - C and MATLAB have their own symbols for Boolean algebra
 - Other courses (eg: ELE17100) will use different symbols again



Boolean Operators

- An operand is a value on which a mathematical operation takes place
 - ightharpoonup eg: In "1 + 2" the 1 and 2 are operands and + is the operator
- OR Evaluates true if either operand is true
 - \triangleright X = A OR B
 - X is true if A or B is true
- AND- Evaluates true only when both operands are true
 - \triangleright X = A AND B
 - X is true only if both A and B is true



Boolean Operators

- Observe that OR and AND are binary operators
 - They operate on two operands
 - ► From Latin "bini" meaning "two together"
- The NOT operator is unitary
 - ie: it only operates on one operand
 - NB: The operand could be a single variable or complex expression
- NOT performs a logical inversion
 - ▶ NOT true = false
 - ▶ NOT false = true



Boolean Condition Examples

- My car needs a service if, since the last service, (more than 6 months has past) OR (more than 15000km have been travelled)
- ➤ You will pass this course if (you score 40% or more in the final exam) AND (the weighted sum of all assessments is more than 50%)
- ➤ A computer program repeats an algorithm if (there is still data to process) AND (errors have not occurred) AND (NOT (the user has terminated the program))

Algorithm Example 4 - Boolean Conditions

Problem: How can trigonometric functions be calculated by a computer?

One Solution: Series expansion! (Seen in MATH11xx).

The function cos(x) can be evaluated with arithmetic as:

$$\cos(x) = \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k}}{(2k)!} = \frac{-x^2}{2!} + \frac{x^4}{4!} + \frac{-x^6}{6!} + \frac{x^8}{8!}...$$
 (3)

Evaluation of this series needs two things:

- 1. The *loop* flow control concept
- 2. Some kind of stop condition



Algorithm Example 4 - Boolean Conditions

- Computers can't count to infinity, we need to know when to stop
- ightharpoonup Computers have limited precision, around 10^{-16} is typical
- ▶ Observe that as k increases in Equation 4 the denominator increases really fast (4!=24, 10!=3628800)
- ► This implies that the value of $\frac{(-1)^k x^{2k}}{(2k)}!$ tends to drop as k increases
- ▶ Therefore, we can add terms until they are "too small"
- A maximum value of k can also be specified for safety

$$\cos(x) = \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k}}{(2k)!} \tag{4}$$



Loops

- ▶ A loop causes an algorithm to execute a given block of instruction multiple times
- Loops typically require an exit condition
 - Without an exit condition they are called infinite loops
 - Yes, these have a purpose
- Multiple types of loops
 - WHILE condition...ENDWHILE
 - ▶ DO...WHILE condition
 - FOR counter FROM 1 TO something



Algorithm Example 4 - Boolean Conditions

```
BEGIN

tmp = 1

k = 0

WHILE (k<10) AND (tmp>1e-6)

tmp = \frac{(-1)^k x^{2k}}{(2k)!}

x = x + tmp

k = k + 1

ENDWHILE

END
```

- The while loop repeats a block of steps until the condition becomes false.
- We loop until 10 iterations have occurred OR a precision limit is reached