

## Heapsort Big-O Analysis:

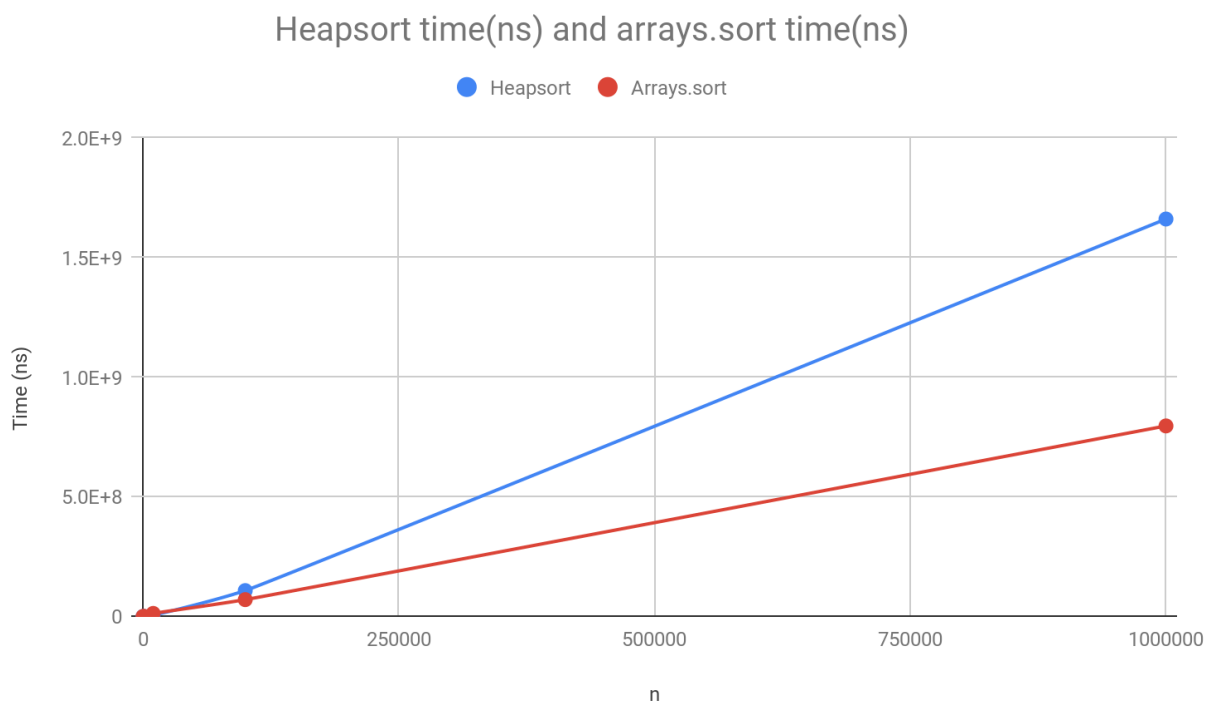
### Methods:

- **Swap** - Time:  $O(1)$  - the swap method simply swaps two elements within the array of people, fairly self explanatory.
- **siftDown** - Time:  $O(\log n)$  - the sift down method performs the sifting operation of the heap. Worst case, this method will visit  $\log(n)$  nodes, one node from each level of the heap. Since the heap is a complete tree, we won't run into bad scenarios with severely unbalanced heaps. All other operations within this method are  $O(1)$ .
- **Heapify** - Time:  $O(n \log n)$  - this method calls the siftDown method  $(n + 2) / 2$  times (simplifies to  $n$  times), so multiplying the complexity of siftDown by  $n$ , we get  $n \log n$ .
- **heapSort** - Time:  $O(n \log n)$  - this method calls heapify once ( $n \log n$ ) and then calls swap and sift down  $n$  times within a loop. The loop will have a runtime of  $n * (\log n + 1)$  which simplifies to  $n \log n$ . The total runtime will be the complexity of heapify plus  $n \log n$ , thus  $O(n \log n) + O(n \log n) = O(2n \log n) = O(n \log n)$ .

**Overall Worst-case Runtime:**  $O(n \log n)$

**Results:**

n	Heapsort time(ns)	arrays.sort time(ns)
100	60053	124499
1000	467656	671154
10000	5343805	12855649
100000	108290634	70444068
1000000	1660660978	796239590

**Comments:**

Both sorts appear to be  $O(n \log n)$ , although the Arrays.sort method seems to be significantly more efficient than my implementation of heapsort.