10 Serie

a) Determinare il carattere delle seguenti serie

$$\sum_{n=1}^{+\infty} \frac{n^2 + 5}{n^4 + 3n^3 - 6n + 2} \tag{58}$$

$$\sum_{n=1}^{+\infty} \frac{1}{\sqrt{n(n+1)}} \tag{59}$$

$$\sum_{n=1}^{+\infty} \left(e^{\frac{1}{n}} - 1 \right) \tag{60}$$

$$\sum_{n=1}^{+\infty} \log \left(1 + \frac{1}{n^{\alpha}} \right) \tag{61}$$

$$\sum_{n=1}^{+\infty} \frac{1}{n \log n} \tag{62}$$

$$\sum_{n=1}^{+\infty} \frac{n!}{n^n} \tag{63}$$

$$\sum_{n=1}^{+\infty} \sin\left(\frac{1}{n^{3\alpha}}\right) n^{\frac{3}{2} - 2\alpha} \tag{64}$$

$$\sum_{n=1}^{+\infty} \frac{4^n}{n^3 (7^{\alpha+2})^n} \tag{65}$$

$$\sum_{n=1}^{+\infty} \left(\cos\frac{1}{n^{\alpha}} - 1\right) n^{1-\alpha} \tag{66}$$

$$\sum_{n=1}^{+\infty} \left(\frac{1}{n} + \sin\frac{1}{n}\right) n^{\alpha} \tag{67}$$

$$\sum_{n=1}^{+\infty} \frac{1 - \cos\frac{b}{n}}{\sin\frac{1}{n^{\alpha}}}, \quad \alpha > 0, \ b \in \mathbb{R}$$
 (68)