

Today

A String Stack ADT

A client: a postfix expression evaluator

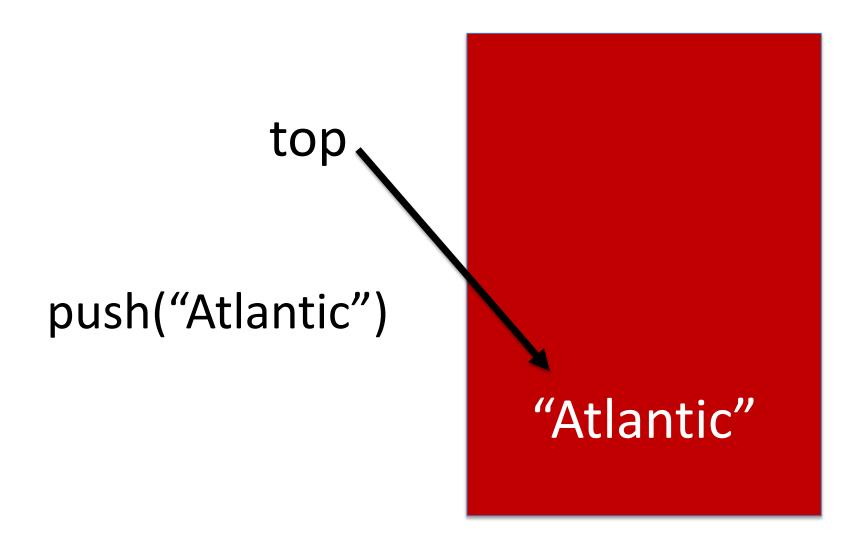
i++ and ++j

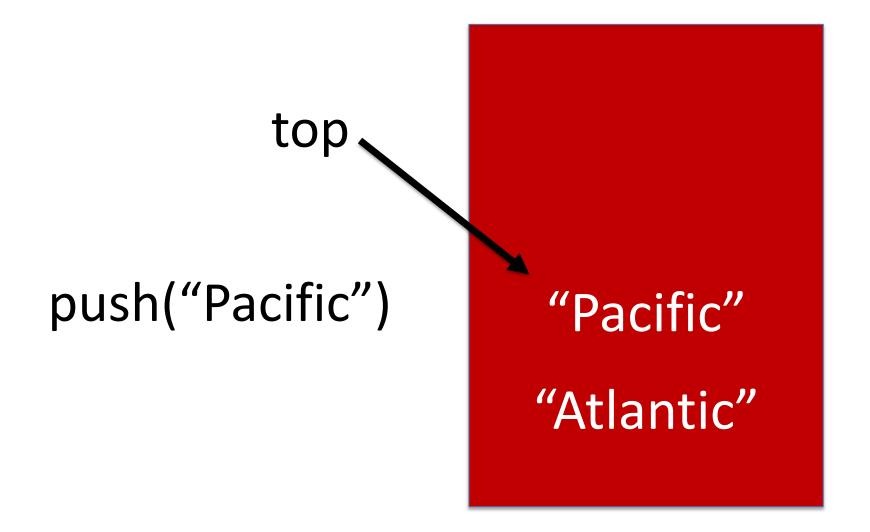
```
12
           int i = 10;
13
14
           int j = 20;
15
           System.out.format("i = %d, j = %d\n", i++, ++j);
16
           System.out.format("i = %d, j = %d\n", i, j);
17
18
           // Prints
19
           // i = 10, j = 21
20
           // i = 11, j = 21
21
```

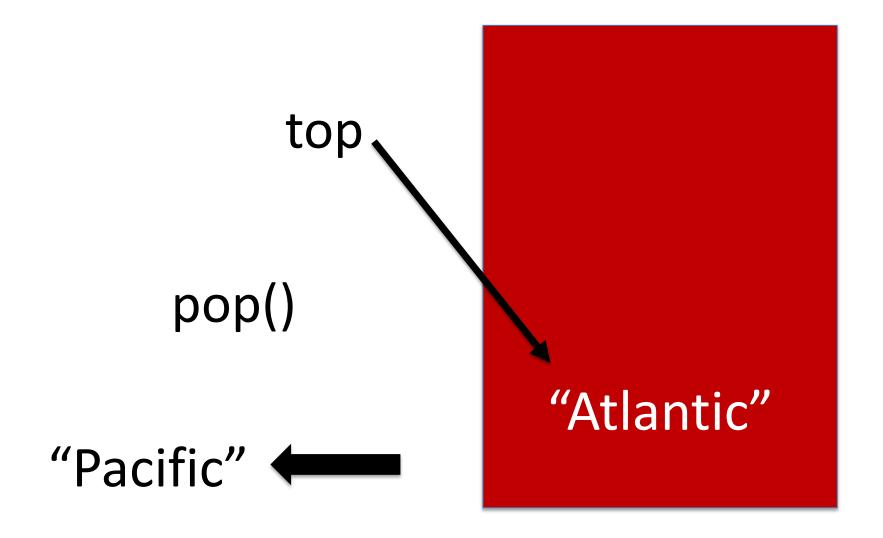


An empty stack









```
// An API for simple stacks of Strings.
       //
       public interface StringStack {
 6
         void push(String s);
 8
         String pop();
10
11
         String peek();
12
13
         boolean isEmpty();
14
15
         String toString();
16
       }
17
```

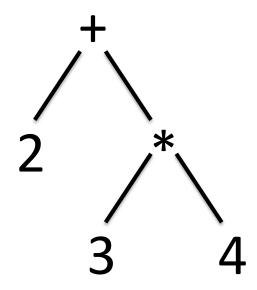
String Stack ADT Code

Postfix Expressions

$$2 + 3 * 4$$

$$2 + (3 * 4)$$

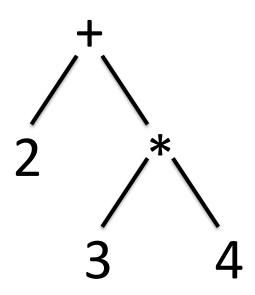
$$2 + (3 * 4)$$



Łukasiewicz (Polish/*prefix*) Notation (1924)

Preorder Traversal:

- 1. Visit the root
- 2. Traverse the left
- 3. Traverse the right

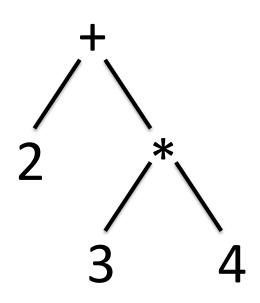


Łukasiewicz (Polish/prefix) Notation

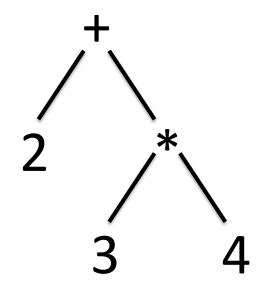
Preorder Traversal:

- 1. Visit the root
- 2. Traverse the left
- 3. Traverse the right

+ 2 * 3 4



The Programming Language LISP uses Polish Notation

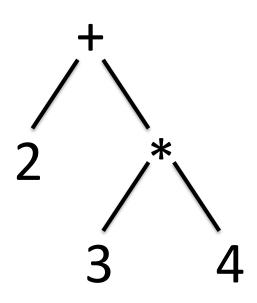


Reverse Polish (postfix) Notation

Postorder Traversal:

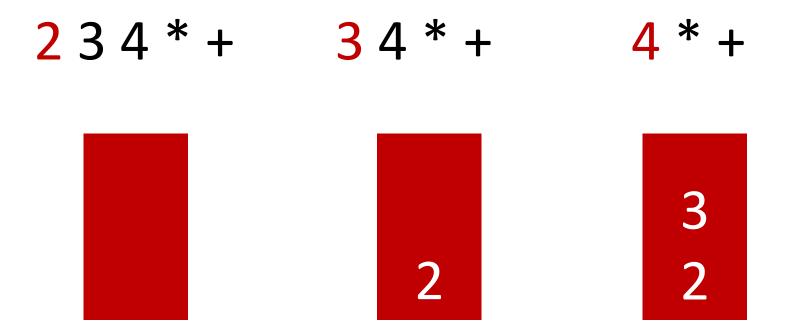
- 1. Traverse the left
- 2. Traverse the right
- 3. Visit the root

2 3 4 * +

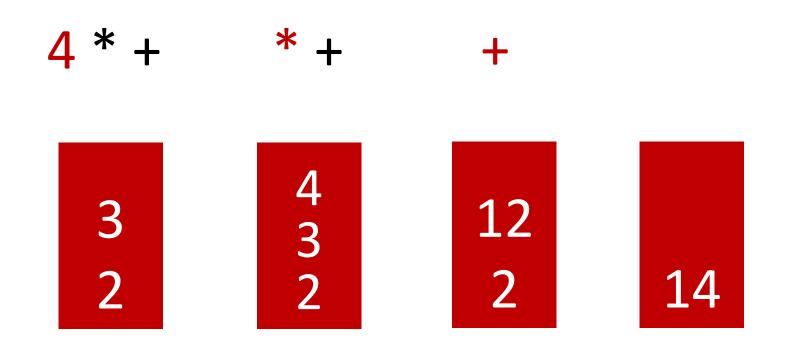


Postfix Notation Evaluation with a Stack

(Burks, Warren & Wright, 1954)



Postfix Notation Evaluation with a Stack



Postfix Evaluation Code