

The original problem is below. We know that $d = r t$ where d is the distance, r is the rate, and t is the time. Let t_1 be the time going and t_2 be the time returning, so we know that $d = 80 t_1$ and $d = 55 t_2$. This means that $80 t_1 = 55 t_2$. We also know that the total time is 45 minutes = $\frac{3}{4}$ hour, which gives $t_1 + t_2 = \frac{3}{4}$ or $t_2 = \frac{3}{4} - t_1$. Substituting t_2 back into the first equation yields $80 t_1 = 55(\frac{3}{4} - t_1)$. Solving this gives $t_1 = \frac{11}{36}$. Finally we know that $d = 80 t_1 = 80 (\frac{11}{36}) = \frac{220}{9} = 24 \frac{4}{9} = 24.4444...$ miles.

Scenic Route

On a vacation trip, Alfred averaged 80 mph traveling from Harrisonburg to Briery Branch. Returning by a different route which covered the same number of miles, he averaged 55 mph. What is the distance between the two "cities" if his total traveling time was 45 min?