

## Longwood Invitational (Fall 2011)

### Problem 3: A Ladder Problem (Contributed by Ben Burrell, Randolph-Macon College)

Suppose that Tom washes windows using a long extension ladder which he can adjust to different heights. For example, he can set the ladder to be forty rungs long -- or only twenty rungs long. Tom uses several different ladders in which the rungs are spaced differently. For instance, on really steep buildings, he might use a ladder on which the rungs are so close together that he can take five or six rungs at a time. However, on some other buildings, he uses a ladder in which the rungs are so far apart he can only take one rung at a time.

Your problem is to determine how many different ways Tom can climb a ladder with  $n$  rungs if each step can take anywhere from 1 to  $m$  rungs. For example, the number of different ways to climb a 5-step ladder where a permitted step can be 1, 2, or 3 rungs (that is,  $n=5$  and  $m=3$ ) is 13 (the possible steps are listed below):

1,1,1,1,1  
1,1,1,2  
1,1,2,1  
1,2,1,1  
2,1,1,1  
1,2,2  
2,1,2  
2,2,1  
1,1,3  
1,3,1  
3,1,1  
2,3  
3,2

#### Input

The input will consist of a series of lines. Each line will contain a pair of values separated by a space. The first value of the pair represents " $n$ ", the number of rungs in the ladder. The second value of the pair represents " $m$ ", the maximum number of rungs Tom can take in a single step. You may assume for each pair of input values that  $1 \leq n \leq 20$  and that  $m \leq n$ .

#### Output

For each line of input you should produce one line of output which contains a single integer. The integer should describe the number of ways in which Tom can climb an  $n$ -rung ladder using only steps of size 1 through  $m$  rungs each.

#### Example

Input:

5 3  
1 1  
10 1  
4 2  
 $n$   $m$

Output:

13  
1  
5

$m=1 \rightarrow n$

(Example continued on back)

$n \geq m$

$1 \leq n \leq 20$

Output:

13  
1  
1  
5

Longwood Institutional (Fall 2011)

Problem 3: A Ladder Problem (Contributed by Dr. Daniel, Stanford-Palo Alto)

Suppose that Tom has a window using a long extension ladder which he can adjust to different heights. For example, he can set the ladder to be four rungs high, or only twenty rungs high. Tom uses various different ladders in which the rungs are spaced differently. For instance, on really steep buildings, he might use a ladder on which the rungs are close together, but he can take five or six rungs at a time. However, on some other buildings, he uses a ladder in which the rungs are so far apart he can only take one rung at a time.

Your problem is to determine how many different ways Tom can climb a ladder with  $n$  rungs if each step can take anywhere from 1 to  $m$  rungs. For example, the number of different ways to climb a 5-step ladder where a permitted step can be 1, 2, or 3 rungs (that is,  $m=3$ ) is 13 (the possible steps are listed below).

1,1,1,1,1  
1,1,1,2  
1,1,2,1  
1,2,1,1  
2,1,1,1  
1,2,2  
2,1,2  
2,2,1  
1,3,1  
1,1,3  
3,1,1  
1,4  
4,1

Input

The input will consist of a series of lines. Each line will contain a pair of values separated by a space. The first value of the pair represents  $n$ , the number of rungs in the ladder. The second value of the pair represents  $m$ , the maximum number of rungs Tom can take in a single step. You may assume for each pair of input values that  $1 \leq n \leq 10$  and that  $m \geq 1$ .

Output

For each line of input you should produce one line of output which contains a single integer. The integer should be the number of ways in which Tom can climb the rungs rather than any steps of size 1 through  $m$  rungs each.

Example

Input  
5 3  
10 2  
10 1

(Example continued on back)