Optimal Control for Robotics - Course Syllabus

Tufts University - Mechanical Engineering Spring 2018

Personnel and Office Hours

Instructor: Matthew Kelly

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Course Website: https://github.com/MatthewPeterKelly/ME149_Spring2018

Office Hours:

• 30 minutes before each class and up to 60 minutes following each class

• students are encouraged to attend at least 20 minutes of office hours per week

Course Information

- Description: Students taking this course will learn the basics of optimal control for robotics applications. There will be a strong focus on trajectory optimization and trajectory-tracking controllers, and assignments will focus on applications and implementation, rather than on theory. In the first part of the course students will learn the core concepts of optimal control: programming, simulation, control, and optimization. In the second part of the course the students will put these concepts together to design and stabilize reference trajectories in simulation. The topics covered in this course are used in a variety of applications, including aircraft, satellites, robot arms, legged robots, quad-rotor helicopters.
- Goals: Upon completing this course, students should:
 - understand the major concepts in optimal control, especially trajectory optimization
 - develop strong programming skills in Matlab
 - be able to implement their own trajectory optimization, design a trajectory-stabilizing controller,
 and simulate a closed-loop dynamic system as it tracks a trajectory.
- Recommended: ME80 or ME180

General Policies

- Scheduling Conflicts: If you have a conflict with the midterm exam, final project, or a homework assignment, then you must notify the instructure at least two weeks in advance.
- *Honor Policy:* Your work should be your own. Cite any help that you receive or resources that you use. Do not directly copy code from other students or elsewhere.
- Style: All work must be clear and legible. Code should be well documented and follow the style guide. All plots should be fully annotated with axis labels, title, and a legend if appropriate.

Course Grading

• Homework assignments: 40%

Midterm exam: 25%Final project: 35%

Homework Policies

Homework schedule:

- Assigned weekly on Tuesday (usually see schedule)
- Due on the following Thursday at 6pm (nine days to complete assignment)
- Graded and returned on the following Tuesday (five day turn-around)

Homework grading:

- Each assignment is worth 50 points
- The assignment with the lowest score will be dropped from final grade
- Late homework: up to two weeks late: -20 points, otherwise -40 points
- You will lose points if your work is not clear, even if your answer is correct

Team work:

- All assignments must be submitted individually
- Students are encouraged to help each other work through assignments
- Directly copying code from other students is prohibited
- In the write-up for each assignment (including the final project), you must list the names of any other students that you worked with, as well as any external resources that you used.

Useful Resources

Matlab Style guide: (.pdf)

https://www.mathworks.com/matlabcentral/fileexchange/46056-matlab-style-guidelines-2-0

Textbook: (primary text for the course)

Practical Methods for Optimal Control and Estimation Using Nonlinear Programming

- John T. Betts, SIAM, Second Edition.

Textbook: (additional reading)

 $Applied\ Optimal\ Control:\ Optimization,\ Estimation,\ and\ Control$

- Arthur E. Bryson Jr. and Yu-Chi Ho

Online Course: (60% overlap with this course)

 $MIT\ Open\ Courseware:\ Under actuated\ Robotics.$

- Russ Tedrake (and others), two versions, both are good.

Lectures

(table on following page)

| Date | HW | Topic |
|---------------------------|--------------------------------------|---|
| R - Jan 18 | $1 \rightarrow$ | Intro to optimal control: major concepts and applications. Intro to Matlab. |
| T - Jan 23 | $2 \rightarrow$ | Intro to simulation: Euler's method. Matlab best practices. |
| R - Jan 25 | 1 ↓ | Midpoint and Heun's Method; Simulation analysis and stability. |
| T - Jan 30 | $3 \rightarrow$ | Runge-Kutta methods and ode45(). |
| R - Feb 1 | 2 ↓ | Introduction to SISO control. |
| ${\bf T}$ - Feb ${\bf 6}$ | $4 \rightarrow$ | Trajectory-tracking control for SISO systems |
| ${\bf R}$ - Feb 8 | 3 ↓ | Control basics for MIMO systems: state space, linear control; 3 Dof planar arm simulation |
| ${\bf T}$ - Feb 13 | $5 \rightarrow$ | Trajectory-tracking for MIMO systems; Working overview of LQR; underactuated systems |
| R - Feb 15 | 4 ↓ | Scalar optimization and root-finding part one |
| ${\rm T}$ - Feb 20 | $6 \rightarrow$ | Scalar optimization and root-finding part two |
| ${\bf R}$ - Feb 22 | | No Class – Monday schedule on Thursday |
| ${\bf T}$ - Feb 27 | 5 ↓ | Constrained optimization part one |
| R - Mar 1 | $7 \rightarrow$ | Constrained optimization part two |
| T - Mar 6 | 8 → | Intro to optimal control: policy vs trajectory optimization, applications |
| R - Mar 8 | 7 ↓ | Single shooting; root finding; simplest walker example; cannon example |
| T - Mar 13 | 8 ↓ | Review for Midterm Exam |
| R - Mar 15 | | In-class Midterm Exam |
| T - Mar 20 | | No Class – Spring Recess |
| R - Mar 22 | | No Class – Spring Recess |
| T - Mar 27 | 9 → | Single shooting revisited |
| R - Mar 29 | | Multiple shooting part one |
| T - Apr 3 | $10 \rightarrow$ | Multiple shooting part two |
| R - Apr 5 | $9 \downarrow \text{F1} \rightarrow$ | Final Project Overview |
| T - Apr 10 | | Direct collocation part one |
| R - Apr 12 | 10 ↓ | Direct collocation part two |
| T - Apr 17 | $F2 \rightarrow$ | Advanced topic: TBD (analytic gradients?) |
| R - Apr 19 | F1 ↓ | Special topic: TBD (guest lecture?) |
| T - Apr 24 | | Trajectory optimization in the real world; In-class office hours for final project |
| R - Apr 26 | F2 ↓ | In-class presentations and discussion |
| T - May 1 | | No Class – Reading Period |