2017 AMC 10B Problems

Instructions

1. This is a 25-question, multiple choice test. Each question is followed by answers marked A, B, C, D and E. Only one of these is correct.
2. You will receive 6 points for each correct answer, 2.5 points for each problem left unanswered if the year is before 2006, 1.5 points for each problem left unanswered if the year is after 2006, and 0 points for each incorrect answer.
3. No aids are permitted other than scratch paper, graph paper, ruler, compass, protractor and erasers (and calculators that are accepted for use on the SAT if before 2006. No problems on the test will *require* the use of a calculator).
4. Figures are not necessarily drawn to scale.
5. You will have **75 minutes** working time to complete the test.

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Problem 1

Mary thought of a positive two-digit number. She multiplied it by 3 and added 11. Then she switched the digits of the result, obtaining a number between 71 and 75, inclusive. What was Mary's number?

(A) 11 **(B)** 12 **(C)** 13 **(D)** 14 **(E)** 15

Solution

Problem 2

Sofia ran 5 laps around the 400-meter track at her school. For each lap, she ran the first 100 meters at an average speed of 4 meters per second and the remaining 300 meters at an average speed of 5 meters per second. How much time did Sofia take running the 5 laps?

(A) 5 minutes and 35 seconds **(B)** 6 minutes and 40 seconds **(C)** 7 minutes and 5 seconds **(D)** 7 minutes and 25 seconds **(E)** 8 minutes and 10 seconds

Solution

Problem 3

Real numbers x, y, and z satisfy the inequalities $0 < x < 1$, $-1 < y < 0$, and $1 < z < 2$. Which of the following numbers is necessarily positive?

(A) $y + x^2$ **(B)** $y + xz$ **(C)** $y + y^2$ **(D)** $y + 2y^2$ **(E)** $y + z$

Solution

Problem 4

Suppose that x and y are nonzero real numbers such that $\dfrac{3x + y}{x - 3y} = -2$. What is the value of $\dfrac{x + 3y}{3x - y}$?

(A) -3 **(B)** -1 **(C)** 1 **(D)** 2 **(E)** 3

Solution

Problem 5

Camilla had twice as many blueberry jelly beans as cherry jelly beans. After eating 10 pieces of each kind, she now has three times as many blueberry jelly beans as cherry jelly beans. How many blueberry jelly beans did she originally have?

(A) 10 **(B)** 20 **(C)** 30 **(D)** 40 **(E)** 50

Solution

Problem 6

What is the largest number of solid 2 in. by 2 in. by 1 in. blocks that can fit in a 3 in. by 2 in. by 3 in. box?

(A) 3 **(B)** 4 **(C)** 5 **(D)** 6 **(E)** 7

Solution

Problem 7

Samia set off on her bicycle to visit her friend, traveling at an average speed of 17 kilometers per hour. When she had gone half the distance to her friend's house, a tire went flat, and she walked the rest of the way at 5 kilometers per hour. In all it took her 44 minutes to reach her friend's house. In kilometers rounded to the nearest tenth, how far did Samia walk?

(A) 2.0 **(B)** 2.2 **(C)** 2.8 **(D)** 3.4 **(E)** 4.4

Solution

Problem 8

Points $A(11, 9)$ and $B(2, -3)$ are vertices of $\triangle ABC$ with $AB = AC$. The altitude from A meets the opposite side at $D(-1, 3)$. What are the coordinates of point C?

(A) $(-8, 9)$ **(B)** $(-4, 8)$ **(C)** $(-4, 9)$ **(D)** $(-2, 3)$ **(E)** $(-1, 0)$

Solution

Problem 9

A radio program has a quiz consisting of 3 multiple-choice questions, each with 3 choices. A contestant wins if he or she gets 2 or more of the questions right. The contestant answers randomly to each question. What is the probability of winning?

(A) $\dfrac{1}{27}$ **(B)** $\dfrac{1}{9}$ **(C)** $\dfrac{2}{9}$ **(D)** $\dfrac{7}{27}$ **(E)** $\dfrac{1}{2}$

Solution

Problem 10

The lines with equations $ax - 2y = c$ and $2x + by = -c$ are perpendicular and intersect at $(1, -5)$. What is c?

(A) -13 **(B)** -8 **(C)** 2 **(D)** 8 **(E)** 13

Solution

Problem 11

At Typico High School, 60% of the students like dancing, and the rest dislike it. Of those who like dancing, 80% say that they like it, and the rest say that they dislike it. Of those who dislike dancing, 90% say that they dislike it, and the rest say that they like it. What fraction of students who say they dislike dancing actually like it?

(A) 10% **(B)** 12% **(C)** 20% **(D)** 25% **(E)** $33\dfrac{1}{3}\%$

Solution

Problem 12

Elmer's new car gives 50% better fuel efficiency. However, the new car uses diesel fuel, which is 20% more expensive per liter than the gasoline the old car used. By what percent will Elmer save money if he uses his new car instead of his old car for a long trip?

(A) 20% **(B)** $26\frac{2}{3}\%$ **(C)** $27\frac{7}{9}\%$ **(D)** $33\frac{1}{3}\%$ **(E)** $66\frac{2}{3}\%$

Solution

Problem 13

There are 20 students participating in an after-school program offering classes in yoga, bridge, and painting. Each student must take at least one of these three classes, but may take two or all three. There are 10 students taking yoga, 13 taking bridge, and 9 taking painting. There are 9 students taking at least two classes. How many students are taking all three classes?

(A) 1 **(B)** 2 **(C)** 3 **(D)** 4 **(E)** 5

Solution

Problem 14

An integer N is selected at random in the range $1 \leq N \leq 2020$. What is the probability that the remainder when N^{16} is divided by 5 is 1?

(A) $\dfrac{1}{5}$ **(B)** $\dfrac{2}{5}$ **(C)** $\dfrac{3}{5}$ **(D)** $\dfrac{4}{5}$ **(E)** 1

Solution

Problem 15

Rectangle $ABCD$ has $AB = 3$ and $BC = 4$. Point E is the foot of the perpendicular from B to diagonal $\overline{AC}$. What is the area of $\triangle AED$?

(A) 1 (B) $\dfrac{42}{25}$ (C) $\dfrac{28}{15}$ (D) 2 (E) $\dfrac{54}{25}$

Solution

Problem 16

How many of the base-ten numerals for the positive integers less than or equal to 2017 contain the digit 0?

(A) 469 (B) 471 (C) 475 (D) 478 (E) 481
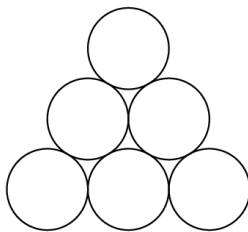
Solution

Problem 17

Call a positive integer *monotonous* if it is a one-digit number or its digits, when read from left to right, form either a strictly increasing or a strictly decreasing sequence. For example, 3, 23578, and 987620 are monotonous, but 88, 7434, and 23557 are not. How many monotonous positive integers are there?

(A) 1024 (B) 1524 (C) 1533 (D) 1536 (E) 2048

Solution

Problem 18

In the figure below, 3 of the 6 disks are to be painted blue, 2 are to be painted red, and 1 is to be painted green. Two paintings that can be obtained from one another by a rotation or a reflection of the entire figure are considered the same. How many different paintings are possible?

(A) 6 (B) 8 (C) 9 (D) 12 (E) 15

Solution

Problem 19

Let ABC be an equilateral triangle. Extend side $\overline{AB}$ beyond B to a point B' so that $BB' = 3AB$. Similarly, extend side $\overline{BC}$ beyond C to a point C' so that $CC' = 3BC$, and extend side $\overline{CA}$ beyond A to a point A' so that $AA' = 3CA$. What is the ratio of the area of $\triangle A'B'C'$ to the area of $\triangle ABC$?

(A) $9 : 1$ (B) $16 : 1$ (C) $25 : 1$ (D) $36 : 1$ (E) $37 : 1$

Solution

Problem 20

The number $21! = 51,090,942,171,709,440,000$ has over $60,000$ positive integer divisors. One of them is chosen at random. What is the probability that it is odd?

(A) $\dfrac{1}{21}$ (B) $\dfrac{1}{19}$ (C) $\dfrac{1}{18}$ (D) $\dfrac{1}{2}$ (E) $\dfrac{11}{21}$

Solution

Problem 21

In $\triangle ABC$, $AB = 6$, $AC = 8$, $BC = 10$, and D is the midpoint of $\overline{BC}$. What is the sum of the radii of the circles inscribed in $\triangle ADB$ and $\triangle ADC$?

(A) $\sqrt{5}$ (B) $\dfrac{11}{4}$ (C) $2\sqrt{2}$ (D) $\dfrac{17}{6}$ (E) 3

Solution

Problem 22

The diameter AB of a circle of radius 2 is extended to a point D outside the circle so that $BD = 3$. Point E is chosen so that $ED = 5$ and line ED is perpendicular to line AD. Segment AE intersects the circle at a point C between A and E. What is the area of $\triangle ABC$?

(A) $\dfrac{120}{37}$ (B) $\dfrac{140}{39}$ (C) $\dfrac{145}{39}$ (D) $\dfrac{140}{37}$ (E) $\dfrac{120}{31}$

Solution

Problem 23

Let $N = 123456789101112\ldots 4344$ be the 79-digit number that is formed by writing the integers from 1 to 44 in order, one after the other. What is the remainder when N is divided by 45?

(A) 1 (B) 4 (C) 9 (D) 18 (E) 44

Solution

Problem 24

The vertices of an equilateral triangle lie on the hyperbola $xy = 1$, and a vertex of this hyperbola is the centroid of the triangle. What is the square of the area of the triangle?

(A) 48 **(B)** 60 **(C)** 108 **(D)** 120 **(E)** 169

Solution

Problem 25

Last year Isabella took 7 math tests and received 7 different scores, each an integer between 91 and 100, inclusive. After each test she noticed that the average of her test scores was an integer. Her score on the seventh test was 95. What was her score on the sixth test?

(A) 92 **(B)** 94 **(C)** 96 **(D)** 98 **(E)** 100

Solution

See also

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