

CAPE1330

Energy Balances

Nonreactive Processes

General procedures:

1. **Perform** all the required materials balance calculations
2. **Use** the appropriate form of the energy balances
closed system: $Q + W = \Delta U + \Delta E_k + \Delta E_p$
open system: $\dot{Q} + \dot{W}_s = \Delta \dot{H} + \Delta \dot{E}_k + \Delta \dot{E}_p$
3. **Choose** a reference state (phase, temperature, and pressure) for each species involved in the process
4. **Calculate** all the required values of \hat{U}_i or \hat{H}_i
5. **Solve** the energy balances for unknown variables

1. Heat Capacity of a Mixture

Calculate the heat required to bring 150 mol/h of a stream containing 60% C_2H_6 and 40% C_3H_8 by volume from 0°C to 400°C . Determine a heat capacity for the mixture as part of the problem solution.

2. Waste-Heat Boiler

A gas stream at 500°C containing 8 mol% CO and 92 mol% CO_2 that was originally going to be sent up a stack is instead sent to a heat exchanger and flows across tubes through which water is flowing.

The water enters at 25°C and is fed at a ratio of 0.2 mol water/mol hot gas, is heated to its boiling point, and forms saturated steam at 5 bar. The steam may be used for heating or power generation in the plant or as the feed to another process unit. The heat exchanger can be assumed to operate adiabatically - that is, all heat transferred from the hot gas goes to heat the water.

The flowchart for an assumed basis of 1 mol feed gas is shown below. Calculate the temperature of the gas leaving the heat exchanger.

2. Waste-Heat Boiler

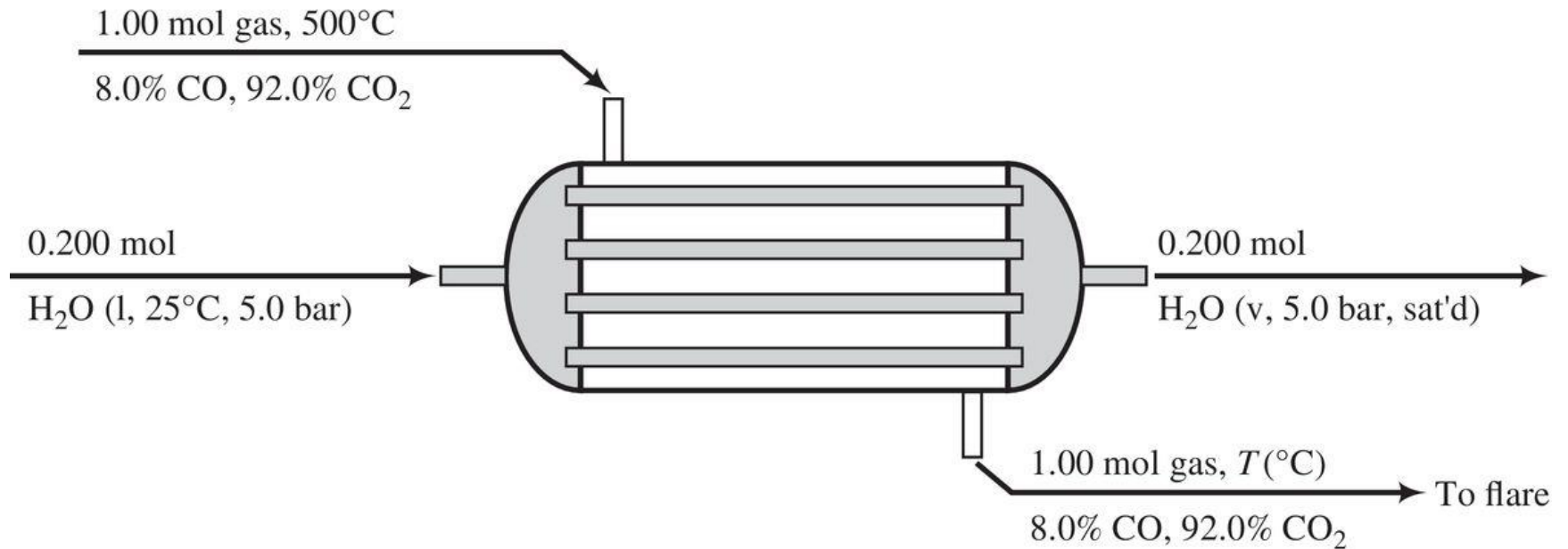


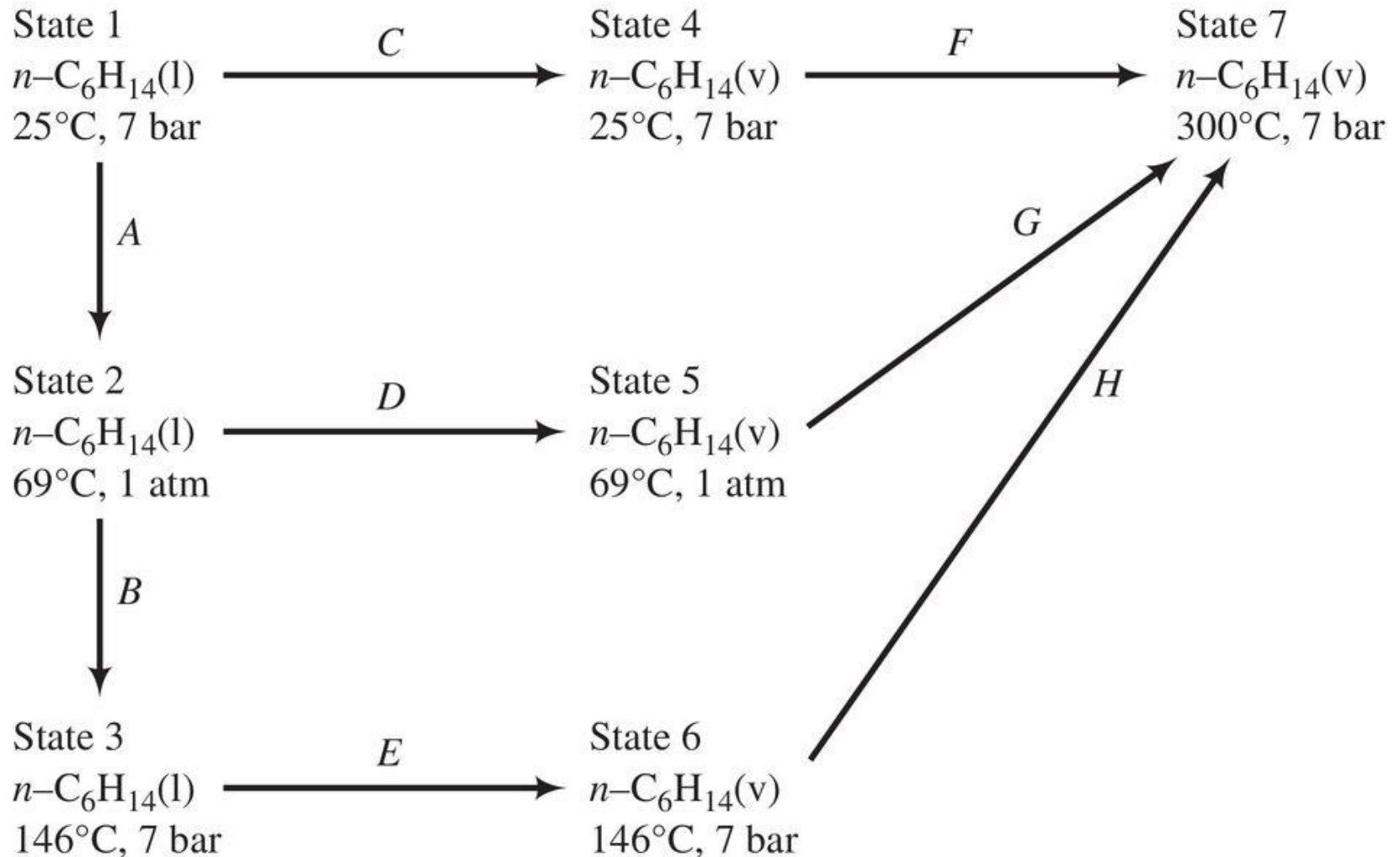
Table B.5 Saturated Steam

$T(^{\circ}\text{C})$	$P(\text{bar})$	$\hat{V}(\text{m}^3/\text{kg})$		$\hat{U}(\text{kJ/kg})$		$\hat{H}(\text{kJ/kg})$		
		Water	Steam	Water	Steam	Water	Evaporation	Steam
70	0.3117	0.001023	5.045	293.0	2469	293.0	2333	2626
72	0.3396	0.001024	4.655	301.4	2472	301.4	2329	2630
74	0.3696	0.001025	4.299	309.8	2474	309.8	2323	2633
76	0.4019	0.001026	3.975	318.2	2476	318.2	2318	2636
78	0.4365	0.001028	3.679	326.4	2479	326.4	2313	2639
80	0.4736	0.001029	3.408	334.8	2482	334.9	2308	2643
82	0.5133	0.001030	3.161	343.2	2484	343.3	2303	2646
84	0.5558	0.001032	2.934	351.6	2487	351.7	2298	2650
86	0.6011	0.001033	2.727	360.0	2489	360.1	2293	2653
88	0.6495	0.001034	2.536	368.4	2491	368.5	2288	2656
90	0.7011	0.001036	2.361	376.9	2493	377.0	2282	2659
92	0.7560	0.001037	2.200	385.3	2496	385.4	2277	2662
94	0.8145	0.001039	2.052	393.7	2499	393.8	2272	2666
96	0.8767	0.001040	1.915	402.1	2501	402.2	2267	2669
98	0.9429	0.001042	1.789	410.6	2504	410.7	2262	2673
100	1.0131	0.001044	1.673	419.0	2507	419.1	2257	2676
102	1.0876	0.001045	1.566	427.1	2509	427.5	2251	2679

3. Vaporisation and Heating

One hundred g-moles per hour of liquid n-hexane at 25°C and 7 bar is vaporised and heated to 300°C at constant pressure. Neglecting the effect of pressure on enthalpy, estimate the rate at which heat must be supplied.

3. Vaporisation and Heating



3. Vaporisation and Heating

Compound	Formula	Mol. Wt.	SG (20°/4°)	$T_m(^{\circ}\text{C})^b$	$\Delta\hat{H}_m(T_m)^{c,j}$ kJ/mol	$T_b(^{\circ}\text{C})^d$	$\Delta\hat{H}_v(T_b)^{e,j}$ kJ/mol	$T_c(\text{K})^f$	$P_c(\text{atm})^g$	$(\Delta\hat{H}_f^{\circ})^{h,j}$ kJ/mol	$(\Delta\hat{H}_c^{\circ})^{i,j}$ kJ/mol
<i>n</i> -Heptane	C ₇ H ₁₆	100.20	0.684	−90.59	14.03	98.43	31.69	540.2	27.0	−224.4(l) −187.8(g)	−4816.9(l) −4853.5(g)
<i>n</i> -Hexane	C ₆ H ₁₄	86.17	0.659	−95.32	13.03	68.74	28.85	507.9	29.9	−198.8(l) −167.2(g)	−4163.1(l) −4194.8(g)
Hydrogen	H ₂	2.016	—	−259.19	0.12	−252.76	0.904	33.3	12.8	0(g)	−285.84(g)
Hydrogen bromide	HBr	80.92	—	−86	—	−67	—	—	—	−36.23(g)	—
Hydrogen chloride	HCl	36.47	—	−114.2	1.99	−85.0	16.1	324.6	81.5	−92.31(g)	—
Hydrogen cyanide	HCN	27.03	—	−14	—	26	—	—	—	+130.54(g)	—
Hydrogen fluoride	HF	20.0	—	−83	—	20	—	503.2	—	−268.6(g) −316.9(aq, 200)	—
Hydrogen sulfide	H ₂ S	34.08	—	−85.5	2.38	−60.3	18.67	373.6	88.9	−19.96(g)	−562.59(g)
Iodine	I ₂	253.8	4.93	113.3	—	184.2	—	826.0	—	0(c)	—
Iron	Fe	55.85	7.7	1535	15.1	2800	354.0	—	—	0(c)	—
Lead	Pb	207.21	11.337 ^{20°/20°}	327.4	5.10	1750	179.9	—	—	0(c)	—
Lead oxide	PbO	223.21	9.5	886	11.7	1472	213	—	—	−219.2(c)	—
Magnesium	Mg	24.32	1.74	650	9.2	1120	131.8	—	—	0(c)	—
Magnesium chloride	MgCl ₂	95.23	2.325 ^{25°}	714	43.1	1418	136.8	—	—	−641.8(c)	—
Magnesium hydroxide	Mg(OH) ₂	58.34	2.4	Decomposes at 350°C				—	—	—	—
Magnesium oxide	MgO	40.32	3.65	2900	77.4	3600	—	—	—	−601.8(c)	—
Mercury	Hg	200.61	13.546	−38.87	—	−356.9	—	—	—	0(c)	—
Methane	CH ₄	16.04	—	−182.5	0.94	−161.5	8.179	190.70	45.8	−74.85(g)	−890.36(g)

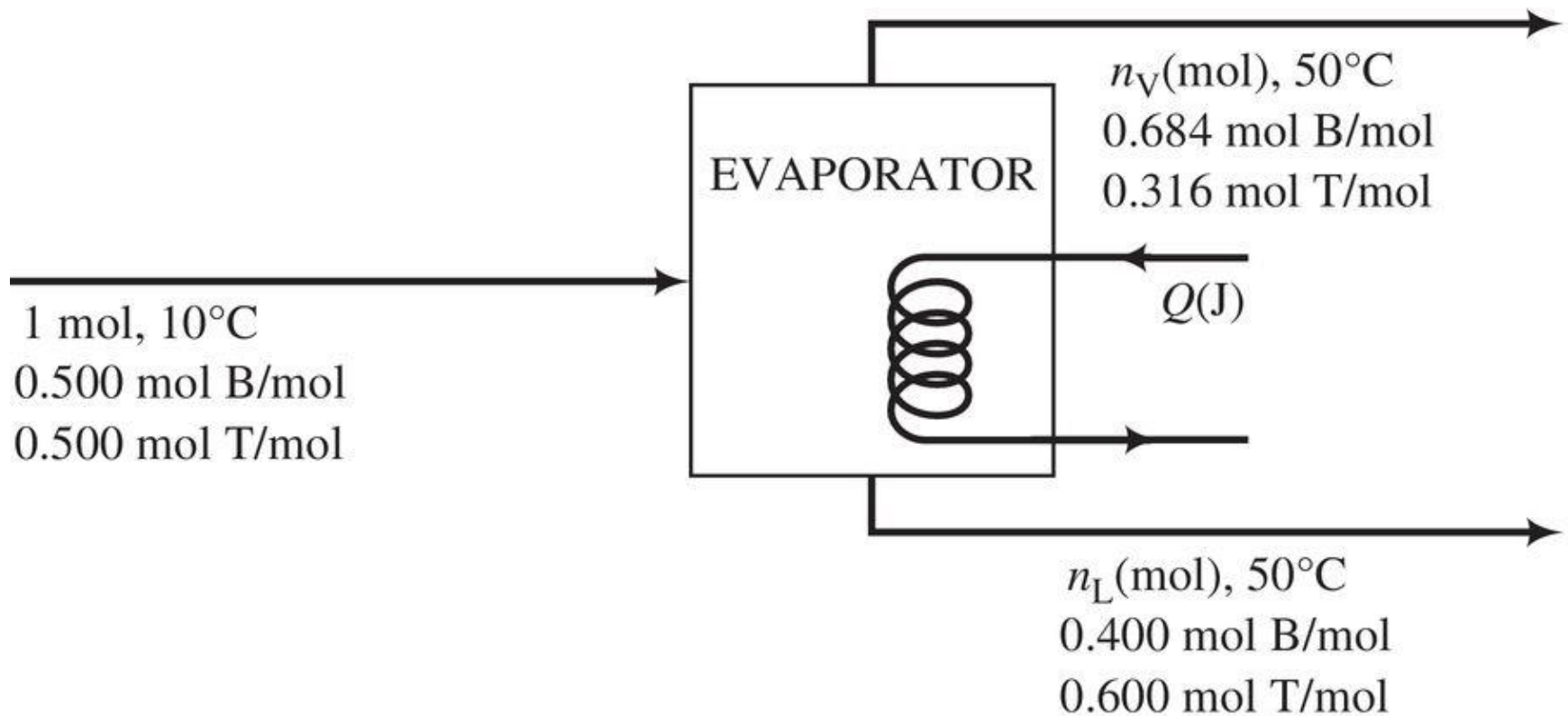
3. Vaporisation and Heating

Compound	Formula	Mol. Wt.	State	Form	Temp. Unit	$a \times 10^3$	$b \times 10^5$	$c \times 10^8$	$d \times 10^{12}$	Range (Units of T)
Cumene (Isopropyl benzene)	C ₉ H ₁₂	120.19	g	1	°C	139.2	53.76	−39.79	120.5	0–1200
Cyclohexane	C ₆ H ₁₂	84.16	g	1	°C	94.140	49.62	−31.90	80.63	0–1200
Cyclopentane	C ₅ H ₁₀	70.13	g	1	°C	73.39	39.28	−25.54	68.66	0–1200
Ethane	C ₂ H ₆	30.07	g	1	°C	49.37	13.92	−5.816	7.280	0–1200
Ethyl alcohol (Ethanol)	C ₂ H ₅ OH	46.07	l	1	°C	103.1				0
			l	1	°C	158.8				100
			g	1	°C	61.34	15.72	−8.749	19.83	0–1200
Ethylene	C ₂ H ₄	28.05	g	1	°C	+40.75	11.47	−6.891	17.66	0–1200
Ferric oxide	Fe ₂ O ₃	159.70	c	2	K	103.4	6.711	−17.72 × 10 ¹⁰	—	273–1097
Formaldehyde	CH ₂ O	30.03	g	1	°C	34.28	4.268	0.0000	−8.694	0–1200
Helium	He	4.00	g	1	°C	20.8				0–1200
<i>n</i> -Hexane	C ₆ H ₁₄	86.17	l	1	°C	216.3				20–100
			g	1	°C	137.44	40.85	−23.92	57.66	0–1200
Hydrogen	H ₂	2.016	g	1	°C	28.84	0.00765	0.3288	−0.8698	0–1500
Hydrogen bromide	HBr	80.92	g	1	°C	29.10	−0.0227	0.9887	−4.858	0–1200
Hydrogen chloride	HCl	36.47	g	1	°C	29.13	−0.1341	0.9715	−4.335	0–1200
Hydrogen cyanide	HCN	27.03	g	1	°C	35.3	2.908	1.092		0–1200
Hydrogen sulfide	H ₂ S	34.08	g	1	°C	33.51	1.547	0.3012	−3.292	0–1500
Magnesium chloride	MgCl ₂	95.23	c	1	K	72.4	1.58			273–991
Magnesium oxide	MgO	40.32	c	2	K	45.44	0.5008	−8.732 × 10 ¹⁰		273–2073
Methane	CH ₄	16.04	g	1	°C	34.31	5.469	0.3661	−11.00	0–1200
			g	1	K	19.87	5.021	1.268	−11.00	273–1500
Methyl alcohol	CH ₃ OH	32.04	l	1	°C	75.86	16.83			0–65

4. Partial Vaporization

An equimolar liquid mixture of benzene (B) and toluene (T) at 10°C is fed continuously to a vessel in which the mixture is heated to 50°C . The liquid product is 40.0 mole% B, and the vapor product is 68.4 mole% B. How much heat must be transferred to the mixture per mole of feed?

4. Partial Vaporization



4. Partial Vaporization

References: B(l, 10°C, 1 atm), T(l, 10°C, 1 atm)

Substance	n_{in} mol	\hat{H}_{in} (kJ/mol)	n_{out} (mol)	\hat{H}_{out} (kJ/mol)
B(l)	0.500	0	0.259	\hat{H}_1
T(l)	0.500	0	0.389	\hat{H}_2
B(v)	—	—	0.241	\hat{H}_3
T(v)	—	—	0.111	\hat{H}_4

4. Partial Vaporization

Compound	Formula	Mol. Wt.	SG (20°/4°)	$T_m(^{\circ}\text{C})^b$	$\Delta\hat{H}_m(T_m)^{c,j}$ kJ/mol	$T_b(^{\circ}\text{C})^d$	$\Delta\hat{H}_v(T_b)^{e,j}$ kJ/mol	$T_c(\text{K})^f$	$P_c(\text{atm})^g$	$(\Delta\hat{H}_f^{\circ})^{h,j}$ kJ/mol	$(\Delta\hat{H}_c^{\circ})^{i,j}$ kJ/mol
Acetaldehyde	CH ₃ CHO	44.05	0.783 ^{18°}	-123.7	—	20.2	25.1	461.0	—	-166.2(g)	-1192.4(g)
Acetic acid	CH ₃ COOH	60.05	1.049	16.6	12.09	118.2	24.39	594.8	57.1	-486.18(l) -438.15(g)	-871.69(l) -919.73(g)
Acetone	C ₃ H ₆ O	58.08	0.791	-95.0	5.69	56.0	30.2	508.0	47.0	-248.2(l) -216.7(g)	-1785.7(l) -1821.4(g)
Acetylene	C ₂ H ₂	26.04	—	—	—	-81.5	17.6	309.5	61.6	+226.75(g)	-1299.6(g)
Ammonia	NH ₃	17.03	—	-77.8	5.653	-33.43	23.351	405.5	111.3	-67.20(l) -46.19(g)	-382.58(g)
Ammonium hydroxide	NH ₄ OH	35.03	—	—	—	—	—	—	—	-366.48(aq)	—
Ammonium nitrate	NH ₄ NO ₃	80.05	1.725 ^{25°}	169.6	5.4	Decomposes at 210°C				-365.14(c) -399.36(aq)	—
Ammonium sulfate	(NH ₄) ₂ SO ₄	132.14	1.769	513	—	Decomposes at 513°C after melting				-1179.3(c) -1173.1(aq)	—
Aniline	C ₆ H ₇ N	93.12	1.022	-6.3	—	184.2	—	699	52.4	—	—
Benzaldehyde	C ₆ H ₅ CHO	106.12	1.046	-26.0	—	179.0	38.40	—	—	-88.83(l) -40.04(g)	-3520.0(l) —
Benzene	C ₆ H ₆	78.11	0.879	5.53	9.837	80.10	30.765	562.6	48.6	+48.66(l) +82.93(g)	-3267.6(l) -3301.5(g)
Benzoic acid	C ₇ H ₆ O ₂	122.12	1.266 ^{15°}	122.2	—	249.8	—	—	—	—	-3226.7(g)
Benzyl alcohol	C ₇ H ₈ O	108.13	1.045	-15.4	—	205.2	—	—	—	—	-3741.8(l)
Bromine	Br ₂	159.83	3.119	-7.4	10.8	58.6	31.0	584	102	0(l)	—
1,2-Butadiene	C ₄ H ₆	54.09	—	-136.5	—	10.1	—	446	—	—	—
1,3-Butadiene	C ₄ H ₆	54.09	—	-109.1	—	-4.6	—	425	42.7	—	—
<i>n</i> -Butane	C ₄ H ₁₀	58.12	—	-138.3	4.661	-0.6	22.305	425.17	37.47	-147.0(l) -124.7(g)	-2855.6(l) -2878.5(g)
Isobutane	C ₄ H ₁₀	58.12	—	-159.6	4.540	-11.73	21.292	408.1	36.0	-158.4(l)	-2849.0(l)

4. Partial Vaporization

Compound	Formula	Mol. Wt.	SG (20°/4°)	$T_m(^{\circ}\text{C})^b$	$\Delta\hat{H}_m(T_m)^{c,j}$ kJ/mol	$T_b(^{\circ}\text{C})^d$	$\Delta\hat{H}_v(T_b)^{e,j}$ kJ/mol	$T_c(\text{K})^f$	$P_c(\text{atm})^g$	$(\Delta\hat{H}_f^{\circ})^{h,j}$ kJ/mol	$(\Delta\hat{H}_c^{\circ})^{i,j}$ kJ/mol
Sodium thiosulfate	$\text{Na}_2\text{S}_2\text{O}_3$	158.11	1.667	—	—	—	—	—	—	−1117.1(c)	—
Sulfur (rhombic)	S_8	256.53	2.07	113	10.04	444.6	83.7	—	—	0(c)	—
Sulfur (monoclinic)	S_8	256.53	1.96	119	14.17	444.6	83.7	—	—	+0.30(c)	—
Sulfur dioxide	SO_2	64.07	—	−75.48	7.402	−10.02	24.91	430.7	77.8	−296.90(g)	—
Sulfur trioxide	SO_3	80.07	—	16.84	25.48	43.3	41.80	491.4	83.8	−395.18(g)	—
Sulfuric acid	H_2SO_4	98.08	1.834 ^{18°}	10.35	9.87	Decomposes at 340°C			—	−811.32(l) −907.51(aq)	—
Toluene	C_7H_8	92.13	0.866	−94.99	6.619	110.62	33.47	593.9	40.3	+12.00(l) +50.00(g)	−3909.9(l) −3947.9(g)
Water	H_2O	18.016	1.00 ^{4°}	0.00	6.0095	100.00	40.656	647.4	218.3	−285.84(l) −241.83(g)	— —
<i>m</i> -Xylene	C_8H_{10}	106.16	0.864	−47.87	11.569	139.10	36.40	619	34.6	−25.42(l) +17.24(g)	−4551.9(l) −4594.5(g)
<i>o</i> -Xylene	C_8H_{10}	106.16	0.880	−25.18	13.598	144.42	36.82	631.5	35.7	−24.44(l) +18.99(g)	−4552.9(l) −4596.3(g)
<i>p</i> -Xylene	C_8H_{10}	106.16	0.861	13.26	17.11	138.35	36.07	618	33.9	−24.43(l) 17.95(g)	−4552.91(l) −4595.2(g)
Zinc	Zn	65.38	7.140	419.5	6.674	907	114.77	—	—	0(c)	—

4. Partial Vaporization

Form 1: $C_p[\text{kJ}/(\text{mol}\cdot^\circ\text{C})]$ or $[\text{kJ}/(\text{mol}\cdot\text{K})] = a + bT + cT^2 + dT^3$

Form 2: $C_p[\text{kJ}/(\text{mol}\cdot^\circ\text{C})]$ or $[\text{kJ}/(\text{mol}\cdot\text{K})] = a + bT + cT^{-2}$

Example: $(C_p)_{\text{acetone(g)}} = 0.07196 + (20.10 \times 10^{-5})T - (12.78 \times 10^{-8})T^2 + (34.76 \times 10^{-12})T^3$, where T is in $^\circ\text{C}$.

Note: The formulas for gases are strictly applicable at pressures low enough for the ideal gas equation of state to apply.

Compound	Formula	Mol. Wt.	State	Form	Temp. Unit	$a \times 10^3$	$b \times 10^5$	$c \times 10^8$	$d \times 10^{12}$	Range (Units of T)
Acetone	<chem>CH3COCH3</chem>	58.08	l	1	$^\circ\text{C}$	123.0	18.6			−30–60
			g	1	$^\circ\text{C}$	71.96	20.10	−12.78	34.76	0–1200
Acetylene	<chem>C2H2</chem>	26.04	g	1	$^\circ\text{C}$	42.43	6.053	−5.033	18.20	0–1200
Air		29.0	g	1	$^\circ\text{C}$	28.94	0.4147	0.3191	−1.965	0–1500
			g	1	K	28.09	0.1965	0.4799	−1.965	273–1800
Ammonia	<chem>NH3</chem>	17.03	g	1	$^\circ\text{C}$	35.15	2.954	0.4421	−6.686	0–1200
Ammonium sulfate	<chem>(NH4)2SO4</chem>	132.15	c	1	K	215.9				275–328
Benzene	<chem>C6H6</chem>	78.11	l	1	$^\circ\text{C}$	126.5	23.4			6–67
			g	1	$^\circ\text{C}$	74.06	32.95	−25.20	77.57	0–1200
Isobutane	<chem>C4H10</chem>	58.12	g	1	$^\circ\text{C}$	89.46	30.13	−18.91	49.87	0–1200
<i>n</i> -Butane	<chem>C4H10</chem>	58.12	g	1	$^\circ\text{C}$	92.30	27.88	−15.47	34.98	0–1200
Isobutene	<chem>C4H8</chem>	56.10	g	1	$^\circ\text{C}$	82.88	25.64	−17.27	50.50	0–1200
Calcium carbide	<chem>CaC2</chem>	64.10	c	2	K	68.62	1.19	-8.66×10^{10}	—	298–720
Calcium carbonate	<chem>CaCO3</chem>	100.09	c	2	K	82.34	4.975	-12.87×10^{10}	—	273–1033
Calcium hydroxide	<chem>Ca(OH)2</chem>	74.10	c	1	K	89.5				276–373
Calcium oxide	<chem>CaO</chem>	56.08	c	2	K	41.84	2.03	-4.52×10^{10}		273–1173
Carbon	<chem>C</chem>	12.01	c	2	K	11.18	1.095	-4.891×10^{10}		273–1373
Carbon dioxide	<chem>CO2</chem>	44.01	g	1	$^\circ\text{C}$	36.11	4.233	−2.887	7.464	0–1500
Carbon monoxide	<chem>CO</chem>	28.01	g	1	$^\circ\text{C}$	28.95	0.4110	0.3548	−2.220	0–1500
Carbon tetrachloride	<chem>CCl4</chem>	153.84	l	1	K	93.39	12.98			273–343
Chlorine	<chem>Cl2</chem>	70.91	g	1	$^\circ\text{C}$	33.60	1.367	−1.607	6.473	0–1200
Copper	<chem>Cu</chem>	63.54	c	1	K	22.76	0.6117			273–1357

4. Partial Vaporization

Nitrogen	N ₂	28.02	g	1	°C	29.00	0.2199	0.5723	−2.871	0–1500
Nitrogen dioxide	NO ₂	46.01	g	1	°C	36.07	3.97	−2.88	7.87	0–1200
Nitrogen tetroxide	N ₂ O ₄	92.02	g	1	°C	75.7	12.5	−11.3		0–300
Nitrous oxide	N ₂ O	44.02	g	1	°C	37.66	4.151	−2.694	10.57	0–1200
Oxygen	O ₂	32.00	g	1	°C	29.10	1.158	−0.6076	1.311	0–1500
<i>n</i> -Pentane	C ₅ H ₁₂	72.15	l	1	°C	155.4	43.68			0–36
			g	1	°C	114.8	34.09	−18.99	42.26	0–1200
Propane	C ₃ H ₈	44.09	g	1	°C	68.032	22.59	−13.11	31.71	0–1200
Propylene	C ₃ H ₆	42.08	g	1	°C	59.580	17.71	−10.17	24.60	0–1200
Sodium carbonate	Na ₂ CO ₃	105.99	c	1	K	121				288–371
Sodium carbonate	Na ₂ CO ₃	286.15	c	1	K	535.6				298
decahydrate	·10H ₂ O									
Sulfur	S	32.07	c	1	K	15.2	2.68			273–368
		(Rhombic)								
			c	1	K	18.3	1.84			368–392
		(Monoclinic)								
Sulfuric acid	H ₂ SO ₄	98.08	l	1	°C	139.1	15.59			10–45
Sulfur dioxide	SO ₂	64.07	g	1	°C	38.91	3.904	−3.104	8.606	0–1500
Sulfur trioxide	SO ₃	80.07	g	1	°C	48.50	9.188	−8.540	32.40	0–1000
Toluene	C ₇ H ₈	92.13	l	1	°C	148.8	32.4			0–110
			g	1	°C	94.18	38.00	−27.86	80.33	0–1200
Water	H ₂ O	18.016	l	1	°C	75.4				0–100
			g	1	°C	33.46	0.6880	0.7604	−3.593	0–1500

5. Creativity Exercise

A gas emerges from a stack at 1200°C. Rather than being released directly to the atmosphere, it can be passed through one or several heat exchangers, and the heat it loses can be put to use in a variety of ways. Think of as many uses of this heat as you can.

5. Creativity Exercise

