

## Unit 1 – Linear &amp; Quadratic Functions

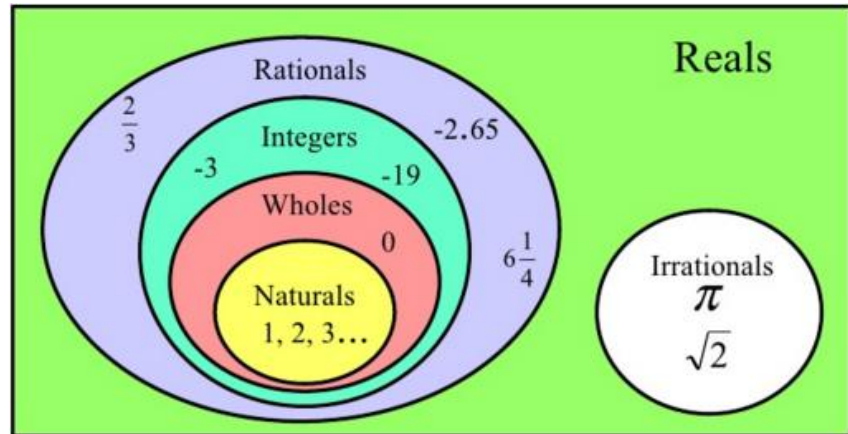
Day	Lesson	Practice Questions	Struggles?
1	U1L1: Domain and Range	<b>Do:</b> Handout	
2	U1L2: Functions & Function Notation	<b>Read:</b> Pg. 14 – 22 <b>Do:</b> Handout Pg. 22 # 1adf, 2, 5ac, 7ac, 10, 11bd, 12, 15c, 16b, 17	
3	<i>Skill Builder: Factoring</i>	<b>Read:</b> Pg. 98 – 101 <b>Do:</b> Pg. 102 # 2 ( <i>just factor, don't describe</i> ), 4 – 7, 9 <b>Challenge:</b> #14	
4	U1L3: Max/Min of a Quadratic	<b>Read:</b> Pg. 148 – 153 <b>Do:</b> Pg. 153 # 1, 2, 4ace, 8, 11ab, <b>Handout</b> Pg. 147 # 12	
5	<i>Skill Builder: Radicals</i>	<b>Read:</b> Pg. 163 – 167 <b>Do:</b> Pg. 167 # 1 – 7ace, 15b, 17	
6	U1L4: Solve Quadratic Equations	<b>Read:</b> Pg. 172 – 177 <b>Do:</b> Pg. 177 # 1bd, 2ad, 4, 5, 6bd, 7, 8c	
7	U1L5: Zeros of a Quadratic Function	<b>Read:</b> Pg. 179 – 184 <b>Do:</b> Pg. 185 # 4ad, 5ab, 6 – 10, 14	
8	<i>Skill Builder: Polynomials</i>	<b>Read:</b> Pg. 84 – 87, 91 – 94 <b>Do:</b> Pg. 88 # 5 – 6ace Pg. 95 # 4 – 5ace, 10, 11ac	
9	U1L6: Equation of a Quadratic Function	<b>Read:</b> Pg. 187 – 191 <b>Do:</b> Pg. 192 # 1 – 3, 4cd, 6, 8, 9, 16	
10	U1L7: Linear/Quadratic Systems	<b>Read:</b> Pg. 194 – 198 <b>Do:</b> Pg. 198 # 1b, 3, 4ac, 6, 8, 10 – 12	
11	Review	<b>Read:</b> Pg. 38 – 39, 105 – 106, 169, 200 – 201 <b>Do:</b> Pg. 76 # 1, 2abcd, 4 – 7 Pg. 132 # 4c, 6g, 7 – 8 Pg. 202 # 4, 5, 9, 12, 13, 15–18, 20–22, 23a #13b: change 300,000 to 30,000 #16: one zero #18: standard form	
12	TEST		

## Unit 1, Lesson 1: Domain and Range

**Domain:** The domain of a relation is the complete set of possible values of the independent ( $x$ ) variable.

**Range:** The range of a relation is the complete set of possible values of the dependent ( $y$ ) variable.

## Number Systems



**Example 1:** A diver jumps from the top of a 10 m cliff. He jumps 1 m into the air, does a front flip and then falls and hits the water 2 seconds after starting his jump.

a) Sketch a height vs. time graph for the function that models the diver's jump.

b) What is the domain and range for the function representing the diver's jump?

## Different ways to describe domain and range

**WORDS:** We use words all the time, so this is a very natural way to describe domain and range.

**For example:** The domain is the time from 0 seconds to 2 seconds.

**INEQUALITY STATEMENT:** This is a more formal way of showing what we put in words.

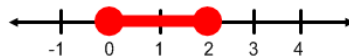
**For example:**  $0 \leq t \leq 2$

**SET BUILDER NOTATION:** The most formal mathematics way of showing domain and range.

**For example:**  $\{t \mid t \in \mathbb{R}, 0 \leq t \leq 2\}$

**NUMBER LINE:** People like seeing pictures, so we sometimes show a line.

**For example:**

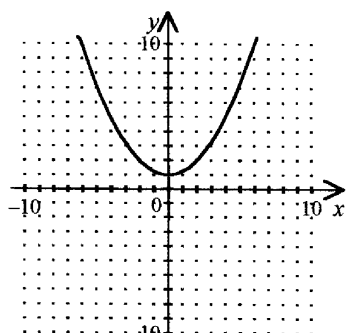


**LIST OF NUMBERS:** Only use this method when we have a finite set of points so we can actually list all numbers.

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## Example 2:

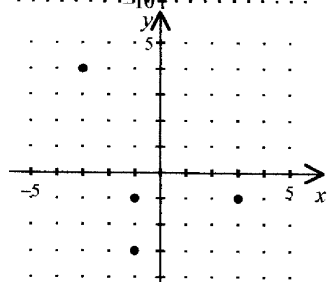
Ex.



D = \_\_\_\_\_

R = \_\_\_\_\_

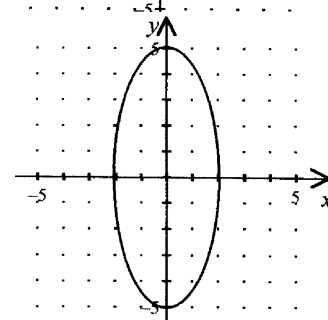
Ex.



D = \_\_\_\_\_

R = \_\_\_\_\_

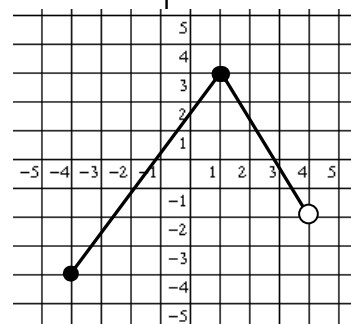
Ex.



D = \_\_\_\_\_

R = \_\_\_\_\_

Ex.



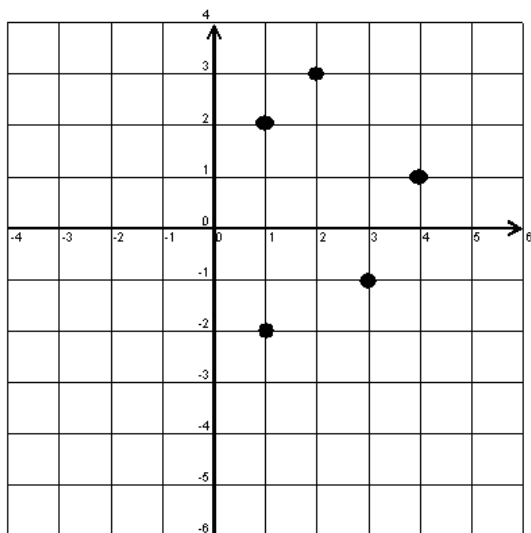
D = \_\_\_\_\_

R = \_\_\_\_\_

**Example 3:** A pool at a fitness centre is being drained. The number of kilolitres of water,  $N$ , in the pool after an elapsed time  $t$ , in minutes, is given by the formula  $N = 100 - 0.25t$ . State the domain and range for this function.

State the domain and the range for each of the following graphs, using set notation.

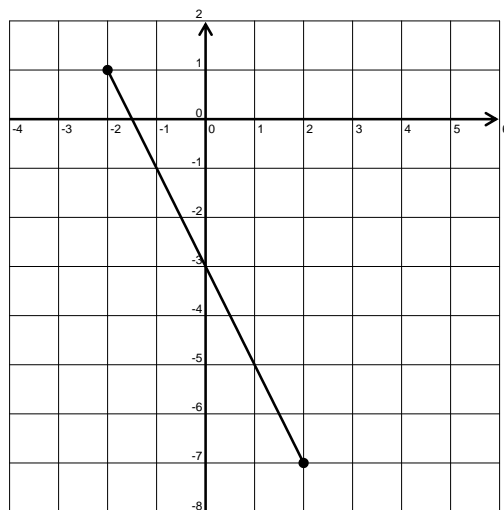
1.



D = \_\_\_\_\_

R = \_\_\_\_\_

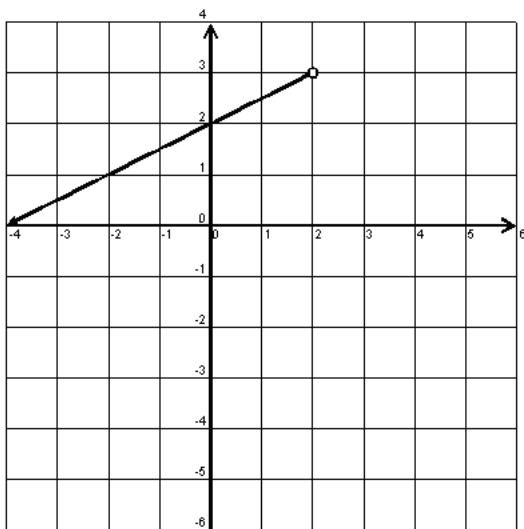
2.



D = \_\_\_\_\_

R = \_\_\_\_\_

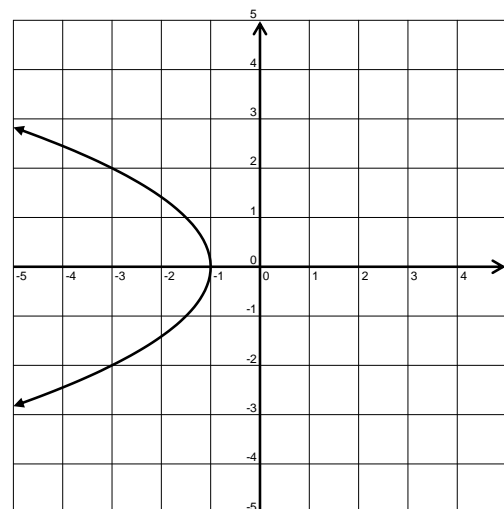
3.



D = \_\_\_\_\_

R = \_\_\_\_\_

4.

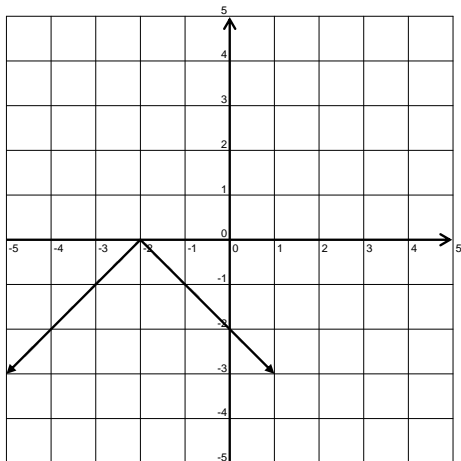


D = \_\_\_\_\_

R = \_\_\_\_\_

MCR.

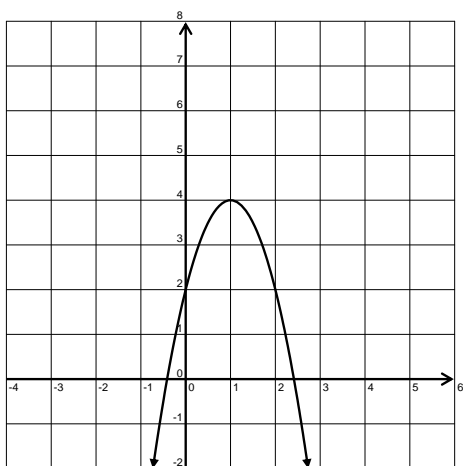
5.



D = \_\_\_\_\_

R = \_\_\_\_\_

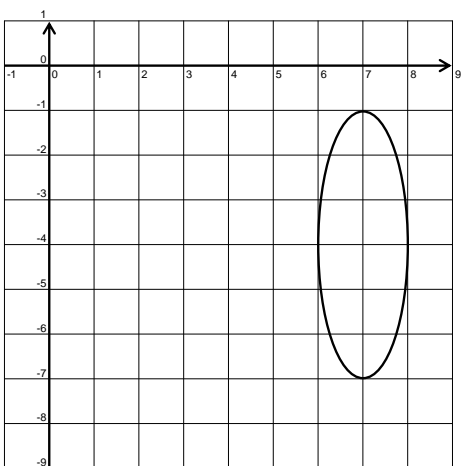
7.



D = \_\_\_\_\_

R = \_\_\_\_\_

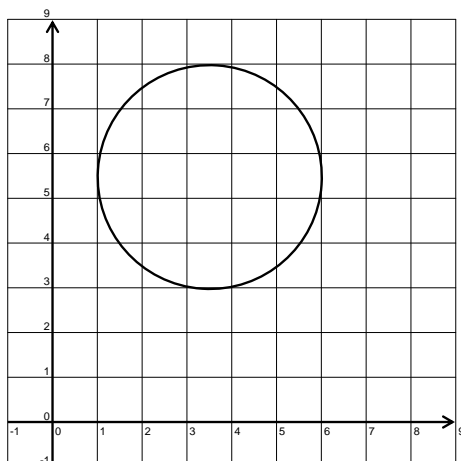
9.



D = \_\_\_\_\_

R = \_\_\_\_\_

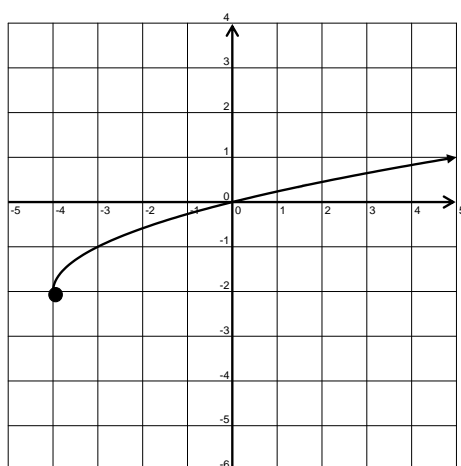
6.



D = \_\_\_\_\_

R = \_\_\_\_\_

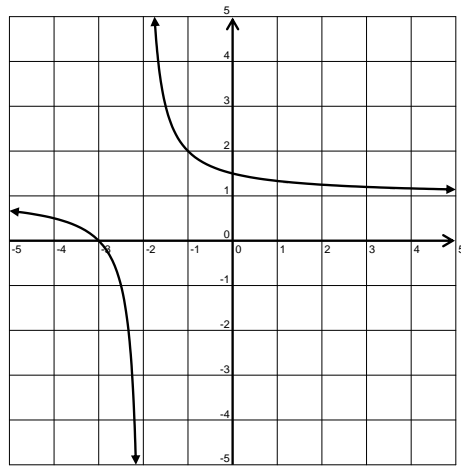
8.



D = \_\_\_\_\_

R = \_\_\_\_\_

10.



D = \_\_\_\_\_

R = \_\_\_\_\_

- **Relation**

- Mapping between a domain and a range
- Can be represented as: list of ordered pairs, mapping, table, graph, equation.

- **Function**

- A relation where each element in the domain maps to a single element in the range
- Given any  $x$  value there is only one  $y$  value associated with it

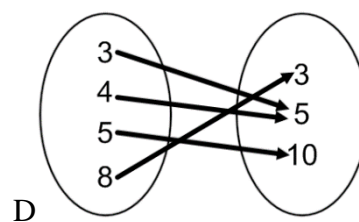
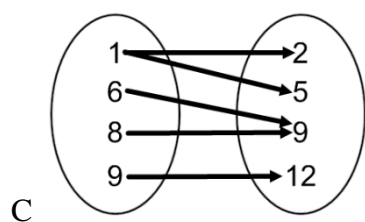
- **Vertical Line Test (VLT)**

- Used to test if a graph represents a function
- If a vertical line through any portion of the graph touches the graph more than once, the graph does not represent a function

**Example: Classify each relation as a function or a non-function.**

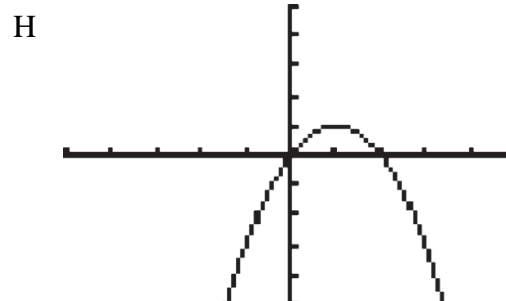
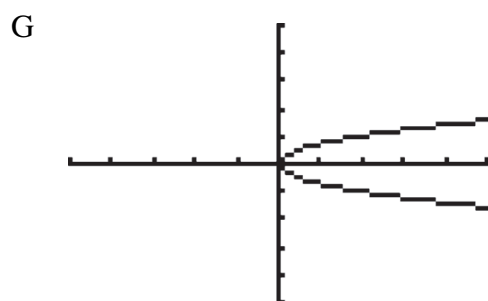
A  $\{(1,2), (3,4), (4,5)\}$

B  $\{(1,2), (1,4), (4,5)\}$



E  $x^2 + y^2 = 36$

F  $y = -3x^2 + 1$



- **Function Notation**

Functions can be described using function notation. The linear equation  $y = -3x + 6$  is a function. In function notation:  $f(x) = -3x + 6$ .

$x$  is the input of the function

$f(x)$  is the output of the function (**it does not mean  $f$  times  $x$** )

$f$  is the name of the function

**MCR 3U McKinnell****Example:** Let  $f(x) = -3x + 6$ . Determine the following:

a)  $f(0)$

b)  $f(-4)$

c)  $f(a - 1)$

d)  $f(2) - f(1)$

e)  $3f(5)$

**Example:** Let  $g(x) = -2x^2 + 2x - 6$ . Determine the following

a)  $g(2)$

b)  $g(2) + g(-1)$

c)  $g(a + 5)$

**Example:** Using the table of values provided, determine the following:

a)  $h(20)$

b)  $h(-1)$

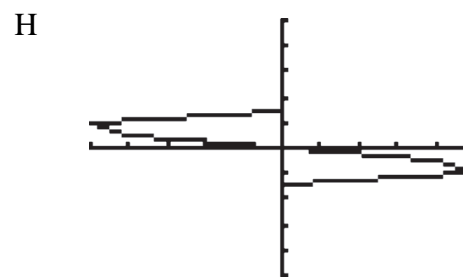
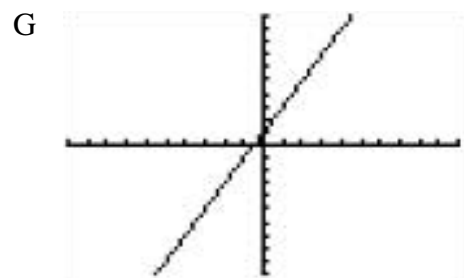
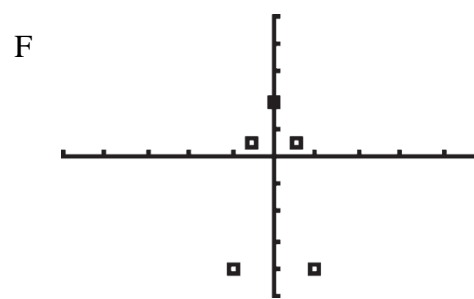
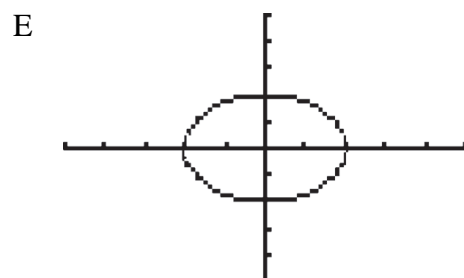
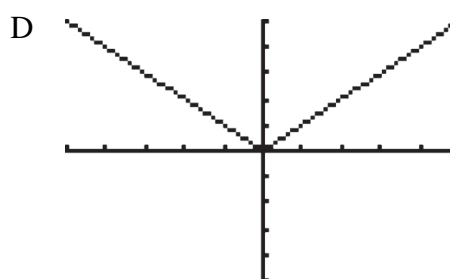
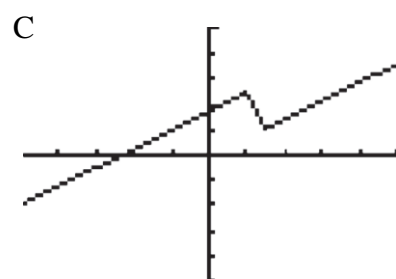
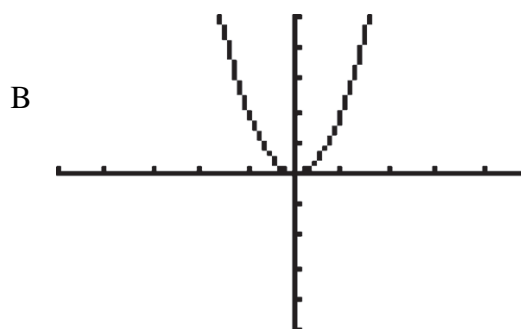
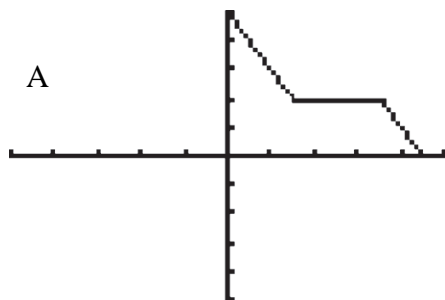
c)  $h(8)$

d) value(s) for  $x$  such that  $h(x) = 9$

$x$	$h(x)$
-5	8
-3	2
0	-1
2	9
8	4
9	4
20	0

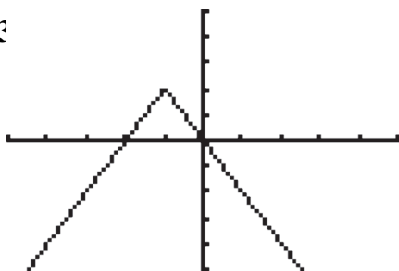
**Example:** Let  $f(x) = x^2 + 5x - 14$ . Determine value(s) for  $x$  such that  $f(x) = -20$

1. Classify each as a function or a non-function.

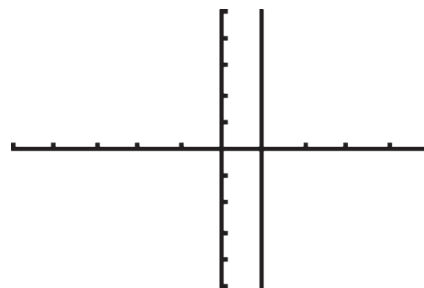




MCR 3  
I



J



K  $\{(0,0), (2,5), (6,10)\}$

L  $\{(2,1), (1,5), (2,6)\}$

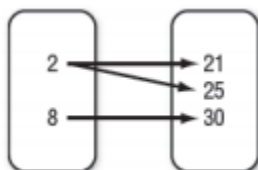
M

x	y
-3	0
-1	-1
0	0
2	-2
3	4

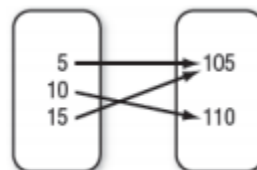
N

x	y
-2	-1
-2	1
-1	0
1	0
2	1

O



P



Q  $y = 5(x - 2)^2 + 8$

R  $4x^2 - 3y^2 = 12$

2. Refer to yesterday's HW Handout (Domain & Range). For each graph, classify as a function or non-function

- Factoring involves changing a polynomial relation from standard form (i.e. \_\_\_\_\_ ) to factored form (i.e. \_\_\_\_\_)
- Remember! **ALWAYS LOOK FOR COMMON FACTORS FIRST!**
- THEN, if a quadratic remains, **FACTOR WHATEVER IS INSIDE THE BRACKETS, IF POSSIBLE.**

1)  $x^2 - 14x + 45$

2)  $y^2 + 2y - 15$

3)  $3x^2 - 11x - 4$

4)  $9x^2 - 25$

5)  $16 - t^2$

6)  $4x^2 - 16$

7)  $4a^2 - 12a + 9$

8)  $x^2 + 4x + 4$

9)  $18x^2 - 32$

10)  $6x^2 + x - 12$

11)  $6x^2 + 2x - 4$

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### Factoring by Grouping (*should have 4 terms in polynomial*)

- Separate the four terms into two groups of two or three terms (you may have to rearrange the terms)
  - For groups of two terms
    - Factor each group so that each has the same common factor remaining
    - Factor this common factor into one bracket and the remaining terms into another bracket
  - For groups of three terms
    - Factor a trinomial into two identical brackets which can then be written as  $( \quad )^2$ .
    - This may result in a difference of squares which can then be factored into two large brackets.
    - Simplify the two large brackets as much as possible, eliminating any brackets within.

### Example – factor each expression by grouping

a)  $xy + 6x + 5y + 30$

b)  $2ab + 2a - 3b - 3$

c)  $x^3 + x^2 + x + 1$

d)  $y^2 - 4y + 4 - 16x^2$

e)  $8x^4 - 18y^2 - 60y - 50$

f)  $2m^2 + 10m + 10n - 2n^2$

**Different forms of a quadratic function**

FORM	GIVES US
<b>Standard form:</b> $f(x) = ax^2 + bx + c$ (Pretty but almost useless)	<i>Direction of opening</i> <i>Vertical stretch</i> <i>y-intercept</i>
<b>Vertex form:</b> $f(x) = a(x - h)^2 + k$ Found by completing the square	<i>Direction of opening</i> <i>Vertical stretch</i> <i>Vertex</i>
<b>Factored form:</b> $f(x) = a(x - r)(x - s)$ Found by factoring	<i>Direction of opening</i> <i>Vertical stretch</i> <i>Zeros or x-intercepts</i>

The **maximum** or **minimum (optimal) value** of a quadratic function is the **y-coordinate of the vertex**. There are a variety of strategies to determine the vertex of a quadratic function.

**Method 1: Factoring** to determine the zeroes & use to determine vertex

**Example:**  $f(x) = -3x^2 - 12x + 15$

**Method 2: Partial Factoring** to determine the axis of symmetry ( $x$ -coordinate of the vertex), then substitute.

**Example:**  $f(x) = 4x^2 + 10x + 3$

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**Method 3: Completing the square** & read vertex  $(h, k)$  from equation in vertex form.

**Example:**  $f(x) = 7x^2 - 9x - 2$

When reading word problems, pay close attention to how variables are defined.

**Example:** The cost function in a computer manufacturing plant is  $C(x) = 0.28x^2 - 0.7x + 1$ , where  $C(x)$  is the cost per hour in millions of dollars and  $x$  is the number of items produced per hour in thousands.

Determine the number of items that will produce the minimum cost and give the minimum production cost.

Determine the **optimal value** for each function by **completing the square** and indicate whether it is a **maximum** or **minimum**.

1.  $f(x) = -0.2x^2 - 3.1x + 7.3$

Optimal Value : \_\_\_\_\_

Max / Min

2.  $g(x) = -5x^2 + 4x - 6$

Optimal Value : \_\_\_\_\_

Max / Min

3.  $P(x) = 2x^2 - 9x$

Optimal Value : \_\_\_\_\_

Max / Min

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4.  $h(t) = -t^2 + \frac{3}{4}t - \frac{1}{2}$

Optimal Value : \_\_\_\_\_

Max / Min

5.  $k(x) = -\frac{2}{3}x^2 + \frac{4}{5}x - 1$

Optimal Value : \_\_\_\_\_

Max / Min

6.  $R(x) = 50x^2 - 120x + 3$

Optimal Value : \_\_\_\_\_

Max / Min

1). 19.3, max 2) $-\frac{26}{5}$ , max 3) $-\frac{81}{8}$ , min 4) $-\frac{23}{64}$ , max 5) $-\frac{19}{25}$ , max 6) $-69$ , min
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**Part A) Evaluate without the use of a calculator:**

$$\sqrt{4 \times 9} =$$

$$\sqrt{4} \times \sqrt{9} =$$

$$\sqrt{4 \times 16} =$$

$$\sqrt{4} \times \sqrt{16} =$$

$$\sqrt{9 \times 16} =$$

$$\sqrt{9} \times \sqrt{16} =$$

$$\sqrt{4 \times 25} =$$

$$\sqrt{4} \times \sqrt{25} =$$

What do you notice? Write a rule to explain your observations.

**Part B) Evaluate (round to 4 decimal places) with a calculator:**

$$\sqrt{5 \times 5} =$$

$$\sqrt{5} \times \sqrt{5} =$$

$$\sqrt{9 \times 3} =$$

$$\sqrt{9} \times \sqrt{3} =$$

$$\sqrt{2 \times 10} =$$

$$\sqrt{2} \times \sqrt{10} =$$

$$\sqrt{6 \times 3} =$$

$$\sqrt{6} \times \sqrt{3} =$$

Does the rule you created in part A still work?

**Part C) Without a calculator, write each radical in a different way. (Notice the similarity to the numbers from part B)**

$$\sqrt{27}$$

$$\sqrt{20}$$

$$\sqrt{18}$$



The **product property** of radicals states:

$$\text{For } a \geq 0, b \geq 0; \sqrt{a}\sqrt{b} = \sqrt{ab}$$

We can use this property to simplify & perform operations with radicals

Simplifying Radicals

1. Find **2** factors, one of which is a perfect square (highest perfect square possible).
2. Rewrite as two radicals. (First radical must be the perfect square.)
3. Evaluate the perfect square.

\*\*\* If the number under your radical cannot be divided evenly by any of the perfect squares, your radical is already in simplest form and cannot be reduced further. \*\*\*

**Practice:** Simplify

a)  $\sqrt{12}$

b)  $2\sqrt{24}$

c)  $\sqrt{32}$

d)  $-\sqrt{8}$

**Multiplying Radicals**

- Outside times outside, stays outside.
- Inside times inside, stays inside.
- Simplify radical

a)  $2\sqrt{2} \times 3\sqrt{7}$

b)  $5\sqrt{6} \times \sqrt{5}$

c)  $-8\sqrt{10} \times 2\sqrt{2}$

**Dividing Radicals**

- Outside divided by outside, stays outside.
- Inside divided by inside, stays inside.
- Simplify radical.

a)  $\frac{2\sqrt{15}}{\sqrt{3}}$

b)  $\frac{\sqrt{24}}{\sqrt{2}}$

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### **Adding/Subtracting Radicals**

- You can only add or subtract like radicals (think algebra: like terms)
- Reduce if needed, then collect like radicals

**Simplify any individual radical terms first.**

**Example:**  $3\sqrt{7} + 2\sqrt{7} = 5\sqrt{7}$

**Practice:** Simplify

a)  $3\sqrt{11} + 2\sqrt{11}$

b)  $5\sqrt{8} - 3\sqrt{18}$

### **Multiplying Radical Expressions**

To multiply radical expressions use the distributive law and simplify where possible.

**Example:**  $3\sqrt{3}(4 - 2\sqrt{8})$

**Example:**  $(2 + 3\sqrt{5})(3 - 2\sqrt{6})$

**Example:**  $(7 + 2\sqrt{6})(6 - \sqrt{6})$

## Unit 1, Lesson 4: Solving Quadratic Equations

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**Quadratic Equation:** An equation of the form  $ax^2 + bx + c = 0$ , where  $a, b, c \in \mathbb{R}$  and  $a \neq 0$ .

The **solution** to a quadratic equation is also called the **roots** of the equation.

There are 3 methods to solve a quadratic equation.

### Method 1: Inverse Operations

Use this method when there is a single  $x$ -term (vertex form)

- Use inverse operations to isolate  $x$
- When you take the square root, recall that there should be 2 answers.
- Leave answer in simplified radical form, unless specified otherwise.

**Example:** Solve  $2(x - 9)^2 - 19 = 5$

### Method 2: Factoring

Try this method before resorting to method #3

- Rearrange equation so it is in standard form  $ax^2 + bx + c = 0$
- Factor, if possible.
- Set each factor to 0 and solve each linear equation.

**Example:** Determine the roots of  $x(4x - 5) = 6$

### Method 3: Quadratic Formula

Use this method when the equation is not factorable.

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- Rearrange equation so it is in standard form  $ax^2 + bx + c = 0$
- Substitute  $a, b, c$  into the quadratic formula  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
- Leave answer in simplified radical form, unless specified otherwise.

**Example:** Solve  $2x(2x + 3) + 6 = 5$

**Example:** The Profit function for a business is modelled by the equation  $P(x) = -0.5x^2 + 10x - 16$ , where  $x$  is the number of items sold in thousands, and  $P(x)$  is the profit in thousands of dollars. Determine the number of items the company must sell in order to break even.

**How to Determine the Number of Zeros (x-intercepts)****Factored form:**  $f(x) = a(x - r)(x - s)$ 

- The number of zeros will be equivalent to the number of **unique factors**.
- If there are no zeros, the equation cannot be written in factored form.

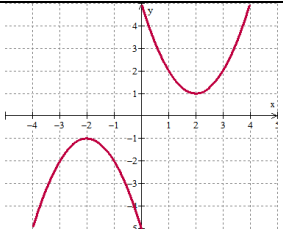
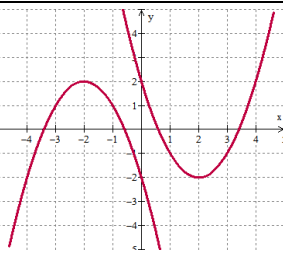
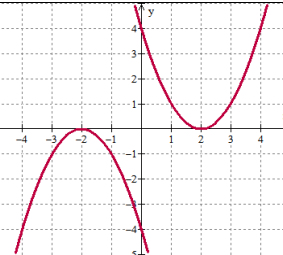
**Example 1:** Without drawing the graph, find the number of zeros of the following functions.

a)  $f(x) = 0.4(x - 1)(x + 2)$

b)  $g(x) = 3(x + 5)^2$

c)  $h(x) = 4x(x - 2)$

**Vertex form:**  $f(x) = a(x - h)^2 + k$ 

	<p>if <math>a</math> &amp; <math>k</math> have the <b>same sign</b></p> <p><math>a &gt; 0</math> &amp; <math>k &gt; 0</math>      or      <math>a &lt; 0</math> &amp; <math>k &lt; 0</math></p> <p><b>no real zeros</b></p>
	<p>if <math>a</math> &amp; <math>k</math> have <b>opposite signs</b></p> <p><math>a &gt; 0</math> &amp; <math>k &lt; 0</math>      or      <math>a &lt; 0</math> &amp; <math>k &gt; 0</math></p> <p><b>two real zeros</b></p>
	<p>if <math>k = 0</math></p> <p><b>one real zero</b></p>

**Example 2:** Without drawing the graph, find the number of zeros of the following functions.

a)  $f(x) = 1.3(x - 4)^2 + 2.2$

b)  $g(x) = 1.7(x + 2)^2 - 4.5$

c)  $h(x) = 3(x - 2.4)^2$

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**Standard form:**  $f(x) = ax^2 + bx + c$

- Calculate the **Discriminant**  $\rightarrow b^2 - 4ac$  (from the quadratic formula)
  - if  $b^2 - 4ac > 0 \rightarrow 2$  real zeros
  - if  $b^2 - 4ac = 0 \rightarrow 1$  real zero
  - if  $b^2 - 4ac < 0 \rightarrow$  no real zeros ( 2 complex zeros)

**Example 3:** Determine the **number** of zeros.

**a)**  $f(x) = x^2 - 8x + 16$

**b)**  $g(x) = 3x^2 + 2x + 4$

**Example 4:** For what values of  $k$  does the equation  $2x^2 + kx + 8 = 0$  have

- a) two distinct, real roots?
- b) one real root?
- c) no real roots?

**Try:** Determine the value(s) of  $k$  such that the function  $f(x) = 3x^2 + kx - 3 + k$  has exactly one zero.

- **Polynomial** – numerical coefficients are real numbers, exponents are non-negative integers
  - Monomial – one term
  - Binomial – two terms
  - Trinomial – three terms
- **Degree** of a polynomial is the value of the highest exponent
  - Polynomial of degree 0 is called a constant
  - Polynomial of degree 1 is called a linear expression
  - Polynomial of degree 2 is called a quadratic expression
  - Polynomial of degree 3 is called a cubic expression
  - Polynomial of degree 4 is called a quartic expression

### Adding and Subtracting Polynomials

- To **add or subtract** polynomials, combine like terms.
- Remember that if you are subtracting a polynomial, you must subtract **each term** of the polynomial.

Ex 1) Simplify  $(-2x^2 + 5x - 3) + (x^2 - 6x + 1) - (-3x^2 - 2x - 4)$

### Multiplying Polynomials

- To **multiply** (or **expand**) polynomials, use the **distributive property** – multiply each term inside the bracket by the number/term outside of the brackets.
  - When a polynomial is multiplied by another polynomial, this means that **every term** in the first polynomial is multiplied by **every term** in the second polynomial.

$$(2x + 3y + 4z)^2 = (2x + 3y + 4z)(2x + 3y + 4z)$$

- After applying the distributive property don't forget to **collect like terms**!

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Ex 2) **Expand**  $(2y - 5)(3y^2 + 4y - 6)$

Ex 3) **Expand**  $(2x^2 - 3x + 1)(4x^2 + 5x - 6)$

Ex 4) **Expand**  $(2x - 5)^3$



## Unit 1, Lesson 6: Equation of a Quadratic Function

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### Investigate:

1. Using graphing software, graph each of the following quadratic functions. How are the graphs the same? How are they different?

$f(x) = x^2 - 3x - 10$
$g(x) = -2x^2 + 6x + 20$
$h(x) = 4x^2 - 12x - 40$
$k(x) = -0.5x^2 + 1.5x + 5$

2. Write each function in factored form. What do you notice?

3. This group of functions forms a **family of quadratic functions**. What is the **common characteristic** of this family?

A **Family of Parabolas** is a group of parabolas that share a common characteristic

**Vertex Form:** Where ‘a’ is varied, this results in a family of parabolas with the same vertex and axis of symmetry

**Factored Form:** Where ‘a’ is varied, this results in a family of parabolas with the same x-intercepts and axis of symmetry

**Standard Form:** Where ‘a’ and ‘b’ are varied, this results in a family of parabolas with the same y-intercept

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**Example:** Write the equation (in standard form) of the quadratic function that passes through the point  $(2, -9)$ , if the roots of the corresponding quadratic equation are 5 and -7.

**Recall:** Expand  $(5 - 6\sqrt{3})(5 + 6\sqrt{3})$

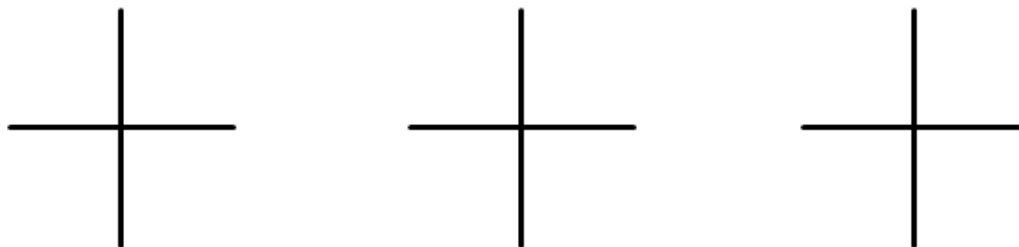
**Example:** Write the equation (in standard form) of the quadratic function that passes through the point  $(-1, 3)$ , if the roots of the corresponding quadratic equation are  $5 \pm 3\sqrt{2}$ .

Unit 1, Lesson 7: Linear/Quadratic Systems

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**Recall:** A **linear system** involves 2 linear functions with the same independent and dependent variables. The solution of the linear system is the point of intersection (POI) of the 2 lines. Linear systems can be solved graphically or algebraically (substitution or elimination).

A **linear-quadratic system** involves one **linear function**, and one **quadratic function**. The solution of the system is the point(s) of intersection of the 2 functions. There may be 0, 1 or 2 solutions.

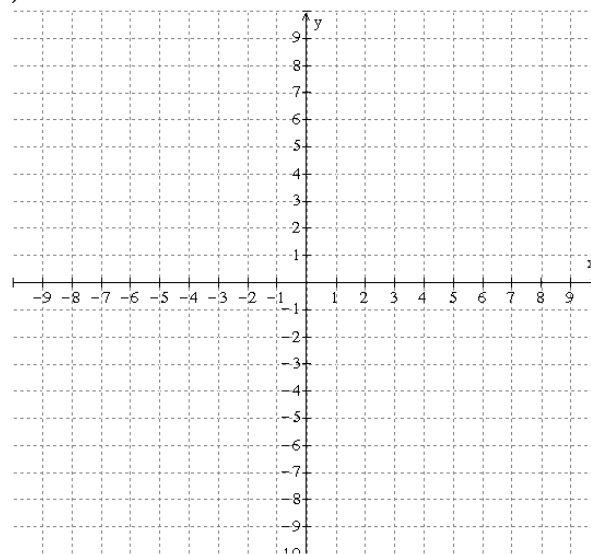


Solving a linear-quadratic system can be done GRAPHICALLY or ALGEBRAICALLY

**GRAPHICALLY** – graph each function and identify the **point(s) of intersection**.

**ALGEBRAICALLY** – solve the system using **substitution**

**Example:** Given  $p(x) = x^2 - 4x$  and  $q(x) = 2x - 5$ , graph to find the point(s) of intersection.



**Example:** Given  $g(x) = 2x - 2$  and  $f(x) = x^2 - 3x + 2$ , determine the point(s) of intersection algebraically.

1. Isolate y in the linear equation
2. Sub. into the quadratic equation
3. Solve the quadratic (factor or quadratic formula)
4. Sub. **each** x-value back into the line to get y

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We can also solve problems involving linear and quadratic functions.

**Example:** A skydiver jumped from an airplane and fell freely for several seconds before releasing her parachute. Her height in metres, above the ground  $t$  seconds after jumping out is given by  $h_1(t) = -4.9t^2 + 5000$  before she released her parachute, and  $h_2(t) = -4t + 4000$  after she released the parachute. How long after jumping did she release her parachute? How high was she above the ground at that time?

**Example:** Determine the equations of the lines that have a slope of 2 and that intersect the quadratic function  $f(x) = x(6 - x)$  once; twice; never.

*Hint for #6 – Breakeven point for a business will happen when the revenue is equal to the cost.*