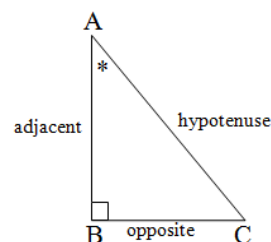


## Lesson 2: Trig Ratios & Special Angles

### Recall: Primary Trigonometric Ratios

$$\begin{aligned} \text{sine of } \angle A &\longrightarrow \sin A = \frac{\text{opposite}}{\text{hypotenuse}} \longrightarrow \sin A = \frac{O}{H} \\ \text{cosine of } \angle A &\longrightarrow \cos A = \frac{\text{adjacent}}{\text{hypotenuse}} \longrightarrow \cos A = \frac{A}{H} \\ \text{tangent of } \angle A &\longrightarrow \tan A = \frac{\text{opposite}}{\text{adjacent}} \longrightarrow \tan A = \frac{O}{A} \end{aligned}$$



\*\* The easiest way to **MEMORIZE** these ratios is to use:

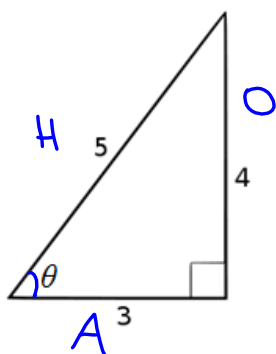
**SOH, CAH, TOA**

### NEW: Reciprocal Trigonometric Ratios

$$\begin{aligned} \text{cosecant of } \angle A &\longrightarrow \csc A = \frac{1}{\sin A} \longrightarrow \csc A = \frac{H}{O} \\ \text{secant of } \angle A &\longrightarrow \sec A = \frac{1}{\cos A} \longrightarrow \sec A = \frac{H}{A} \\ \text{cotangent of } \angle A &\longrightarrow \cot A = \frac{1}{\tan A} \longrightarrow \cot A = \frac{A}{O} \end{aligned}$$

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Ex 1) Determine the 6 trigonometric ratios for  $\theta$ .



$$\sin \theta = \frac{4}{5}$$

$$\csc \theta = \frac{5}{4}$$

$$\cos \theta = \frac{3}{5}$$

$$\sec \theta = \frac{5}{3}$$

$$\tan \theta = \frac{4}{3}$$

$$\cot \theta = \frac{3}{4}$$

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Special Triangles

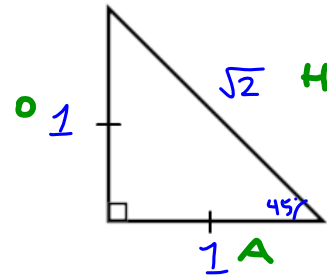
Special triangles are used to determine **exact ratios** for certain special angles.  
(no calculators!)

45-45-90 triangle

Consider a **right isosceles** triangle, with legs measuring 1 unit. Label the angles.

Determine the exact measure of the hypotenuse.

$$\begin{aligned} a^2 + b^2 &= c^2 \\ 1^2 + 1^2 &= c^2 \\ 2 &= c^2 \\ \sqrt{2} &= c \end{aligned}$$



From this we can determine the **exact values** of

$$\begin{aligned} \sin 45^\circ &= \frac{O}{H} \\ \sin 45^\circ &= \frac{1}{\sqrt{2}} \end{aligned}$$

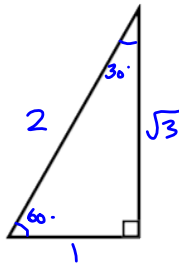
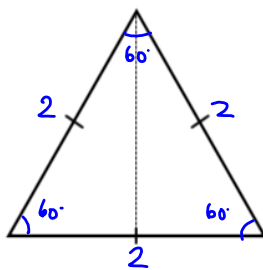
$$\begin{aligned} \cos 45^\circ &= \frac{A}{H} \\ \cos 45^\circ &= \frac{1}{\sqrt{2}} \end{aligned}$$

$$\begin{aligned} \tan 45^\circ &= \frac{O}{A} \\ &= \frac{1}{1} \\ \tan 45^\circ &= 1 \end{aligned}$$

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30-60-90 triangle

Consider an **equilateral** triangle, with sides measuring 2 units. Divide into 2 congruent right triangles (along the altitude). Determine the interior angles & the exact measure of each side.



$$\begin{aligned} a^2 + b^2 &= c^2 \\ 1^2 + b^2 &= 2^2 \\ 1 + b^2 &= 4 \\ b^2 &= 3 \\ b &= \sqrt{3} \end{aligned}$$

From this we can determine the **exact values** of

$$\sin 30^\circ = \frac{1}{2}$$

$$\cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$\tan 30^\circ = \frac{1}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{\sqrt{3}}{3}$$

$$\sin 60^\circ = \frac{\sqrt{3}}{2}$$

$$\cos 60^\circ = \frac{1}{2}$$

$$\tan 60^\circ = \sqrt{3}$$

For all triangles, the **smallest side** is across from the **smallest angle** and the **largest side** is across from the **largest angle**.

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**"Rationalizing the denominator"** is a process that is used to change a rational expression so it does *not* have a radical in the denominator. It uses the **identity property of 1** (any number multiplied by 1 retains its value.)

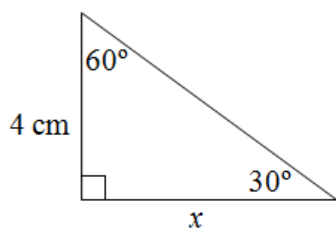
NOTE:  $\sin^2\theta = (\sin\theta)^2$  in both cases we are squaring the ratio, not the angle  
( $\sin^2\theta \neq \sin\theta^2$ )

Ex 2) Determine the exact value of  $\sin^2 60^\circ \times \sin 45^\circ$ . Rationalize the denominator, if necessary.

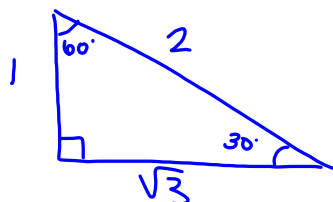
$$\begin{aligned}
 &= \left(\frac{\sqrt{3}}{2}\right)^2 \left(\frac{\sqrt{2}}{2}\right) \\
 &= \left(\frac{3}{4}\right) \left(\frac{\sqrt{2}}{2}\right) \\
 &= \frac{3\sqrt{2}}{8}
 \end{aligned}$$

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Ex 4) Use special triangles to determine the exact length of side  $x$ .



$$\begin{aligned}
 \frac{1}{\sqrt{3}} &= \frac{4}{x} \\
 x &= 4\sqrt{3}
 \end{aligned}$$



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HW U3L2:

1. p.280 #1-3, 5a)i,iv, 9

2. p.286 #3, 4, 5a, 6b, 8, 11

3. sign & correct tests