

Name: \_\_\_\_\_

Mark: \_\_\_\_\_ / 20

| K/U       | A         | T         | C         |
|-----------|-----------|-----------|-----------|
| _____ / 6 | _____ / 6 | _____ / 4 | _____ / 4 |

**Introduction:**

The transformed city is a city designed based on the concept of transformation. Every building is a transformation of the main building City Hall (building #1). You are given a rule of transformation to:

- 1) identify the transformation for building #2 - #6 in comparison with the city hall;
- 2) based on the coordinates of the city hall, determine the coordinates for buildings #2 - #6;
- 3) graph each building in the city on the given coordinate plane, based on the coordinates determined in the last step.

- Building 1 (main building) - City Hall  
- its location is represented by the relation  $f(x)$ .
- Building 2 - Police station  
- its location is represented by the relation  $g(x) = f(x + 12)$ .
- Building 3 - Hospital  
- its location is represented by the relation  $h(x) = f(x) - 13$ .
- Building 4: Local TV station  
- its location is represented by the relation  $k(x) = f(3x)$ .
- Building 5: Public library  
- its location is represented by the relation  $m(x) = 2f(x) - 3$ .
- Building 6: Airport  
- its location is represented by the relation  $n(x) = -f(x + 10) + 4$ .

**Submission Checklist:**

- Completed worksheet that includes all elements:
  - Filled table 1 (transformations)
  - Filled table 2 (coordinate points)
  - Completed table 3 (coordinate plane with 6 drawn buildings)
- You may submit your final work in a scanned pdf (preferred) / photos in one document.

**Hint:**

| Transformation Rules |  |  |
|----------------------|--|--|
| Function Notation    | Type of Transformation                 | Change to Coordinate Point                       |
| $f(x) + c$           | Vertical translation up $c$ units      | $(x, y) \rightarrow (x, y + c)$                  |
| $f(x) - c$           | Vertical translation down $c$ units    | $(x, y) \rightarrow (x, y - c)$                  |
| $f(x + d)$           | Horizontal translation left $d$ units  | $(x, y) \rightarrow (x - d, y)$                  |
| $f(x - d)$           | Horizontal translation right $d$ units | $(x, y) \rightarrow (x + d, y)$                  |
| $-f(x)$              | Reflection over x-axis                 | $(x, y) \rightarrow (x, -y)$                     |
| $f(-x)$              | Reflection over y-axis                 | $(x, y) \rightarrow (-x, y)$                     |
| $af(x)$              | Vertical stretch for $ a  > 0$         | $(x, y) \rightarrow (x, ay)$                     |
| $af(x)$              | Vertical compression for $0 <  a  < 1$ | $(x, y) \rightarrow (x, ay)$                     |
| $f(kx)$              | Horizontal compression for $ k  > 0$   | $(x, y) \rightarrow \left(\frac{x}{k}, y\right)$ |
| $f(kx)$              | Horizontal stretch for $0 <  k  < 1$   | $(x, y) \rightarrow \left(\frac{x}{k}, y\right)$ |

**Table 1 [K+C]: Identify and describe transformations of each of the following relations compared to  $f(x)$ .**

|                         |
|-------------------------|
| $g(x) = f(x + 12)$      |
| $h(x) = f(x) - 13$      |
| $k(x) = f(2x)$          |
| $m(x) = 3f(x) - 3$      |
| $n(x) = -f(x + 10) + 4$ |

**Table 2 [T]: Complete the coordinate points for each function transformed from  $f(x)$ .**

**Show your work below.** (e.g. which formula did you choose? how did you apply it?)

| $f(x)$ | $g(x)$ | $h(x)$ | $k(x)$ | $m(x)$ | $n(x)$ |
|--------|--------|--------|--------|--------|--------|
| (2,2)  |        |        |        |        |        |
| (5,2)  |        |        |        |        |        |
| (5,6)  |        |        |        |        |        |
| (4,6)  |        |        |        |        |        |
| (4,5)  |        |        |        |        |        |
| (2,5)  |        |        |        |        |        |

**Table 3 [A]:** According to the coordinates, **draw** buildings #2 - #6 and **label** them with the building names.

