

### Lesson 5: Representing Functions with Equations (Day 2)

For graphs of sinusoidal functions, we are often interested in obtaining the *simplest* equation. This means:

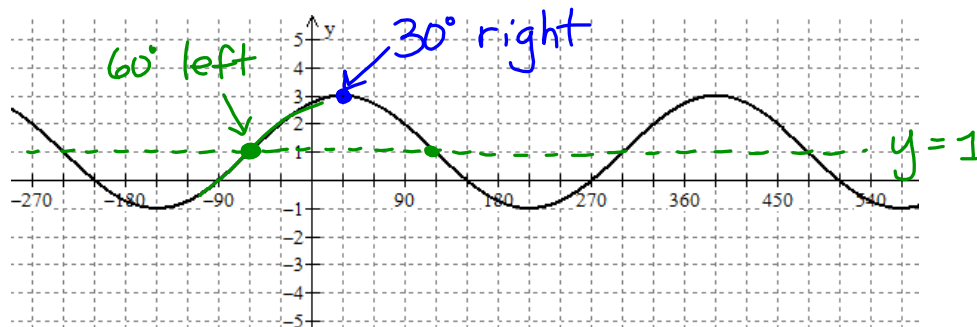
- Avoid phase shifts (horizontal translations), if possible
  - *ideally  $d=0$*  Sometimes you can use a reflection in the x-axis instead of a phase shift
  - If possible, choose a base curve (sine or cosine) that avoids a phase shift
- Avoid using reflections in the y-axis

From the graph, it is easiest to identify its properties, and then use those properties to determine the transformations and the equation.

Parameter	Property	How to determine/calculate
$a$	Amplitude	$ a  = \frac{\max - \min}{2}$ $a < 0$ if a reflection is needed to avoid a phase shift
$k$	# of cycles in the domain of the base curve	$k = \frac{360^\circ}{\text{period}}$
$d$	Phase shift	Sine as base curve <ul style="list-style-type: none"> <li>• Locate the equation of the axis.</li> <li>• Find the <b>POI</b> between the <b>curve</b> and the <b>equation of the axis</b> closest to the y-axis where the graph is <b>increasing</b>.</li> <li>• The <math>\theta</math>-value of this point is the phase shift.</li> </ul> Cosine as base curve <ul style="list-style-type: none"> <li>• Go to the <b>maximum</b> closest to the y-axis</li> <li>• The <math>\theta</math>-value of this point is the phase shift.</li> </ul>
$c$	Vertical displacement, also the y-intercept of the equation of the axis	$c = \frac{\max + \min}{2}$

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Ex 7) Determine the (simplest) **phase shift** for the following function using:



a) sine as the base curve

$$d = -60^\circ$$

$$(x + 60^\circ)$$

b) cosine as the base curve

$$d = +30^\circ$$

$$(x - 30^\circ)$$

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Ex 8) Determine the simplest sinusoidal equation for the following function, using:

$$C = +1$$

$$a = 3$$

$$\text{period} = 180^\circ$$

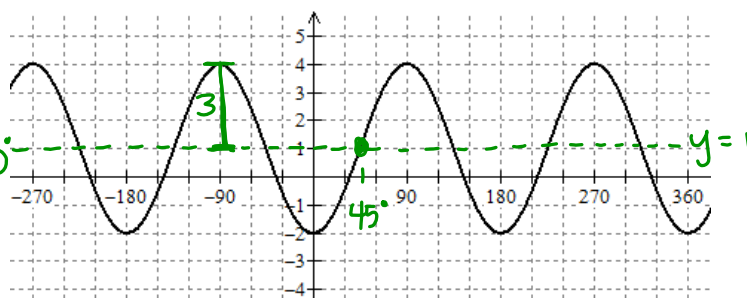
$$K = \frac{360^\circ}{\text{period}}$$

$$K = 360^\circ \div 180 = 2$$

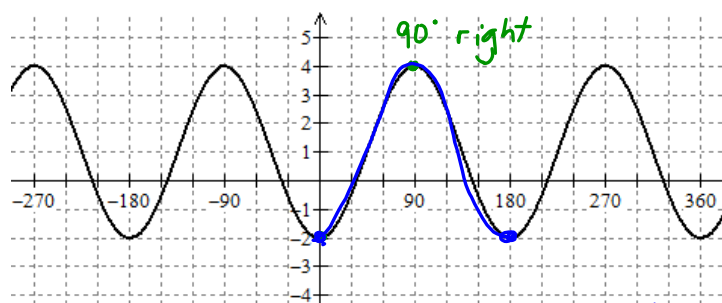
a) sine as the base curve

$$d = +45^\circ$$

$$g(x) = 3 \sin[2(x - 45^\circ)] + 1$$



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$a = 3$   
 $C = +1$   
 $K = 2$  } same as above

$$d = 90^\circ$$

or  $d = 0$  if we

RITXA

correct, but not ideal.

b) cosine as the base curve

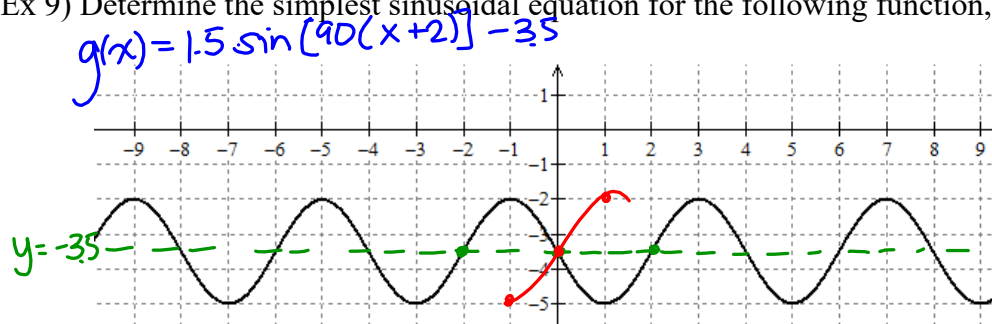
$$g(x) = 3 \cos[2(x - 90^\circ)] + 1$$

$$g(x) = -3 \cos 2x + 1$$

ideal answer

May 3-10:53 AM

Ex 9) Determine the simplest sinusoidal equation for the following function, using:



a) sine as the base curve

$$C = -3.5$$

$$a = 1.5$$

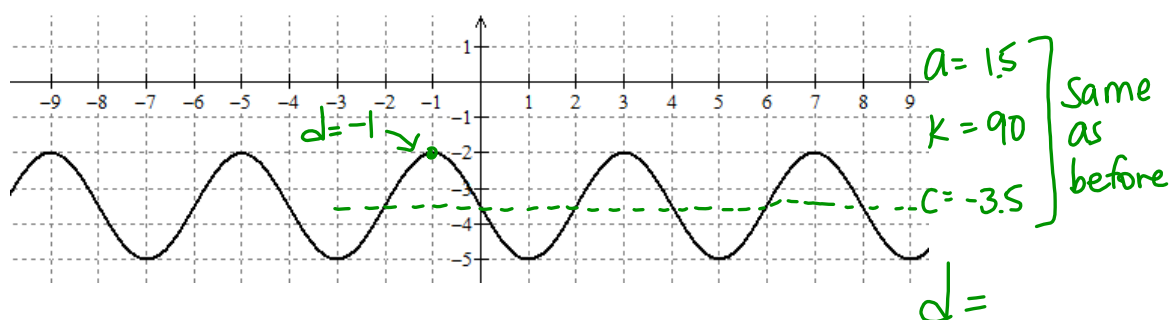
$$k = 90$$

$$d = 0 \text{ if I RITXA}$$

$$\frac{360^\circ}{\text{period}} = \frac{360^\circ}{4}$$

$$g(x) = -1.5 \sin 90x - 3.5$$

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b) cosine as the base curve

$$g(x) = 1.5 \cos [90(x+1)] - 3.5$$

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Ex 10) Determine a sinusoidal equation for a function with the following properties:  
amplitude 3 units, minimum at (0, -4), period of  $90^\circ$

a) using sine as the base curve

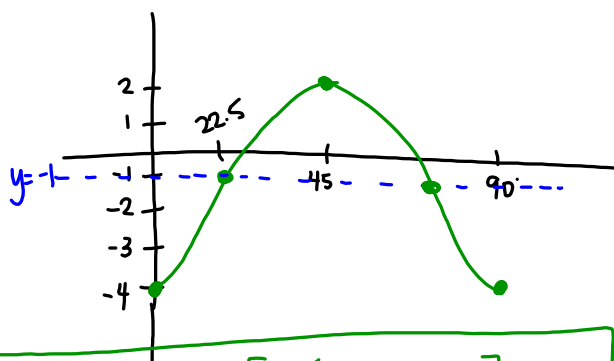
$$a = 3$$

$$c = -1$$

$$K = \frac{360^\circ}{90}$$

$$K = 4$$

$$d = +22.5$$



$$g(x) = 3 \sin [4(x - 22.5)] - 1$$

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Ex 10) Determine a sinusoidal equation for a function with the following properties:  
amplitude 3 units, minimum at (0, -4), period of  $90^\circ$

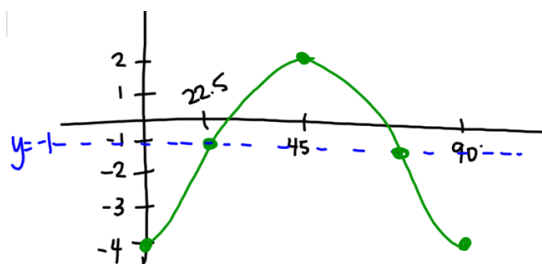
b) using cosine as the base curve

$$a = 3$$

$$K = 4$$

$$c = -1$$

$$d = 0 \quad \text{* if the graph is RITXA}$$



$$g(x) = -3 \cos 4x - 1$$

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## HW U4L5 Day 2:

1. Handout *\*there are a few typos in the answer key, so please refer to this to check your answers:*

$$\begin{array}{l}
 1. f(\theta) = -3 \sin(4\theta) + 1 \quad 2. f(\theta) = -\cos\left(\frac{1}{2}\theta\right) - 2 \quad 3. f(\theta) = 8 \cos\left[\frac{1}{3}(\theta - 30^\circ)\right] + 3 \quad 4. f(\theta) = 2 \sin[6(\theta + 7.5^\circ)] + 5 \text{ or } f(\theta) = 2 \cos[6(\theta + 7.5^\circ)] + 5 \\
 5. f(\theta) = 4 \sin\left[\frac{3}{4}(\theta - 90^\circ)\right] - 1 \quad 6. f(\theta) = 5 \sin 30\theta + 2 \quad 7. f(\theta) = \frac{5}{2} \sin[15(\theta - 5^\circ)] + \frac{7}{2} \quad 8. f(\theta) = 6 \cos[36(\theta + 1^\circ)] - 3 \\
 9. f(\theta) = 4 \sin\left(\frac{1}{2}\theta\right) + 2 \text{ or } f(\theta) = 4 \cos\left(\frac{1}{2}\theta\right) + 2 \quad 10. f(\theta) = 6 \sin(8\theta) - 2 \text{ or } f(\theta) = 6 \cos(8\theta) - 2 \\
 11. f(\theta) = 3 \sin(\theta - 30^\circ) + 9 \text{ or } f(\theta) = 3 \cos(\theta - 30^\circ) + 9 \quad 12. f(\theta) = 8 \sin \theta + 5 \text{ or } f(\theta) = 8 \cos(\theta - 90^\circ) + 5 \\
 13. f(\theta) = 2 \sin\left[\frac{1}{2}(\theta + 180^\circ)\right] + 1 \text{ or } f(\theta) = 2 \cos\left(\frac{1}{2}\theta\right) + 1 \quad 14. f(\theta) = 4 \sin 3(\theta - 30^\circ) + 10 \text{ or } f(\theta) = -4 \cos 3\theta + 10 \\
 15. f(\theta) = 6 \sin 2(\theta + 45^\circ) - 5 \text{ or } f(\theta) = 6 \cos 2\theta - 5
 \end{array}$$

2. p.383 #5

3. p. 391 #1, 3, 4, 6, 7 *Correction: 1b.  $\cos(x-90)+2$*

4. Sign and correct transformation quizzes