

Homework answers (Handouts)

#1 Functions: A, B, C, D, F, G, I, K, M, P, Q

#1 Non-Functions: E, H, J, L, N, O, R

#2 Functions: 2, 3, 5, 7, 8, 10

#2 Non-Functions: 1, 4, 6, 9

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Skill Builder: Factoring Polynomials



- Factoring means changing a quadratic relation from standard form $f(x) = ax^2 + bx + c$ into factored form

$$f(x) = a(x - r)(x - s)$$

- Remember! ALWAYS look for **GREATEST COMMON FACTORS** first!
- THEN FACTOR whatever is INSIDE THE BRACKETS, if possible.

Example 1: Factor $x^2 - 14x + 45$

$$\begin{array}{l} M +45 \\ A -14 \\ x -9 \\ x -5 \end{array}$$

$$= (x - 9)(x - 5)$$

Example 3: Factor $3x^2 - 11x - 4$

$$\begin{array}{l} M -12 \\ A -11 \\ x -12 \rightarrow \frac{3x}{-12} \rightarrow \frac{x}{-4} \\ x +1 \rightarrow \frac{3x}{+1} \rightarrow \frac{3x}{+1} \end{array}$$

$$= (x - 4)(3x + 1)$$

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Example 4: Factor $9x^2 - 25$

DOS \swarrow 2 terms
 \searrow both $\sqrt{\quad}$
 minus

$$(3x+5)(3x-5)$$

Example 7: Factor $4a^2 - 12x + 9$

$$(2a-3)^2$$

P S T \swarrow 3 terms
 \searrow front & back
 are $\sqrt{\quad}$
 2

$$\square^2 + 2\square\triangle + \triangle^2$$

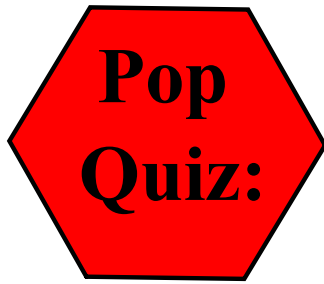
$$(\square + \triangle)^2$$

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Do the rest on your own now.

2. $(y-3)(y+5)$
5. $(4-t)(4+t)$
6. $4(x-2)(x+2)$
8. $(x+2)^2$
9. $2(3x-4)(3x+4)$
10. $(3x-4)(2x+3)$
11. $2(3x-2)(x+1)$

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Factor the following **as much as possible!**

1) $x^2 - 14x + 45$

2) $y^2 + 2y - 15$

3) $3x^2 - 11x - 4$

4) $9x^2 - 25$

5) $16 - t^2$

6) $4x^2 - 16$

7) $4a^2 - 12a + 9$

8) $x^2 + 4x + 4$

9) $18x^2 - 32$

10) $6x^2 + x - 12$

11) $6x^2 + 2x - 4$

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Recall: Distributive property

$$a(b + c) = ab + ac$$

You distribute the **a** to the **b** and, then you distribute the **a** to the **c**.



Here is a different way to look at expanding It will help you understand factoring by grouping on the next page:

Expand $(x + 2)(y + z)$

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Factoring by Grouping (should have 4 terms in polynomial)

- Separate the four terms into two groups of two or three terms (you may have to rearrange the terms)
 - For groups of two terms
 - Factor each group so that each has the same common factor remaining
 - Factor this common factor into one bracket and the remaining terms into another bracket
 - For groups of three terms
 - Factor a trinomial into two identical brackets which can then be written as $()^2$.
 - This may result in a difference of squares which can then be factored into two large brackets.
 - Simplify the two large brackets as much as possible, eliminating any brackets within.

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Example – factor each expression by grouping

a) $xy + 6x + 5y + 30$

$$x(y+6) + 5(y+6)$$

$$(y+6)(x+5)$$

b) $2ab + 2a - 3b - 3$

$$2a(b+1) - 3(b+1)$$

$$(b+1)(2a-3)$$

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$$c) \underbrace{x^3 + x^2 + x + 1}$$

$$x^2(x+1) + 1(x+1)$$

$$\boxed{(x+1)(x^2+1)}$$

$$PST \rightarrow d) \underbrace{y^2 - 4y + 4} - \underbrace{16x^2}$$

$$(y-2)^2 - 16x^2$$

$$DOS: (y-2)^2 - (4x)^2$$

$$\boxed{(y-2+4x)(y-2-4x)}$$

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$$e) 8x^4 - 18y^2 - 60y - 50$$

$$2(4x^4 - \underbrace{9y^2 - 30y - 25})$$

$$2(4x^4 - (\underbrace{9y^2 + 30y + 25})_{PST})$$

$$2(4x^4 - (3y+5)^2) \text{ DOS}$$

$$2(2x^2 + 3y+5)(2x^2 - (3y+5))$$

$$\boxed{2(2x^2 + 3y+5)(2x^2 - 3y - 5)}$$

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$$f) 2m^2 + 10m + 10n - 2n^2$$

$$2(m^2 + 5m + 5n - n^2)$$

$$2(\underbrace{m^2 - n^2} + \underbrace{5m + 5n})$$

$$2[(\underbrace{m+n})(\underbrace{m-n}) + 5(\underbrace{m+n})]$$

$$\boxed{2(m+n)(m-n+5)}$$

HW:

1. p. 102 #2 (just factor, don't describe), 4-7, 9
challenge: 14
2. Study for the quiz tomorrow on the first 3 lessons