

# The Derivative

**Definition:** The derivative is the slope of the tangent line to the curve at any point  $x$ . It can also be defined as the rate of change at any point  $x$ .

The function must be defined at the point  $x$ .

Examples of where the function is **not** defined include: Vertical Asymptotes (V. A.) and holes.

Examples of where the function is **not** differentiable are sharp corners, endpoints, vertical tangents.

## 1<sup>st</sup> Principles Definition of the Derivative

### Lagrange Notation

$$y' = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

**or**

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

### Leibniz Notation

$$\frac{dy}{dx} = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

**Example 1:** Determine  $y'$  if  $y = \sqrt{x+1}$ .

**Example 2:** Determine  $\frac{dy}{dx}$  at  $x=3$  if  $y = 2x^2 + 6x + 11$ .