Section 2.5 – Linear and Non-Linear Relationships

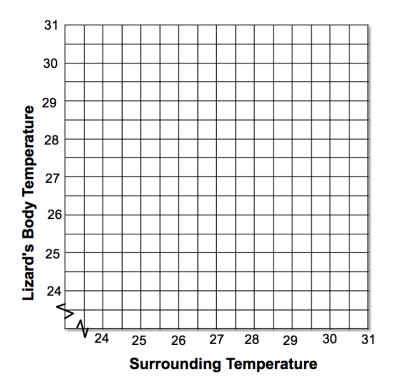
MPM1D

Part 1: Do It Now

The gymnophthalmid lizard lives in the Amazon rainforest. Recent research found that this lizard keeps its body temperature close to the temperature of its surroundings. The table lists data from this research.

Surrounding Temperature (°C)	25.0	24.8	27.9	30.3	28.2	24.8	25.6	29.9	25.5	28.4	28.5	28.0	27.9
Lizard's Body Temperature (°C)	26.2	28.2	29.7	30.3	29.8	28.3	27.6	30.8	29.5	30.0	28.8	28.7	29.0

a) Graph the data



- **b)** Draw a line of best fit
- **c)** Estimate the lizard's body temperature if the surrounding temperature is 26°C. Is this interpolation or extrapolation?
- **d**) Estimate the lizard's temperature if the surrounding temperature is 31 degrees Celcius. Is this interpolation or extrapolation?

Example 1:

A scatter plot of the following ten points is given below. 3 4 5 6 10 x 1 y 1.1 1.3 1.8 2.6 3.7 4.5 5.7 7.1 8.9 12.3 14 12 10 8 6 4 2 3 4 5 6 7 8 9 10 11 12 13 14 15

Gandolf predicts that when x is 11, y will be 11. Merlyn predicts that when x is 11, y will be 15.

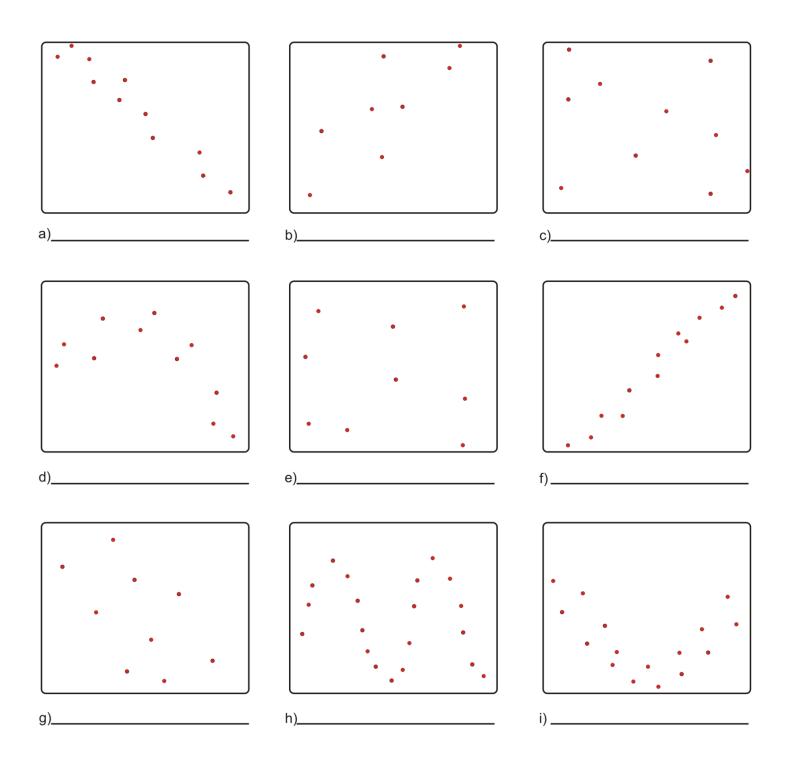
Who is correct? Why?

Many non-linear relations can be modeled with a ______. You can draw curves of best fit using the same method as for a line of best fit. A curve of best fit should:

- 1. Pass through or close to as many points as possible,
- 2. Any points that are not on the curve should be distributed evenly above and below it.

Example 2: Describing Scatter Plots and Lines/Curves of Best Fit

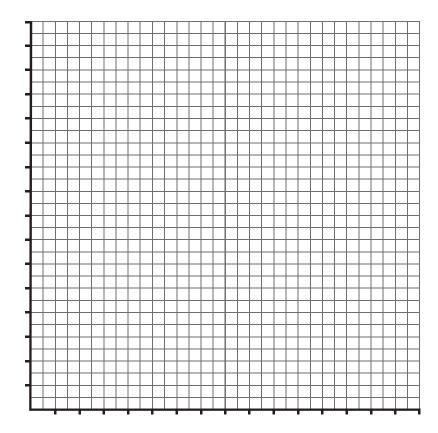
Draw a line or curve of best fit for each of the scatter plots below, if possible. Write two or three key words to describe each relation on the line below the scatter plot. (*positive relationship, negative relationship, no relationship, strong, weak, linear, non-linear*)



Example 3: Test the hypothesis: The older you are, the more money you earn.

Plot the data on the scatter plot below, choosing appropriate scales and labels.

Age	Earnings (\$)
25	22000
30	26500
35	29500
37	29000
38	30000
40	32000
41	35000
45	36000
55	41000
60	41000
62	42500
65	43000
70	37000
75	37500



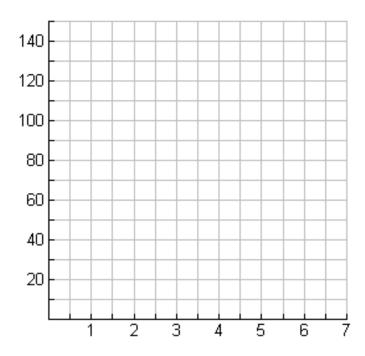
- **a)** Draw a curve of best fit. Describe the trend in the data.
- **b)** Does the data support the hypothesis? Give reasons to support your answer. (Refer to the scatter plot.)

c) Explain why the data for ages over 65 do not correspond with the hypothesis.

Example 4: A skydiver jumps from an airplane. The distance fallen and time taken are recorded in the table.

Time (<i>s</i>)	Distance (m)
0	0
1	5
2	19
3	42
4	74
5	115

a) Draw a scatter plot of the relation and draw a line or curve of best fit.



b) Classify the relation as linear or non-linear. Explain your choice.

c) How far will the skydiver have fallen in 3.5 s?