# L7 – 6.3 Transformations of Exponential and Logarithmic Functions MHF4U

### **Part 1: Properties of Exponential Functions**

**General Equation:**  $y = a(b)^{k(x-d)} + c$  where the base function is  $y = b^x$ 

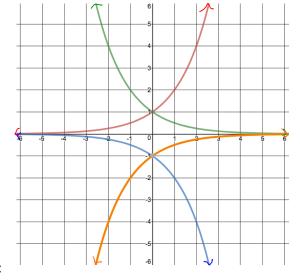
There are 4 possible shapes for an exponential function



**2)** 
$$a > 0$$
 and  $0 < b < 1$  (ex.  $y = \left(\frac{1}{2}\right)^x$ )

3) 
$$a < 0$$
 and  $b > 1$  (ex.  $y = -1(2)^x$ )

**4)** 
$$a < 0$$
 and  $0 < b < 1$  (ex.  $y = -1\left(\frac{1}{2}\right)^x$ )



To graph the base function  $y = b^x$ , Find the following key features:

- Horizontal asymptote
  - o Starts at y = 0 and can be shifted by c
- y intercept
  - o set x = 0 and solve
- At least one other point to be sure of shape
  - Common to choose x = 1 and solve for y

You can then use transformational properties of a, k, d, and c to graph a transformed function

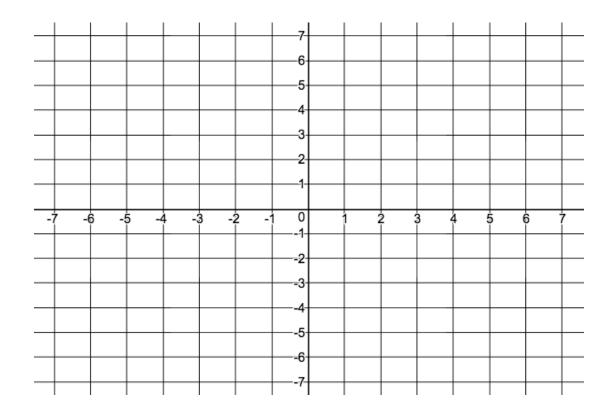
### **Part 2: Transformations of Exponential Functions**

**Example 1:** Sketch the graph of  $f(x) = 2(3)^{x+4} - 5$  and  $g(x) = -3^{\frac{1}{2}x} + 4$  using transformations

| $y = 3^x$ |   |  |
|-----------|---|--|
| x         | у |  |
|           |   |  |
|           |   |  |
|           |   |  |
|           |   |  |

| $f(x) = 2(3)^{x+4} - 5$ |  |
|-------------------------|--|
|                         |  |
|                         |  |
|                         |  |
|                         |  |
|                         |  |

| $g(x) = -3^{\frac{1}{2}x} + 4$ |  |  |
|--------------------------------|--|--|
|                                |  |  |
|                                |  |  |
|                                |  |  |
|                                |  |  |
|                                |  |  |



#### **Part 3: Properties of Logarithmic Functions**

**General Equation:**  $y = a \log_b [k(x-d)] + c$  where the base function is  $y = \log_b x$ 

Remember that  $y = \log_b x$  is the inverse of the exponential function  $y = b^x$ 

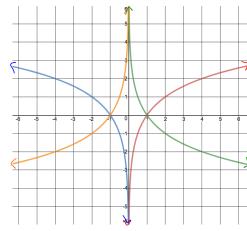
There are 4 possible shapes for a logarithmic function

1) 
$$k > 0$$
 and  $b > 1$  (ex.  $y = \log_2(x)$ )

**2)** 
$$k > 0$$
 and  $0 < b < 1$  (ex.  $y = \log_{0.5}(x)$ )

3) 
$$k < 0$$
 and  $b > 1$  (ex.  $y = \log_2(-x)$ )

**4)** 
$$k < 0$$
 and  $0 < b < 1$  (ex.  $y = \log_{0.5}(-x)$ )



To graph the base function  $y = \log_b x$ , Find the following key features:

- Vertical asymptote
  - Starts at x = 0 and can be shifted by d
- x intercept
  - o set y = 0 and solve
- At least one other point to be sure of shape
  - Common to choose y = 1 and solve for x

## Part 4: Transformations of Logarithmic Functions

**Example 2:** Sketch the graph of  $f(x) = -4\log_3(x) + 2$  and  $g(x) = \log_3[-(x+2)] - 4$  using transformations

| $y = \log_3(x)$  |   |  |
|------------------|---|--|
| $\boldsymbol{x}$ | у |  |
|                  |   |  |
|                  |   |  |
|                  |   |  |
|                  |   |  |

| $f(x) = -4\log_3(x) + 2$ |  |
|--------------------------|--|
|                          |  |
|                          |  |
|                          |  |
|                          |  |
|                          |  |

| $g(x) = \log_3[-(x+2)] - 4$ |  |
|-----------------------------|--|
|                             |  |
|                             |  |
|                             |  |
|                             |  |
|                             |  |

