## W2 - 2.1 - Synthetic Division

MHF4U

SOLUTIONS

be used to check the division.

**a)** 
$$x^3 - 7x - 6$$
 divided by  $x - 3$ 

c) 
$$6x^4 + 13x^3 - 34x^2 - 47x + 28$$
 divided by  $x + 3$ 

-3 6 13 -34 -47 28  
1 -18 15 57 -30 +  
16 -5 -19 10 -2  

$$\chi^3 \chi^2 \chi \# R$$

$$(x^4 + 13x^3 - 34x^2 - 47x + 25)$$
  
=  $(x+3)(6x^3 - 5x^2 - 19x + 10) - 2$ 

e) 
$$12x^4 - 56x^3 + 59x^2 + 9x - 18$$
 divided by  $2x + 1$ 

**b)** 
$$2x^3 - 7x^2 - 7x + 19$$
 divided by  $x - 1$ 

$$2x^{3}-7x^{2}-7x+19=(x-1)(2x^{2}-5x-12)+7$$

**d)** 
$$2x^3 + x^2 - 22x + 20$$
 divided by  $2x - 3$ 

f) 
$$6x^3 - 15x^2 - 2x + 5$$
 divided by  $2x - 5 = 2(x - 5)$ 

$$63-15x^2-2x+5=(2x-5)(3x^2-1)$$

**g)** 
$$x^3 - 2x + 1$$
 divided by  $x - 4$ 

**h)** 
$$x^3 + 2x^2 - 6x + 1$$
 divided by  $x + 2$ 

$$\sqrt{x^3-2x+1}=(x-4)(x^2+4x+14)+57$$

2) Divide  $x^4 - 16x^3 + 4x^2 + 10x - 11$  by each of the following binomials...

a) 
$$x - 2$$

**b)** 
$$x + 4$$

$$x^{4} - 16x^{3} + 4x^{2} + 10x - 11$$

$$= (x - 2)(x^{3} - (4x^{2} - 24x - 38) - 87$$

$$=(x-2)(x^{3}-14x^{2}-24x-38)-47$$

$$=(x-2)(x^{3}-14x^{2}-24x-38)-47$$

$$=(x+4)(x^{3}-20x^{2}+84x-326)+1293$$

3) Are either of the binomials in question #2 factors of  $x^4 - 16x^3 + 4x^2 + 10x - 11$ ? Explain.

No, because there is a non-zero Renainder for each.

## **ANSWER KEY**

(a) 
$$x^3 - 7x - 6 = (x - 3)(x^2 + 3x + 2)$$
 b)  $2x^3 - 7x^2 - 7x + 19 = (x - 1)(2x^2 - 5x - 12) + 7$ 

c) 
$$6x^4 + 13x^3 - 34x^2 - 47x + 28 = (x+3)(6x^3 - 5x^2 - 19x + 10) - 2$$

d) 
$$2x^3 + x^2 - 22x + 20 = (2x - 3)(x^2 + 2x - 8) - 4$$

e) 
$$12x^4 - 56x^3 + 59x^2 + 9x - 18 = (2x + 1)(6x^3 - 31x^2 + 45x - 18)$$
 f)  $6x^3 - 15x^2 - 2x + 5 = (2x - 5)(3x^2 - 1)$ 

g) 
$$x^3 - 2x + 1 = (x - 4)(x^2 + 4x + 14) + 57$$
 h)  $x^3 + 2x^2 - 6x + 1 = (x + 2)(x^2 - 6) + 13$ 

2)a) 
$$x^4 - 16x^3 + 4x^2 + 10x - 11 = (x - 2)(x^3 - 14x^2 - 24x - 38) - 87$$

**b)** 
$$x^4 - 16x^3 + 4x^2 + 10x - 11 = (x + 4)(x^3 - 20x^2 + 84x - 326) + 1293$$

3) No, because for each division problem, there is a remainder.