L4 - 7.1/7.2 - Solving Exponential Equations MHF4U

Part 1: Changing the Base of Powers

Exponential functions can be written in many different ways. It is often useful to express an exponential expression using a different base than the one that is given.

Example 1: Express each of the following in terms of a power with a base of 2.

a) 8

b) 4^3

- c) $\sqrt{16} \times (\sqrt[5]{32})^3$
- **d)** 12

Part d) shows that any positive number can be expressed as a power of any other positive number.

Example 2: Solve each equation by getting a common base

Remember: if $x^a = x^b$, then a = b

a)
$$4^{x+5} = 64^x$$

b)
$$4^{2x} = 8^{x-3}$$

Part 2: Solving Exponential Equations

When you have powers in your equation with	n different bases and it is difficult to write with the sa	me base, it
may be easier to solve by taking the	of both sides and applying the	of
logarithms to remove the variable from the $_$	·	

Example 3: Solve each equation

a)
$$4^{2x-1} = 3^{x+2}$$

Take log of both sides

Use power law of logarithms

Use distributive property to expand

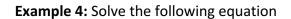
Move variable terms to one side

Common factor

b)
$$2^{x+1} = 3^{x-1}$$

Part 3: Applying the Quadratic Formula

Sometimes there is no obvious method of solving an exponential equation. If you notice two powers with the same base and an exponent of x, there may be a hidden quadratic.



Multiply both sides by 2^x Distribute

Rearrange in to standard form $ax^2 + bx + c = 0$ Solve using quadratic formula

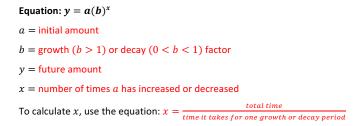
Don't forget to simplify the radical expression

Now substitute 2^x back in for k and solve

Case 1 Case 2

Part 4: Application Question

Remember:



Example 5: A bacteria culture doubles every 15 minutes. How long will it take for a culture of 20 bacteria to grow to a population of 163 840?

Example 6: One minute after a 100-mg sample of Polonium-218 is placed into a nuclear chamber, only 80-mg remains. What is the half-life of polonium-218?