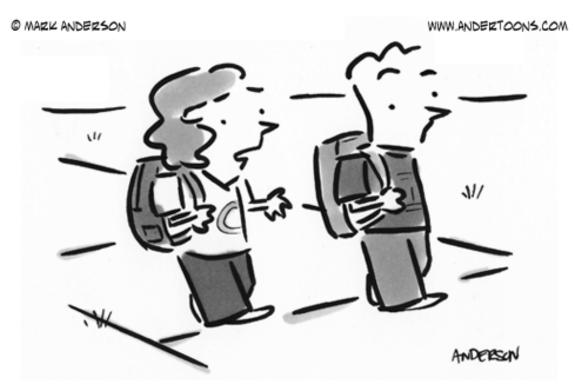
# Chapter 2- Factor Theorem and Inequalities

*WORKBOOK* 

MHF4U



"I don't like long division; I always feel bad for the remainders."

- 1) Use the remainder theorem to determine the remainder when  $2x^3 + 7x^2 8x + 3$  is divided by each binomial.
- a) x + 1

**b)** x - 2

c) x + 3

**2)a)** Divide  $x^3 + 3x^2 - 2x + 5$  by x + 1. Express the result in quotient form.

- **b)** Write the corresponding statement that can be used to check the division.
- 3) Divide  $3x^4 4x^3 6x^2 + 17x 8$  by 3x 4. Express the result in quotient form.

**b)** Write the corresponding statement that can be used to check the division.

4) Perform each division. Express the result in quotient form.

**a)** 
$$x^3 + 7x^2 - 3x + 4$$
 divided by  $x + 2$ 

**b)** 
$$6x^3 + x^2 - 14x - 6$$
 divided by  $3x + 2$ 

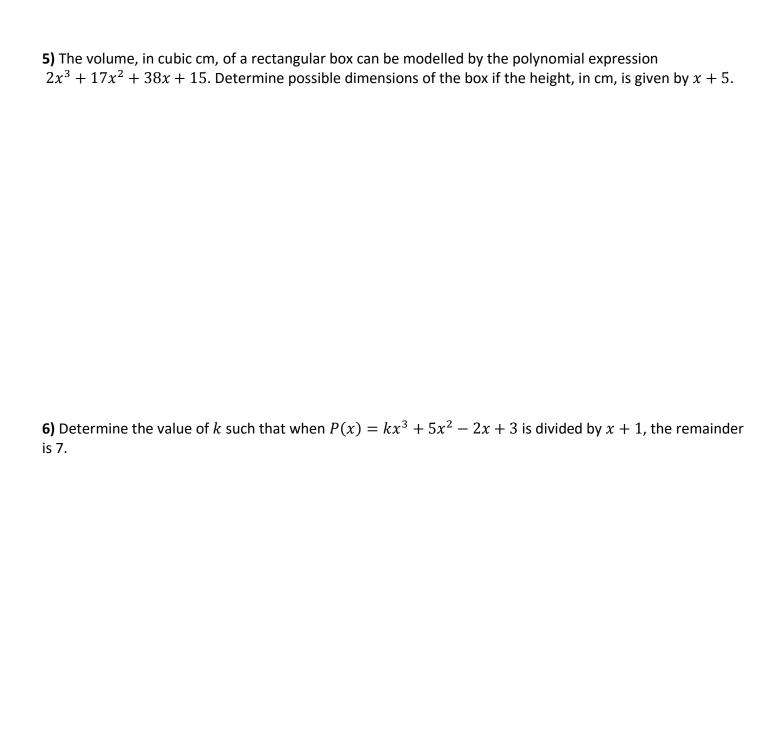
**c)** 
$$10x^3 + 11 - 9x^2 - 8x$$
 divided by  $5x - 2$  **d)**  $11x - 4x^4 - 7$  divided by  $x - 3$ 

**d)** 
$$11x - 4x^4 - 7$$
 divided by  $x - 3$ 

**e)** 
$$6x^3 + x^2 + 7x + 3$$
 divided by  $3x + 2$ 

**f)** 
$$8x^3 + 4x^2 - 31$$
 divided by  $2x - 3$ 

**g)** 
$$6x^2 - 6 + 8x^3$$
 divided by  $4x - 3$ 



## W2 - 2.1 - Synthetic Division

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1) Calculate each of the following using synthetic division. Express your answer using the statement that could be used to check the division.

**a)** 
$$x^3 - 7x - 6$$
 divided by  $x - 3$ 

**b)** 
$$2x^3 - 7x^2 - 7x + 19$$
 divided by  $x - 1$ 

c) 
$$6x^4 + 13x^3 - 34x^2 - 47x + 28$$
 divided by  $x + 3$  d)  $2x^3 + x^2 - 22x + 20$  divided by  $2x - 3$ 

**d)** 
$$2x^3 + x^2 - 22x + 20$$
 divided by  $2x - 3$ 

e) 
$$12x^4 - 56x^3 + 59x^2 + 9x - 18$$
 divided by  $2x + 1$  f)  $6x^3 - 15x^2 - 2x + 5$  divided by  $2x - 5$ 

**f)** 
$$6x^3 - 15x^2 - 2x + 5$$
 divided by  $2x - 5$ 

**g)** 
$$x^3 - 2x + 1$$
 divided by  $x - 4$ 

**h)**  $x^3 + 2x^2 - 6x + 1$  divided by x + 2

2) Divide  $x^4 - 16x^3 + 4x^2 + 10x - 11$  by each of the following binomials...

**a)** 
$$x - 2$$

**b)** 
$$x + 4$$

3) Are either of the binomials in question #2 factors of  $x^4 - 16x^3 + 4x^2 + 10x - 11$ ? Explain.

## W3 - 2.2 - Factor Theorem

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1) Determine if x + 3 is a factor of each polynomial:

**a)** 
$$x^3 + x^2 - x + 6$$

**b)** 
$$2x^3 + 9x^2 + 10x + 3$$

**c)** 
$$x^3 + 27$$

2) Find possible factors of the following polynomials using integral zero theorem. Then, factor the polynomial.

a) 
$$x^3 + 3x^2 - 6x - 8$$

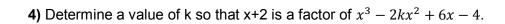
**b)** 
$$x^3 + 4x^2 - 15x - 18$$
 **c)**  $x^3 - 3x^2 - 10x + 24$ 

c) 
$$x^3 - 3x^2 - 10x + 24$$

3) Factor by grouping:

**a)** 
$$x^3 + x^2 - 9x - 9$$

**b)** 
$$2x^3 - x^2 - 72x + 36$$



a) 
$$3x^3 + x^2 - 22x - 24$$

**b)** 
$$2x^3 - 9x^2 + 10x - 3$$

c) 
$$6x^3 - 11x^2 - 26x + 15$$

**d)** 
$$4x^3 + 3x^2 - 4x - 3$$

6) Factor each polynomial

a) 
$$2x^3 + 5x^2 - x - 6$$

b) 
$$4x^3 - 7x - 3$$

c) 
$$x^4 - 15x^2 - 10x + 24$$

# W4 - 2.3 - Solving Polynomial Equations MHF4U

1) Determine the solutions of the following polynomials.

a) 
$$(3x + 2)(x + 9)(x - 2) = 0$$

b) 
$$(x^2 + 1)(x - 4) = 0$$

**2)** Determine the solutions of the following polynomials by factoring. Use the tools you have learned this unit to help you. (remainder theorem, integral zero theorem, division etc.)

**a)** 
$$x^3 - 4x^2 - 3x + 18 = 0$$

b) 
$$x^3 - 3x^2 - 4x + 12 = 0$$

c) 
$$x^4 - x^3 - 11x^2 + 9x + 18 = 0$$

d) 
$$x^3 - 64 = 0$$

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

**e)** 
$$2x^3 - 7x^2 + 10x - 5 = 0$$

**3)** Solve each equation by first factoring the sum or difference of cubes.

**a)** 
$$x^3 - 8 = 0$$

**b)** 
$$x^3 + 27 = 0$$

4) Solve by factoring

a) 
$$x^3 - 4x^2 - 7x + 10 = 0$$

**b)** 
$$2x^3 - 11x^2 + 12x + 9 = 0$$

c)  $x^4 - x^3 - 2x - 4 = 0$ 

# W5 – 2.4 – Families of Polynomial Functions MHF4U

- 1) The zeros of a quadratic function are -7 and -3.
- a) Determine an equation for the family of quadratic functions with these zeros.
- b) Write equations for two functions that belong to this family.
- c) Determine an equation for the member of the family that passes through the point (2, 18).
- 2) Examine the following functions. Which function does not belong to the same family?

a) 
$$y = 1.5(x+4)(x-5)(x-2)$$

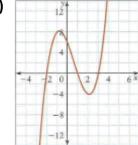
**b)** 
$$y = -1.5(x-2)(x-5)(x+4)$$

c) 
$$y = 1.5(x-2)(x+4)(x-2)$$

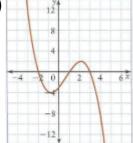
**d)** 
$$y = 3(x-5)(x-2)(x+4)$$

**3)** The graphs of four polynomial functions are given. Which graphs represent functions that belong to the same family?

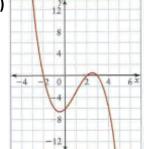




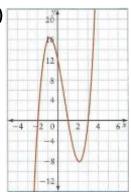
B)



C)

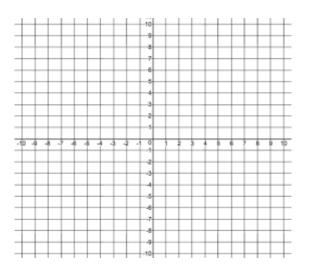


D)

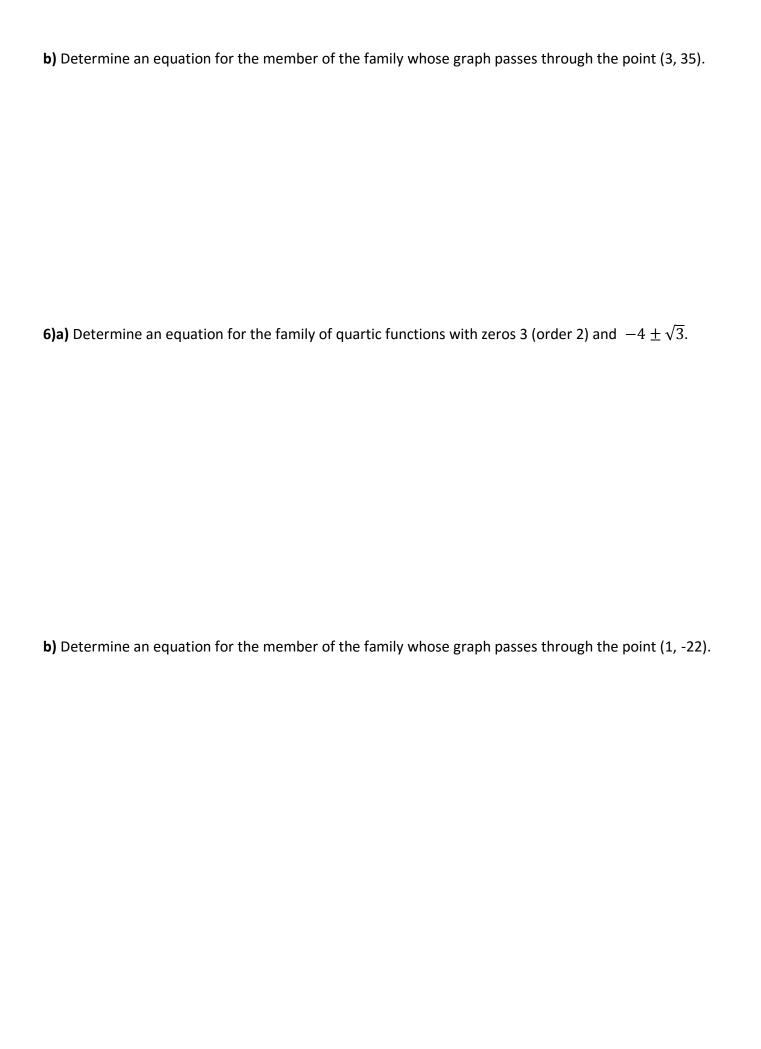


- **4)a)** Determine an equation for the family of cubic functions with zeros -2, -1, and  $\frac{1}{2}$
- **b)** Write equations for two functions that belong to this family.
- c) Determine an equation for the member of the family whose graph has a y-intercept of 6.

d) Sketch a graph of the function from part c).

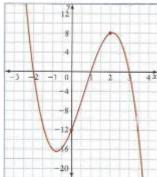


**5)a)** Determine an equation for the family of cubic functions with zeros  $1 \pm \sqrt{2}$  and  $-\frac{1}{2}$ 

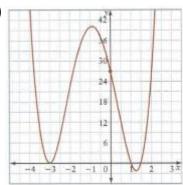


## 7) Determine an equation for each of the following functions





b)



## W6 – 2.5 – Solving Inequalities

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1) Solve each linear inequality

**a)** 
$$x + 3 \le 5$$

**b)** 
$$7x < 4 + 3x$$

2) Solve each inequality by graphing

a) 
$$(x+3)(x-2) > 0$$

**b)** 
$$(x+2)(3-x)(x+1) < 0$$

3) Solve each of the following polynomial inequalities

a) 
$$x^2 - 7x + 10 \ge 0$$

**b)** 
$$x^3 + 6x^2 - 16x > 0$$

c) 
$$-x^2 + 36 \ge 0$$

**d)** 
$$x^4 - 26x^2 + 25 > 0$$

**e)** 
$$x^3 - 3x^2 \ge 25x - 75$$

$$f) - x^3 + 28x + 48 \ge 0$$

**g)** 
$$x^3 - 2x^2 - 5x + 6 < 0$$

**h)** 
$$5x^3 - 12x^2 - 11x + 6 \le 0$$

**4)** The price, p, in dollars, of a stock t years after 1999 can be modelled by the function  $p(t)=0.5t^3-5.5t^2+14t$ . When will the stock be more than \$90? You may use technology to help you determine the solution.