W4 – 4.5 Prove Trig Identities
MHF4U

Prove each identity using the space on the following pages.

a) $\sin(x+y) = \sin x \cos y + \cos x \sin y$

b) $\tan(x-y) = \frac{\tan x - \tan y}{1+\tan x \tan y}$

c) $\sin(2x) = 2\sin x \cos x$

d) $\cos(2x) = \cos^2 x - \sin^2 x$

e) $\cot\theta - \tan\theta = 2\cot(2\theta)$

f) $\frac{\sin(2\theta)}{1-\cos(2\theta)} = \cot\theta$

g) $\sin x \sec x = \tan x$

h) $\frac{1-\sin x}{\cos x} = \frac{\cos x}{1+\sin x}$

i) $\frac{\sec\theta - 1}{1-\cos\theta} = \sec\theta$

j) $\frac{\sin x - \cos x}{\cos x} + \frac{\sin x + \cos x}{\sin x} = \sec x \csc x$

k) $\frac{1-\sin^2 x \cos^2 x}{\cos^4 x} = \tan^4 x + \tan^2 x + 1$

l) $\frac{\cos(2x)+1}{\sin(2x)} = \cot x$

m) $\cot\theta - \tan\theta = 2\cot(2\theta)$

n) $(\sin x + \cos x)^2 = 1 + \sin(2x)$

o) $\frac{2\tan x}{1+\tan^2 x} = \sin(2x)$

p) $\sin\left(\frac{\pi}{4}+x\right) + \sin\left(\frac{\pi}{4}-x\right) = \sqrt{2}\cos x$

q) $\cos^4 x - \sin^4 x = \cos(2x)$

r) $\csc(2x) + \cot(2x) = \cot x$

s) $\cos(2x) = 2\cos^2 x - 1$

t) $\sin\left(\frac{3\pi}{2}-x\right) = -\cos x$

u) $\frac{\cos(2x)+1}{\sin(2x)} = \cot x$

v) $\cot x + \tan x = 2\csc(2x)$