

Algorithm 4.8 (Hopcroft):

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 $P := [Q]_{E_0};$   
 $L := (\text{if } (|F| \leq |Q \setminus F|) \text{ then } \{F\} \text{ else } \{Q \setminus F\} \text{ fi}) \times V;$   
{invariant:  $[Q]_E \sqsubseteq P \sqsubseteq [Q]_{E_0} \wedge L \subseteq (P \times V)$   
     $\wedge (\forall Q_0, Q_1, a : Q_0 \in Q \wedge (Q_1, a) \in L : \neg \text{Splittable}(Q_0, Q_1, a)) \Rightarrow (P = [Q]_E)}$   
do  $L \neq \emptyset \longrightarrow$   
    let  $Q_1, a : (Q_1, a) \in L;$   
     $P_{old} := P;$   
     $L := L \setminus \{(Q_1, a)\};$   
    {invariant:  $[Q]_E \sqsubseteq P \sqsubseteq P_{old}$ }  
    for  $Q_0 : Q_0 \in P_{old} \wedge \text{Splittable}(Q_0, Q_1, a)$  do  
         $Q'_0 := \{p : p \in Q_0 \wedge T(p, a) \in Q_1\};$   
         $P := P \setminus \{Q_0\} \cup \{Q_0 \setminus Q'_0, Q'_0\};$   
        for  $b : b \in V$  do  
            if  $(Q_0, b) \in L \longrightarrow L := L \setminus \{(Q_0, b)\} \cup \{(Q'_0, b), (Q_0 \setminus Q'_0, b)\}$   
            |  $(Q_0, b) \notin L \longrightarrow$   
                 $L := L \cup (\text{if } (|Q'_0| \leq |Q_0 \setminus Q'_0|) \text{ then } \{(Q'_0, b)\} \text{ else } \{(Q_0 \setminus Q'_0, b)\} \text{ fi})$   
            fi  
        rof  
    rof  
     $\{(\forall Q_0 : Q_0 \in P : \neg \text{Splittable}(Q_0, Q_1, a))\}$   
od  $\{P = [Q]_E\}$ 
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