Department of Mechanical and Aerospace Engineering MEE 440/AEE 521 – Flight Vehicle Performance/Dynamics Homework-4

1. For the aircraft assigned to you and use the corresponding aircraft data, provided drawings. Extract the relevant geometric parameters and provide estimates for all the longitudinal coefficients. Make sure to have all the necessary parameters required to compute the following parameters. Submit the homeowrk as a MATLAB CODE. Display only the required parameters.

Horizontal Tail Parameters

- **Vertical Parameters**
 - \bullet $c_{T_V} =$
 - \bullet $c_{R_V} =$
 - \bullet $b_V =$
 - $b_{2V} = 2 \times b_V$
 - $\Lambda_{LE_V} =$
 - $\lambda_V = \frac{c_{T_V}}{c_{R_V}} =$
 - $S_V = \frac{b_V}{2} c_R (1 + \lambda_V) =$
 - $S_{2V} = \frac{b_{2V}}{2} c_R (1 + \lambda_V) =$
 - $AR_V = \frac{b_{2V}^2}{S_{2V}} =$
 - $\bar{c}_V = \frac{2}{3}c_{R_V}\frac{1+\lambda_V+\lambda_V^2}{1+\lambda_V} =$
 - $x_{MAC_V} = \frac{b_{2V}}{6} \frac{(1+2\lambda_V)}{(1+\lambda_V)} \tan(\Lambda_{LE_V}) =$
 - $y_{MAC_V} = \frac{b_{2V}}{6} \frac{(1+2\lambda_V)}{(1+\lambda_V)} =$
 - $\tan(\Lambda_x) = \tan(\Lambda_{LE_V}) \frac{4x(1-\lambda_V)}{AR_V(1+\lambda_V)}$ - $\Lambda_{0.5_V} =$
 - $-\Lambda_{0.25_V} =$

- $r_1 =$
- $Z_H =$
- \bullet $\frac{b_V}{2*r_1} =$
- From Fig. $4.15 \Rightarrow c_1 =$
- \bullet $\frac{-Z_H}{b_V} =$
- $\bullet \ x_{AC_{H\to V}} = x_{MAC} + (0.25 \times \bar{c}_H)$
- $\bullet \ \frac{x_{AC_{H \to V}}}{\bar{c}_{V}} =$
- From Fig. $4.16 \Rightarrow c_2 =$
- $\frac{S_H}{.5*S_{2V}} =$
- From Fig. $4.18 \Rightarrow K_{HV} =$
- $A_{R_{V_{eff}}} = c_1 \times AR_V \times (1 + K_{HV} * (c_2 1)) =$
- \bullet $k_V =$
- \bullet $c_{L_{\alpha_{V|_{Mach}}}} =$
- $mach \times cos(\Lambda_{0.5}) =$
- $\bullet \ \frac{AR}{\cos(\Lambda_{0.5})} =$
- From Fig. 4.40 $\Rightarrow K_{M_{\Lambda}} =$
- A =
- \bullet $\frac{A}{b} =$
- From Fig. 4.41 $\Rightarrow K_f =$
- Using $\lambda, AR, \Lambda_{\frac{c}{2}}$ From Fig 4.39 $\Rightarrow \left(\frac{c_{l_{\beta}}}{c_{L_{1}}}\right)_{\Lambda_{c/2}} =$
- Using λ, AR From Fig $4.42 \Rightarrow \left(\frac{c_{l_{\beta}}}{c_{L_1}}\right)_{AR} =$
- $\Gamma_W =$

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- Using $\lambda, \Lambda_{0.5}$ From Fig $4.43 \Rightarrow \left(\frac{c_{l_{\beta}}}{\Gamma_W}\right) =$
- $mach \times cos(\Lambda_{0.5}) =$
- $\bullet \ \frac{AR}{\cos(\Lambda_{0.5})} =$
- From Fig. $4.44 \Rightarrow K_{M_{\Gamma}} =$
- Fuselage Average Height =
- Fuselage Average Width =
- $S_{f_{AVG}} = \pi \times \frac{FuselageAverageHeight}{2} \times \frac{FuselageAverageWidth}{2} =$
- $\bullet \ d = \sqrt{\frac{S_{f_{AVG}}}{0.7854}} =$
- $\left(\frac{\Delta c_{l_{\beta}}}{\Gamma_W}\right) = -0.005 \times AR \times \frac{d^2}{b^2} =$
- $Z_W =$
- $\left(\Delta c_{l_{\beta}}\right)_{Z_W} = \frac{1.2 \times \sqrt{AR}}{57.3} \times \frac{Z_w}{b} \times \frac{2d}{b} =$
- $\varepsilon_W = 2^{\circ} \deg$
- Using Λ , AR From Fig 4.46 $\Rightarrow \left(\frac{\Delta c_{l_{\beta}}}{\varepsilon_W \tan \Lambda_{c/4}}\right) =$
- Using $\frac{b_V}{2r_1}$, From Fig 13 $\Rightarrow k_{Y_V} =$
- $\eta_V \cdot \left(1 + \frac{d\sigma}{d\beta}\right) = 0.724 + 3.06 \frac{S_V/S}{1 + \cos(\Lambda_{c/4})} + 0.4 \frac{Z_W}{d} + 0.009 \cdot AR =$
- $X_V =$
- \bullet $Z_V =$
- \bullet $\alpha_1 =$
- \bullet d =
- \bullet $S_{P \to V} =$
- Using $\frac{Z_W}{d/2}$ and Fig. 4.8 to get $K_{int} =$
- $\eta_V =$
- $\bullet \ y_{R_I} = \qquad \Rightarrow \eta_I = \qquad \Rightarrow K_{R_I} =$
- $y_{R_F} = \Rightarrow \eta_F = \Rightarrow K_{R_F} =$
- $\Delta K_R =$
- $\frac{\bar{c}_{Rudder}}{\bar{c}_{Vert.Tail}} =$, using Fig. 4.26 $\tau_R =$
- \bullet $X_R =$
- $Z_R =$

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$$\bullet \ y_{A_I} = \qquad \Rightarrow \eta_I = \qquad \Rightarrow RME_I =$$

•
$$y_{A_O} = \Rightarrow \eta_O = \Rightarrow RME_O =$$

•
$$\Delta RME =$$

•
$$\beta = \beta_H = \sqrt{1 - mach^2} =$$

•
$$\Lambda_{\beta} =$$

•
$$k_A = \frac{{\left({{c_{l_\alpha }}} \right)_{WingSection}} \Big|_{Mach}}{2\pi} =$$

•
$$\frac{\beta \cdot AR}{k} =$$
 , Using $\Lambda_{\beta}, \frac{\beta \cdot AR}{k}, \lambda$ and Fig. 4.51

•
$$\frac{\bar{c}_{Aileron}}{\bar{c}_{Wing_{aileron}}} =$$
 , using Fig. 4.55 $\tau_A =$

•
$$l_{CG} =$$

•
$$l_B =$$

•
$$S_{B_S} =$$

•
$$Z_1 =$$

•
$$Z_2 =$$

•
$$Z_{max} =$$

$$\bullet$$
 $W_{max} =$

•
$$Re_{Fuselage} = \frac{V \times l_B}{v} =$$

• Using Fig. 4.68
$$K_N =$$

•
$$K_{Re_l} =$$

• Using Fig. 4.73,
$$\Delta K_{n_A} = K_{n_0} - K_{n_I} =$$

•
$$\frac{\beta \cdot AR}{k}, \Lambda_{\beta}, \lambda$$
using Fig's. 4.80 & 4.81 $RDP =$

$$\bullet \ k_{A_{H}} = \frac{\left. \left(c_{l_{\alpha_{H}}} \right)_{WingSection} \right|_{Mach} \cdot \beta_{H}}{2\pi} =$$

•
$$\Lambda_{\beta_H} =$$

•
$$\frac{\beta_H \cdot AR_H}{k_{A_H}}$$
, Λ_{β_H} , λ_H using Fig's. 4.80 & 4.81 $RDP_H =$

• B =
$$\sqrt{1 - Mach^2 \cos(\Lambda_{\frac{c}{4}})^2}$$
 =

•
$$C = \frac{\left[AR + 4\cos\left(\Lambda_{c/4}\right)\right]}{\left[AR \cdot B + 4\cos\left(\Lambda_{c/4}\right)\right]} \cdot \left\{\frac{AR \cdot B + \frac{1}{2}\left[AR \cdot B + 4\cos\left(\Lambda_{c/4}\right)\right] \cdot \tan^2\left(\Lambda_{c/4}\right)}{AR + \frac{1}{2}\left[AR + 4\cos\left(\Lambda_{c/4}\right)\right] \cdot \tan^2\left(\Lambda_{c/4}\right)}\right\} =$$

$$\bullet \left. \left(\frac{c_{np}}{c_{L_1}} \right) \right|_{\substack{\text{Mach} = 0 \\ C_L = 0}} = -\frac{1}{6} \cdot \frac{AR + 6\left(AR + \cos\left(\Lambda_{c/4}\right)\right) \cdot \left[\left(\bar{x}_{CG} - \bar{x}_{AC}\right) \frac{\tan\left(\Lambda_{c/4}\right)}{AR} + \frac{\tan^2\left(\Lambda_{c/4}\right)}{12} \right]}{\left(AR + \cos\left(\Lambda_{c/4}\right)\right)} = -\frac{1}{6} \cdot \frac{AR + 6\left(AR + \cos\left(\Lambda_{c/4}\right)\right) \cdot \left[\left(\bar{x}_{CG} - \bar{x}_{AC}\right) \frac{\tan\left(\Lambda_{c/4}\right)}{AR} + \frac{\tan^2\left(\Lambda_{c/4}\right)}{12} \right]}{\left(AR + \cos\left(\Lambda_{c/4}\right)\right)} = -\frac{1}{6} \cdot \frac{AR + 6\left(AR + \cos\left(\Lambda_{c/4}\right)\right) \cdot \left[\left(\bar{x}_{CG} - \bar{x}_{AC}\right) \frac{\tan\left(\Lambda_{c/4}\right)}{AR} + \frac{\tan^2\left(\Lambda_{c/4}\right)}{12} \right]}{\left(AR + \cos\left(\Lambda_{c/4}\right)\right)} = -\frac{1}{6} \cdot \frac{AR + 6\left(AR + \cos\left(\Lambda_{c/4}\right)\right) \cdot \left[\left(\bar{x}_{CG} - \bar{x}_{AC}\right) \frac{\tan\left(\Lambda_{c/4}\right)}{AR} + \frac{\tan^2\left(\Lambda_{c/4}\right)}{12} \right]}{\left(AR + \cos\left(\Lambda_{c/4}\right)\right)} = -\frac{1}{6} \cdot \frac{AR + 6\left(AR + \cos\left(\Lambda_{c/4}\right)\right) \cdot \left[\left(\bar{x}_{CG} - \bar{x}_{AC}\right) \frac{\tan\left(\Lambda_{c/4}\right)}{AR} + \frac{\tan^2\left(\Lambda_{c/4}\right)}{12} \right]}{\left(AR + \cos\left(\Lambda_{c/4}\right)\right)} = -\frac{1}{6} \cdot \frac{AR + 6\left(AR + \cos\left(\Lambda_{c/4}\right)\right) \cdot \left[\left(\bar{x}_{CG} - \bar{x}_{AC}\right) \frac{\tan\left(\Lambda_{c/4}\right)}{AR} + \frac{\tan^2\left(\Lambda_{c/4}\right)}{12} \right]}{\left(AR + \cos\left(\Lambda_{c/4}\right)\right)} = -\frac{1}{6} \cdot \frac{AR + 6\left(AR + \cos\left(\Lambda_{c/4}\right)\right) \cdot \left[\left(\bar{x}_{CG} - \bar{x}_{AC}\right) \frac{\tan\left(\Lambda_{c/4}\right)}{AR} + \frac{\tan^2\left(\Lambda_{c/4}\right)}{12} \right]}{\left(AR + \cos\left(\Lambda_{c/4}\right)\right)} = -\frac{1}{6} \cdot \frac{AR + 6\left(AR + \cos\left(\Lambda_{c/4}\right)\right) \cdot \left[\left(\bar{x}_{CG} - \bar{x}_{AC}\right) \frac{\tan\left(\Lambda_{c/4}\right)}{AR} + \frac{\tan^2\left(\Lambda_{c/4}\right)}{12} \right]}{\left(AR + \cos\left(\Lambda_{c/4}\right)\right)} = -\frac{1}{6} \cdot \frac{AR + 6\left(AR + \cos\left(\Lambda_{c/4}\right)\right)}{\left(AR + \cos\left(\Lambda_{c/4}\right)\right)} = -\frac{1}{6} \cdot \frac{AR + 6\left(AR + \cos\left(\Lambda_{c/4}\right) - \frac{\tan^2\left(\Lambda_{c/4}\right)}{AR} + \frac{\tan^2\left(\Lambda_{c/4}\right)}{$$

•
$$\lambda, AR$$
 and using Fig. 4.83 $\frac{\Delta c_{np}}{\varepsilon_W} =$



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$$\bullet \ D = \frac{1 + \frac{AR\left(1 - B^2\right)}{2B\left[AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)\right]} + \left[\frac{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)}{AR \cdot B + 4\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \left[\frac{AR + 2\cos\left(\Lambda_{c/4}\right)}{AR \cdot B + 4\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{8}} = \frac{1 + \frac{AR\left(1 - B^2\right)}{2B\left[AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)\right]} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR \cdot B + 2\cos\left(\Lambda_{c/4}\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR\left(1 - B^2\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR\left(1 - B^2\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{8}}{1 + \frac{AR\left(1 - B^2\right)}{AR\left(1 - B^2\right)} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{1 + \frac{AR\left(1 - B^2\right)}{AR\left(1 - B^2\right)}} \cdot \frac{\tan^2\left(\Lambda_{c/4}\right)}{1 + \frac{AR\left(1 - B^2\right)}{AR\left(1 - B^2\right$$

•
$$\lambda, AR, \Lambda_{\frac{c}{4}}$$
, using Fig. 4.85, $\left. \left(\frac{c_{lr}}{c_{L_1}} \right) \right|_{\substack{Mach=0 \ C_L=0}} =$

• λ, AR and using Fig. 4.87, $\frac{\Delta c_{l_r}}{\varepsilon_W} =$

Aerodynamic Parameters

•
$$C_{Y_{\beta}} =$$

•
$$C_{Y_{\delta_A}} =$$

•
$$C_{Y_{\delta_R}} =$$

•
$$C_{n_\beta} =$$

•
$$C_{n_{\delta_A}} =$$

•
$$C_{n_{\delta_R}} =$$

•
$$C_{l_{\beta}} =$$

•
$$C_{l_{\delta_A}} =$$

•
$$C_{l_{\delta_R}} =$$

•
$$C_{l_p} =$$

$$\bullet$$
 $C_{Y_p} =$

$$\bullet \ C_{n_p} =$$

•
$$C_{l_r} =$$

$$\bullet$$
 $C_{Y_r} =$

•
$$C_{n_r} =$$