

Regular Grammar in Discrete Mathematics

The regular languages can be generated by regular grammar. In regular grammar, the left-hand side always consists of a single non-terminal. The left side cannot have more than one non-terminal or any terminal variable. There can be a single terminal or a single terminal followed by a non-terminal on the right-hand side.

The production of regular grammar will be in the following form:

$$X \rightarrow xY$$
$$X \rightarrow x$$
$$X \rightarrow Yx$$

Where

X and Y are used to indicate the Variable (V).



'x' is used to indicate the string of terminals (T^*)

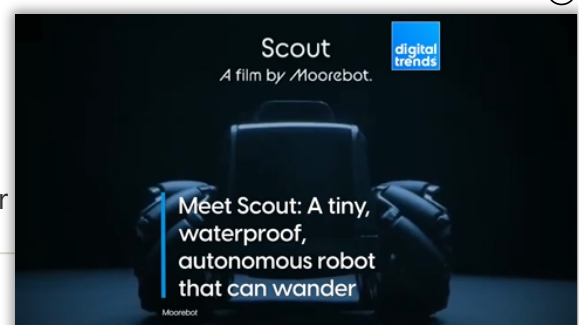
Types of Regular Grammar

There are two types of regular grammar, which are described as follows:

- Left Linear grammar (LLG)
- Right Linear Grammar (RLG)

Left Linear Grammar

The production must be in the following form in the left linear

$$X \rightarrow xY$$


$X \rightarrow x$

Where

X, Y belongs to a variable (V), and ' x ' belongs to T^* .

Right Linear Grammar

The production must be in the following form in the right linear grammar.

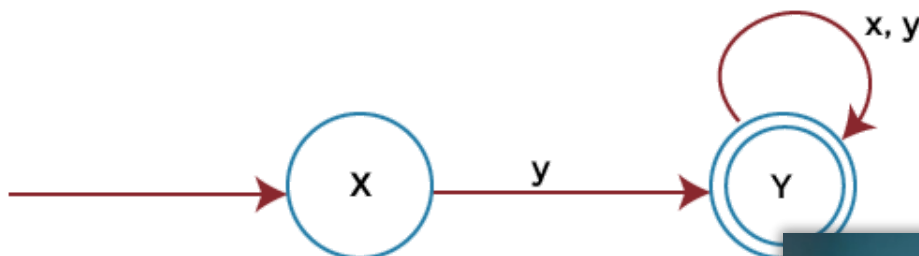
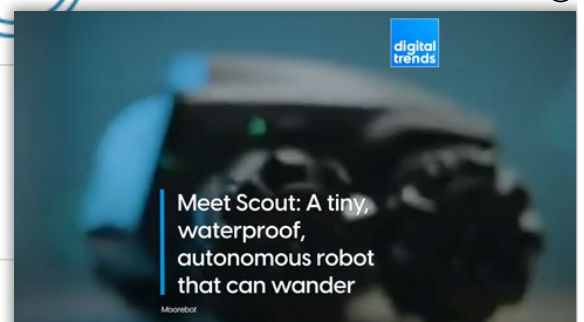
 $X \rightarrow Yx$ $X \rightarrow x$

Where

X, Y belongs to a variable (V), and ' x ' belongs to T^* .

The regular language can be described as a language that is generated by the type 3 grammar and for which finite automata can be designed. It is able to convert FA into type 3 grammar.

Example: In this example, we will show the finite automata accepting a string that begins with the symbol y .

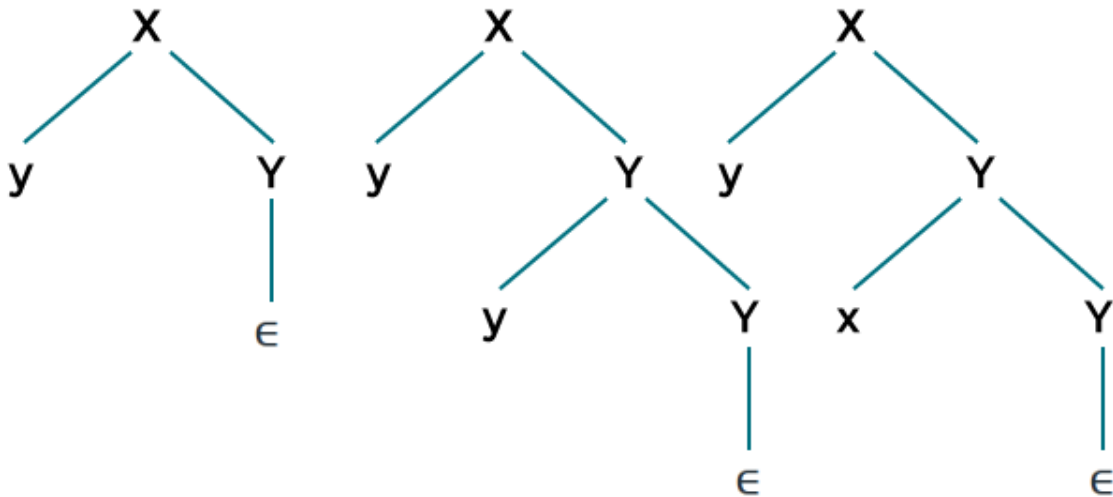
 $\Sigma = \{x, y\}$ Initial State (q_0) = X Final State (F) = Y 

The right linear grammar corresponding to FA is described as follows:

$$X \rightarrow yY$$

$$Y \rightarrow \epsilon/xY/yY$$

As we can see that the above grammar is right-linear grammar. This grammar can be written directly through finite automata.



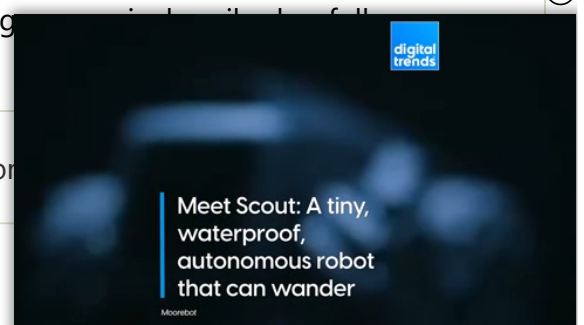
This grammar derives strings which are starting with B

A string can be generated with the help of above RLG, which begins with b. After that b, this string can accept any input symbol (i.e., $\Sigma = \{x, y\}$).

The regular language which corresponds to the right linear grammar is:

$$L = \{y, yx, yy, yxx, yxy, yyy, \dots\}$$

We will get the following grammar if we reverse the production

$$X \rightarrow Yy$$


$$Y \rightarrow \epsilon/Yx/Yy$$

This grammar derives the language that has all the strings that end with b, which is described as follows:

$$L' = \{y, yy, xy, xxy, yxy, xyy, yyy, \dots\}$$

In conclusion, we can say that suppose we have finite automata which represent language L , and we convert it into the right linear grammar, which also represents the same language L . In this case, when we reverse the RLG (right linear grammar), we will get the left linear grammar representing language L' , which is the reverse of L .

Conversion of RLG into LLG

The following steps will be used when we convert the right linear grammar into the left linear grammar for language L .

Step 1: For language L , we have to reverse the FA (Finite automata).

Step 2: After that, we have to write the right linear grammar for it.

Step 3: Now, we will reverse the RLG.

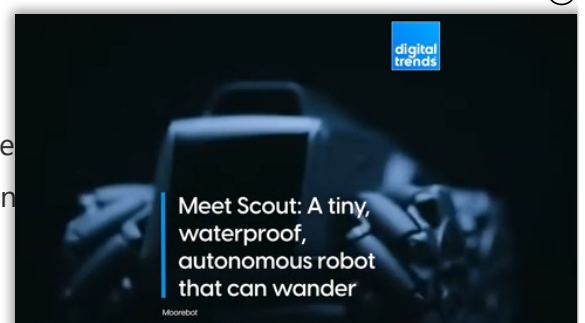
After step 3, we will get the grammar that generates the language, which is able to represent the left linear grammar for the same language L .



Here L is used to describe the language for FA (finite automata), and L^R is used to describe the reversal of language L .

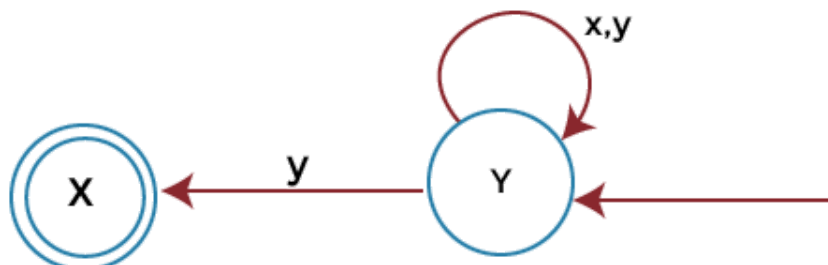
Example:

In this example, we will use the above finite automata representing string that begins with the symbol y . This language contains in convert this automata into the left linear grammar.



Solution:

Step 1: The reversal of finite automata is described as follows:



The reversal of FA that represent all strings starting with b.

Step 2: For this reversal FA, the corresponding right linear grammar is described as follows:

$$Y \rightarrow xY / yY / yX$$

$$X \rightarrow \epsilon$$

Step 3:

Now we will reverse the above right linear grammar and get the following grammar:

$$Y \rightarrow Yx / Yy / Xy$$

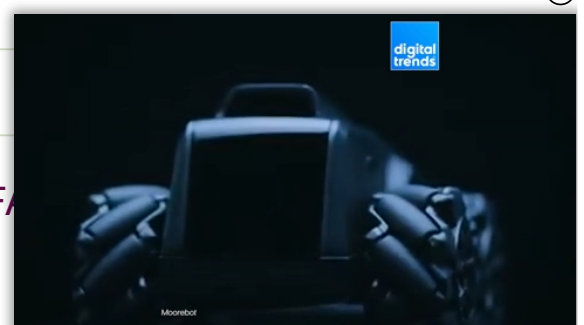
$$X \rightarrow \epsilon$$

So this grammar is left linear grammar, which is used to represent all string that begins with the symbol y. So

$$L = \{y, yx, yy, yxx, yxy, yyx, yyy, \dots\}$$

Conversion of RLG (Right linear grammar) to FA

We will begin from the first production.



From every left variable/alphabet, we will go to the symbol followed by it.

Start state: The first production state is known as the start state.

Final state: All the states which end up with terminals without following any further non-terminal.

Example:

In this example, we have the right linear grammar for language L. This grammar shows all the strings which end with 0.

$$X \rightarrow 0X / 1Y / 0Y$$

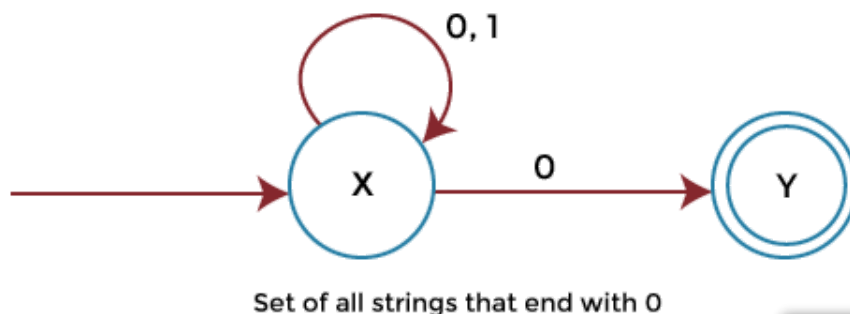
$$Y \rightarrow \epsilon$$

So the finite automata which correspond to right linear grammar are described as follows:

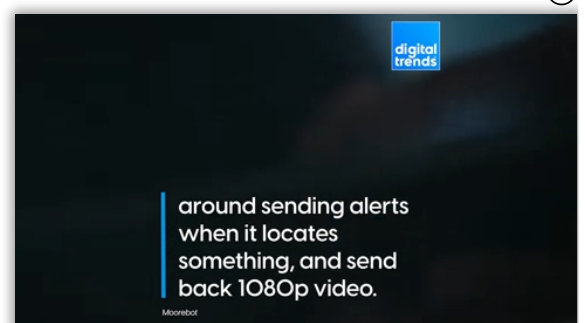
Here we will begin with variable X and use its production like this:

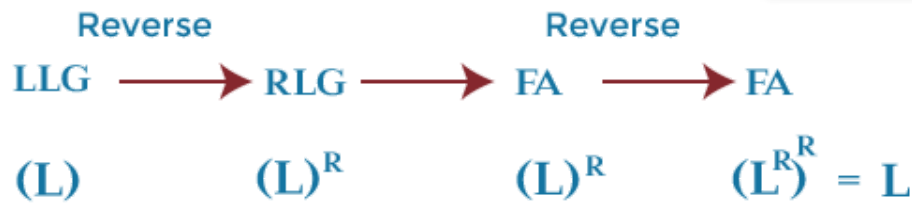
- The production $X \rightarrow 0X$ means that when the transition gets '0' as an input symbol, then state transition will always remain in the same state X.
- The production $X \rightarrow 1Y$ means that when the transition gets '1' as an input symbol, then the state transition will go to state Y from state X.
- The production $X \rightarrow 0Y$ means that when the transition gets '0' as an input symbol, then the state transition will go to state Y from state X.
- The production $Y \rightarrow \epsilon$ means that this state does not require any type of state transitions. In the corresponding FA (finite automata), this type of production would be the final state because its RHS is terminal.

So for the corresponding right linear grammar, the final NFA (nonfinite automat) is described as follows:



Conversion of LLG to FA:



**Explanation:**

Here we have first converted the LLG into the RLG grammar. Here LLG (Left linear grammar) represents the language L, which RLG (Right linear grammar) represents the reversal of language L, i.e., L^R . After that, we will design the FA corresponding to this reversal language (L^R). After that, we will reverse the finite automata (FA). The reversal FA is the final FA for language L.

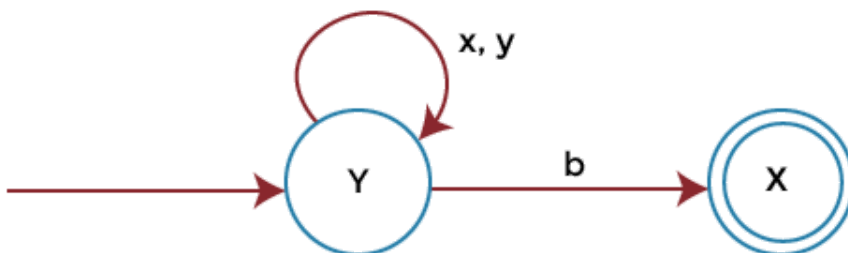
Conversion of LLG into RLG

To explain this, we will take the above grammar, which is used to represent the language L, and accept all sets of strings that begin with variable y. The left linear grammar for this grammar is described as follows:

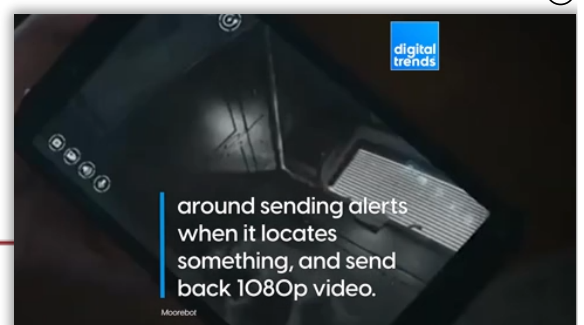
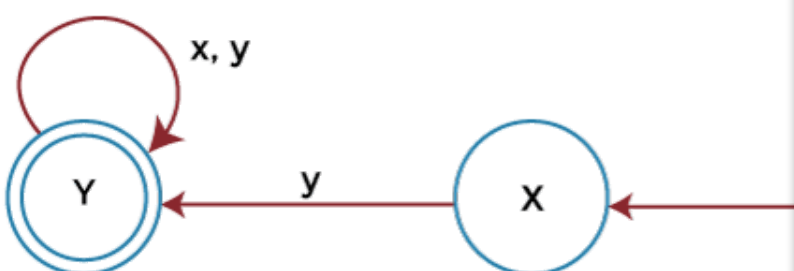
$Y \rightarrow Yx / Yy / Xy$
 $X \rightarrow \epsilon$

Step 1:

In this step, we will convert the LLG into FA. There is the same process of conversion as described above. So

**Step 2:**

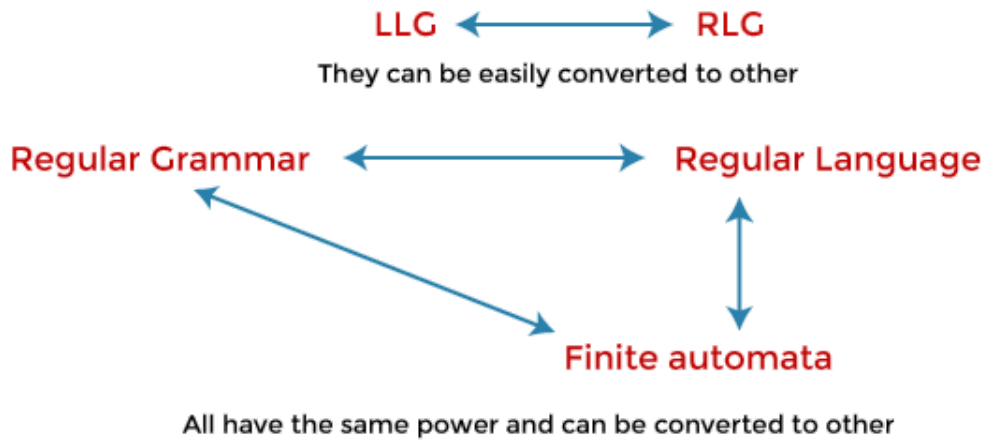
In this step, we will reverse the FA. That means we will convert the initial state into the final state and the final state into starting state. We will also reverse all the edges like this:



Step 3:

In this step, we will write RLG corresponding to reversed finite automata.

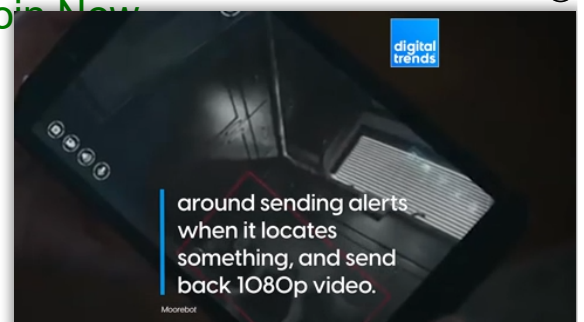
$$X \rightarrow yY$$

$$Y \rightarrow xY/yY/\epsilon$$

[< Prev](#)
[Next >](#)

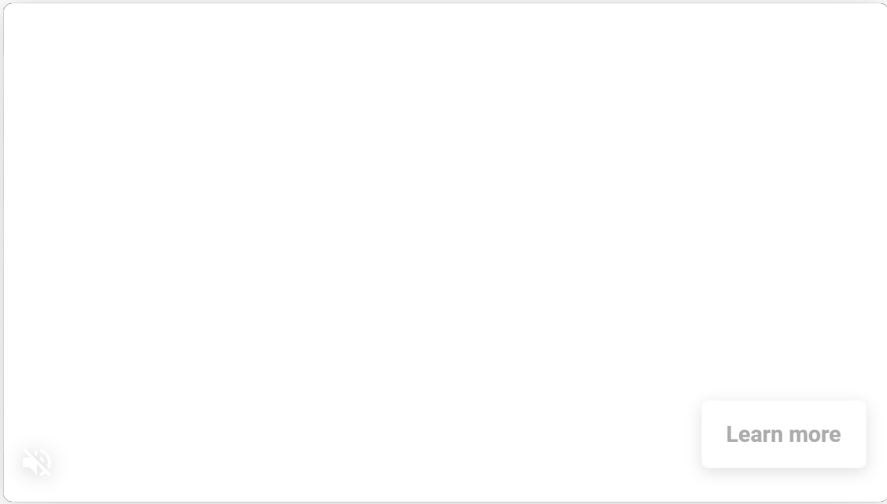

For Videos Join Our Youtube Channel: [Join Now](#)

Feedback

















- Send your Feedback to feedback@jvatpoint.com



Help Others, Please Share




Learn Latest Tutorials


 Splunk	 SPSS	 Swagger	 Transact-SQL
 Tumblr	 ReactJS	 Regex	 Reinforcement Learning
 R Programming tutorial R Programming	 RxJS tutorial RxJS	 React Native tutorial React Native	 Python Design Patterns Python Design Patterns
 Python Pillow tutorial Python Pillow	 Python Turtle tutorial Python Turtle	 Keras tutorial Keras	




Preparation




Aptitude
Aptitude




Logical Reasoning
Reasoning



Verbal Ability
Verbal Ability




Interview Questions
Interview Questions




Company Interview Questions
Company Questions


Trending Technologies




Artificial Intelligence Tutorial
Artificial Intelligence




AWS Tutorial
AWS




Selenium tutorial
Selenium




Cloud Computing tutorial
Cloud Computing




Hadoop tutorial
Hadoop




ReactJS Tutorial
ReactJS




Data Science Tutorial
Data Science




Angular 7 Tutorial
Angular 7




Blockchain Tutorial
Blockchain




Git Tutorial
Git




Machine Learning Tutorial
Machine Learning



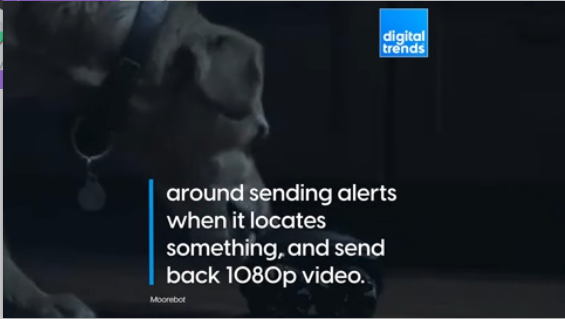
DevOps Tutorial
DevOps



SEMRUSH



Move your business forward with content marketing —





digital trends


around sending alerts when it locates something, and send back 1080p video.


B.Tech / MCA

 DBMS tutorial
DBMS

 Data Structures tutorial
Data Structures


 DAA tutorial
DAA

 Operating System tutorial
Operating System


 Computer Network tutorial
Computer Network

 Compiler Design tutorial
Compiler Design


 Computer Organization and Architecture
Computer Organization

 Discrete Mathematics Tutorial
Discrete Mathematics


 Ethical Hacking Tutorial
Ethical Hacking


 Computer Graphics Tutorial
Computer Graphics


 Software Engineering Tutorial
Software Engineering


 html tutorial
Web Technology


 Cyber Security tutorial
Cyber Security


 Automata Tutorial
Automata


 C Language tutorial
C Programming


 C++ tutorial
C++

 Java tutorial
Java

 .Net Framework tutorial
.Net

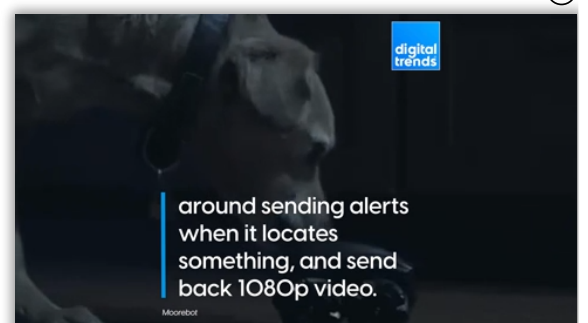
 Python tutorial
Python



 List of Programs
Programs

 Control Systems tutorial
Control System


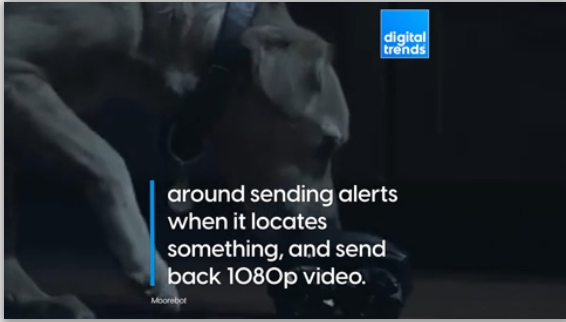
 Data Mining Tutorial
Data Mining

 Data Warehouse Tutorial
Data Warehouse





Move your business for
with content marketing -



around sending alerts
when it locates
something, and send
back 1080p video.

